Citizenship versus ethnicity: The role of institutions in shaping identity choice

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Abstract

This paper examines the role that political institutions play in inducing or subduing ethnic identification. I provide a formal model of ethnic identification as a function of institutional design and social context that focuses on one question: What kinds of institutions will induce individuals to identify with the state rather than along ethnic lines? Among other things, the model offers predictions about when political institutions are capable of inducing a national identity. I conclude with an application of the model to the question of institutional design in Iraq. The model provides one explanation for why a period of low Sunni representation in Iraqi government would increase sectarianism, and why a more proportional Iraqi parliament may not remedy the problem.
“Those who hold out hope for democracy in plural societies are virtually unanimous in their belief that institutional design is the key to avoiding disaster, with constitutional engineering, particularly of electoral systems, treated as an important lever.”


Political institutions are frequently invoked as an important means of resolving societal conflict. In the Federalist #10, Madison wrote of the need to mitigate the problem of “factions” by delegating the management of government to elected representatives. In more recent times experts have been called upon to design political systems to help ameliorate intergroup rivalries and tensions. Examples include the use of list proportional representation in post-apartheid South Africa, which some believe led to a successful multiethnic government there, and the use of the alternative vote in Sri Lanka, which others argue led to a moderation-inducing presidential system in a country with a long history of bitter ethnic conflict (Horowitz 2000a).1 Issues of intergroup conflict are also of relevance in established democracies, many of which have amended their electoral laws to ensure that a certain percentage of legislative seats go to women2 or ethnic minorities3, and that ban extremist parties from fielding candidates.4

This paper explores the role that institutional context plays in inducing or subduing ethnic identification. I begin with the observation that every individual simultaneously belongs to a large collection of groups, and yet we all choose, either consciously or subconsciously, to associate with
some groups more than others. If these choices are partly dependent on political context, then the questions of why we make associative choices and how these choices affect our political attitudes and preferences have important consequences for institutional design. In particular, the model I present will focus on one specific question in institutional design: What kinds of institutions will induce individuals to identify with the state rather than along ethnic lines?

A number of scholars have studied the effect of political and economic institutions on group identity. This literature by and large takes an instrumentalist and constructivist view of ethnicity: ethnic identities can emerge as a consequence of the conscious efforts of political elites to further their own goals, and ethnic identities can be socially constructed. This paper similarly takes the view that ethnic identities may be manipulated through political means. Rather than specifically modeling a political elite seeking to affect change, I instead construct a general framework for analyzing the effect of institutional change on ethnic identification across a society. The model represents a first step toward formalizing the underlying features of institutions that affect inter-group relations.

Specifically, I consider the case of a single state that is composed of a finite number of ethnic groups. Every individual belongs to one of these groups. Individuals choose whether to identify with their ethnic group or with the state as a whole, and these choices will affect individual preferences over policy. This captures a setting in which, for example, a man may think of himself as either Sunni or as an Iraqi, and each choice will imply a different utility function for him. Identification with a group implies that the individual cares about the well-being of the group, and thus exhibits bias toward the group. The conception of identity as entailing an ingroup bias is motivated
by a large literature in social psychology that defines identification with a group as yielding "a shift towards the perception of the self as an interchangeable exemplar of some social category and away from the perception of the self as a unique person" (Turner et al. 1987, p. 50).

Individual identity choices will depend upon the realized well-being, or status, of each group. Individuals, either consciously or subconsciously, choose an identity that yields the highest payoff given the particular situation at hand. This framework is compatible with the notion of "situational selection," the idea that while ethnic groupings may be fixed, ethnic identification can depend in part on situational forces (Bates 2006; Melson 1971; Melson and Wolpe 1970). In this paper, identities are activated by a situation consisting of both political institutions and the social context that individuals live within. The "social context" I consider is composed of the collection of groups within society, the distribution of individual preferences over policies, and the distribution of wealth across social groups.6

While the question of "How to induce universalism over ethnocentrism?" is purposefully narrow, this paper provides a tractable analytic approach to modeling identity choice as a function of the composition of society. Varying the size and number of ethnic groups, the distribution of preferences across and within ethnic groups, and the wealth of groups, the model is capable of making predictions about:

1. When political institutions are and are not capable of inducing a national identity

2. When economic aid and/or redistribution is capable of inducing a national identity

3. The types of societies that are most prone to strong ethnic identities
4. The types of groups an institution should favor when the institutional goal is to induce identification with the state.

The question of whether ethnic identification is beneficial or detrimental to democracy is obviously complex. There are clearly situations in which strong ethnic identities can be beneficial to the state as a whole, or in which strong state identification might be detrimental to society. Ethnic identities may mobilize individuals to become politically involved, give individuals a sense of social responsibility, and provide strong social networks. However, it is also generally acknowledged that strong and heterogeneous ethnic identities within a state can result in a political system that is dominated by a single group, leading to the permanent exclusion of other groups from the political realm. This view is predicated on an assumption that fluid majorities and minorities are essential to stable democracies, and thus, that ethnic diversity poses a particular challenge to democracy (Horowitz 2000b, p. 84; Rabushka and Shepsle 1972, p. 217). The motivation behind this paper is simply the observation that increased ethnic identification has been concordant with increased sectarian violence in some important instances, although by no means all instances. Thus, when I describe the institutional goal of inducing “identification with the state” I am specifically considering the goal of inducing a civic nationalism, universalism, or simply what Elkins and Sides (2007) refer to as “state attachment,” in which citizens possess some ethic of the common good.7

The paper proceeds as follows: I first present the formal model of group identification and political institutions, and the equilibrium concept, which is derived from recent work by Shayo (2007). I then discuss several analytic implications of the model, including comparative statics and implications for institutional design. Next, I present an application of the model to the question of
institutional design in Iraq, a setting in which there are three distinct ethnic groups with varying preferences over the degree of state secularism, and individuals face a trade-off between ethnic self-assertion and nationalistic identity. This section presents one explanation for the question of why a period of low Sunni representation in Iraqi government could increase sectarianism. The final section concludes.

The Model

Society contains a finite collection of ethnic groups. Every individual belongs to one such group, but may choose whether to identify with his ethnic group or with the state as a whole. Thus, ethnic groupings are fixed, but identities are not. Individual choices over identities affect the preferences of individuals, and thus affect any choice of policy made by society.

Individual decisions will be driven by three main factors: the social context that individuals reside within, the effect of identity choice on individual utility, and the political institution that collective decisions are made through. The following three sections define these concepts.

Social context

I use the term social context to refer to the environment in which all individuals live and interact within. Formally, social context will consist of three elements: the collection of ethnic groups within the state, the distribution of individual preferences within and across these groups, and the distribution of wealth across groups.
To begin, society consists of a single state, $N$, containing a continuum of citizens, or individuals. Each individual is indexed by a real number $i$ on the $[0, 1]$ interval. The policy space is assumed to be a compact and convex subset of the real line $X \subseteq \mathbb{R}$.

Within the state there are a finite number of ethnic groups, $g_1, \ldots, g_k$. Every individual in the state belongs to one of these groups. The groups may be of different sizes, with $\alpha_g$ denoting the percentage of the population in group $g$. The groups may also be differentially wealthy, with some groups richer than others. Let $c_g \in \mathbb{R}_+$ be a constant denoting the wealth of group $g$. I use the term $\bar{c} = \sum_g \alpha_g c_g$ to represent “national wealth,” the average wealth of a citizen of the state.

Let $g^i$ denote the ethnic group that citizen $i$ belongs to. Following the terminology in Shayo (2007), the personal preferences of citizens are described by a quadratic material payoff function, $\pi_i(x) = c_{g^i} - (p_i - x)^2$, where $p_i \in X$ is citizen $i$'s ideal point. Thus, citizens that belong to wealthy groups will have higher realizations of their material payoff functions, ceteris paribus. This captures the idea that members of certain groups may have a material advantage over members of other groups, irrespective of policy $x$.

For each group $g$ the ideal points of the citizens belonging to $g$ are distributed according to an atomless probability density $f_g$ over $\mathbb{R}$, with cumulative density $F_g$. The total distribution of ideal points across society is then the convex combination of the group distributions: $f_N = \sum_g \alpha_g f_g$, with cumulative density $F_N$. 
The effect of identity choice

I assume that when an individual identifies with a group he cares about the well-being of that group, and exhibits a particular type of bias towards that group. This ingroup bias could stem from a “common fate” conception of group identity in which the individual perceives his payoff to be linked to the payoffs of others in his group (Rabbie et al. 1989). Or it could stem from the notion that individuals seek a “positive distinctiveness,” or an advantage for the ingroup over relevant outgroups. This would correspond to a conception of group identification based on social identity theory, which posits that the evaluation of any group depends on its standing relative to other groups, and that individuals may choose to identify with higher-status groups in order to enhance their self-esteem (Tajfel and Turner 1986).9

Throughout, I will use the average material payoff of a group to represent the well-being of that group. Let the average material payoff of a member of ethnic group \( g \) at policy \( x \) be denoted

\[
\mu_g(x) = \int_{i \in g} \pi_i(x) dF_g(p_i).
\]

Similarly, let the average material payoff of the nation be

\[
\mu_N(x) = \int \pi_i(x) dF_N(p_i).
\]

Relative group comparisons With the exception of Theorem 1 (an equilibrium existence result), all of the results that follow will depend on an assumption that individuals care about the well-being of their group relative to other groups. A justification of the use of this assumption in this context stems from Horowitz’s argument that ethnic comparisons form the basis of conflict in many states, with the comparison between backwards and advanced groups being particularly salient (Horowitz 2000b, pp. 143-149). Horowitz refers to this type of identification as stemming from a fundamental
tendency of individuals to “cleave and compare.” Furthermore, he notes that the presence of a third party, such as a colonizer, can play a significant role in these intergroup comparisons by stoking intergroup rivalries (Horowitz 2000b, p. 165).

In Penn (2008) I relax the assumption that individuals evaluate their group’s status relative to other groups. Specifically, I examine several different forms of ingroup bias and show that when ethnic identification simply grants individuals level status effects based on the absolute status of their group – as opposed to relative status effects in which individuals seek positive distinctiveness for their group – it is impossible to induce a situation in which all individuals identify with the state. This result says that a national identity may not be possible without the potential for rivalry between politically relevant subgroups.10

The following paragraphs formally define the notion of identity that I invoke. An action $a_i \in \{g^i, N\}$ for individual $i$ is a choice of identity, or self-categorization. Individuals can choose to identify either with their ethnic group ($a_i = g^i$) or with the state ($a_i = N$).11 Individuals may also choose to identify with both groups. Let $i$’s strategy space be $\Sigma_i$, the set of probability distributions over $\{g^i, N\}$. A mixed strategy for player $i$, $s_i$, is an element of $\Sigma_i$, with $s_i(a_i)$ being the probability that $s_i$ assigns to action $a_i$. Thus, $s_i(g^i) = .5$ and $s_i(N) = .5$ implies that player $i$ identifies equally with both the nation and his ethnic group.12

At any fixed policy $x \in X$, individuals receive utility from both policy outcome $x$ and from their choice of identity, $s_i$. Furthermore, individuals receive utility from an interaction between these two variables, because any given policy outcome may affect different groups differently, and individuals care about the well-being of the group that they choose to identify with. Specifically,
Player $i$’s utility from strategy $g^i$ at policy $x \in X$ is

$$u_i(x, g^i) = \pi_i(x) + \gamma \sum_{g \neq g^i} (\mu_{g^i}(x) - \mu_g(x)),$$

or $i$’s material payoff $\pi_i(x)$ plus a term representing the status of $i$’s ethnic group relative to other groups in society: $\gamma \sum_{g \neq g^i} (\mu_{g^i}(x) - \mu_g(x))$, where $\gamma > 0$ is the weight individuals assign to their identity choice.

This conception of status is similarly used in Shayo (2007) and, as discussed earlier in this section, is consistent with group identification being based on a desire for positive distinctiveness in the vein of social identity theory. Utility increases as the average well-being of a member of one’s own ethnic group increases. However, utility is decreasing in the average well-being of members of other ethnic groups.

When individuals identify with the nation, relative comparisons have a different meaning because I am considering solely domestic policies, or policies that do not directly affect citizens of other nations. In particular, I assume that any term representing the status of another nation would be a constant, and I will normalize this constant to zero. $^{13}$ Player $i$’s utility from strategy $N$ at policy $x \in X$ is

$$u_i(x, N) = \pi_i(x) + \gamma \mu_N(x),$$

or $i$’s material payoff $\pi_i(x)$ plus a term that simply represents the well-being of the nation. Thus, utility increases as the average well-being of a citizen of the nation increases. It follows that Player $i$’s utility from mixed strategy $s_i$ at policy $x \in X$ is

$$u_i(x, s_i) = \pi_i(x) + \gamma \left( s_i(g^i) \sum_{g \neq g^i} (\mu_{g^i}(x) - \mu_g(x)) + s_i(N)\mu_N(x) \right),$$

$^{14}$
Political institutions

Political institutions in this model govern how the preferences of different societal groups are aggregated into policy. If an institution favors one group over another, then the policy preferences of members of the favored group are weighed more heavily in determining national policy. Intuitively, we can think of an institutionally favored group as being more capable of winning legislative seats. The voting weight given to a group by a given institution may be a function of many different factors, the most obvious of which is the electoral formula used within the institution. However, other characteristics of a political institution can also affect proportionality; examples include minimum electoral thresholds, district boundaries, ballot structure, voting and candidacy requirements, and access to the media. Thus, political institutions are not necessarily equivalent to electoral rules.

Formally, a political institution is a collection of weights \( \rho = (\rho_1, \ldots, \rho_k) \) assigned to ethnic groups \( g_1, \ldots, g_k \) such that \( \sum_j \rho_j = 1 \). Thus, the institution represents the composition of parliament with respect to the various ethnic groups. Since the policy space is one-dimensional and individual preferences are single-peaked, the policy outcome will be the weighted median, an outcome that would be derived by a majoritarian process of intra-legislative bargaining assuming the legislature is composed according to \( \rho \).

Before defining the concept of a weighted median, note that \( i \)'s utility function is single-peaked for any choice of identity \( s_i \) by \( i \). Let \( n_i(s_i) \) be \( i \)'s utility-maximizing policy when \( i \) chooses identity \( s_i \), or the peak of of \( u_i \).

**Definition 1** At strategy profile \( s \) let \( f_g(n_i(s_i)) \) be the distribution of group \( g \) voters’ utility-
maximizing policies. For a given institution $\rho$, a weighted median is a policy $x(\rho, s_i) \in X$ that satisfies the following:

$$\int_{-\infty}^{x(\rho, s_i)} \sum_g \rho_g dF_g(n_i(s_i)) = \frac{1}{2}.$$ 

In words, a weighted median is a policy outcome equal to the median of the distribution of voter utility-maximizing policies, when the preferences of members of each group are weighted according to $\rho$. We can interpret institutions in this model as representing governments in which each group $g$ wins a percentage $\rho_g$ of legislative seats, legislators are responsive to the preferences of their constituents, and legislative voting occurs through majority rule.

This conception of institutions as representation schemes is in keeping with a vein of literature on comparative electoral systems that studies the proportionality profiles of different systems. Highly proportional electoral systems minimize the distortion between the percentage of votes a party wins and the percentage of seats it gets in parliament. Measures of proportionality such as the Gallagher index are commonly used to evaluate different electoral systems, with the general finding being that majoritarian and plurality systems are the least proportional, and the list systems of proportional representation the most proportional. While these measures are imperfect, they provide a clean, one-dimensional way of evaluating and comparing different real-world institutions.

Finally, note that an institution biases policy in favor of particular groups regardless of whether individuals choose to identify with those groups or not. An example is the institutional norm in some countries of staggering male and female candidates on party lists (a practice called “zip-
ping”), in order to ensure that a certain number of female candidates win seats. This institution can be regarded as biasing policy outcomes toward the interests of women, regardless of whether women choose to identify with “women” as a group.

**Equilibrium concept**

The equilibrium concept is a variant of *social identity equilibrium*, defined in Shayo (2007). At equilibrium, people choose to associate with the group that maximizes their utility out of the set of groups that they possibly *could* associate with. When people associate with such groups, and make decisions based upon their group identification, they still want to retain that group identification. Equilibrium is a collection of group identifications $s^*$ and a policy $x^*$ that satisfy this property. The following definition formalizes this idea.

**Definition 2** At a fixed institution $\rho$, a social identity equilibrium is a policy $x^*$ and collection of identities $s^*$ such that the following two conditions hold:

1. For all $i \in N$, $s^*_i \in \text{argmax}_{s_i \in \Sigma_i} u_i(x^*, s_i)$

2. $x^* = x(\rho, s^*)$, the weighted median induced by institution $\rho$ and strategy profile $s^*$.

The first condition says that in equilibrium no individual wants to deviate from his choice of group identity $s^*_i$ at equilibrium policy $x^*$. The second condition implies that policy $x^*$ is indeed the median policy induced by $\rho$ under strategy profile $s^*$.

Theorem 1 proves that there exists a social identity equilibrium, possibly in mixed strategies. The theorem is proved for a general version of this model in which the policy space is multidimen-
sional, individuals may simultaneously belong to many different groups, and the only assumption
made on individual utility functions is continuity. In particular, the proof of this theorem allows for
many different conceptions of ingroup bias by allowing for the general inclusion of an “identity”
term in the utility function as in Akerlof & Kranton (2000). Moreover, this term need not specifically be bias; it could, for example, represent valence. However, a important difference between
this model and the models of Akerlof and Kranton (2000), Dickson & Scheve (2006), and Dickson
(2006) is that the identity term I require is group-specific rather than individual-specific. Theorem
1 and its proof are relegated to the Appendix.

Results

The assumptions made in the previous section have several useful implications. The first is that,
at a given policy \( x \in X \), an individual will choose to identify with his ethnic group \( g^i \) if and
only if \( \sum_{g \neq g^i} \mu_{g^i}(x) - \mu_g(x) > \mu_N(x) \), and will choose a nationalistic identity if and only if
\( \mu_N(x) > \sum_{g \neq g^i} \mu_{g^i}(x) - \mu_g(x) \). Thus, when two individuals \( i \) and \( i' \) are members of the same
ethnic group then they will choose the same identity unless they are indifferent between the two
choices. For simplicity I will assume that when individuals are indifferent between identity choices
they identify nationally. A second useful implication is that ethnic identification simply shifts an
individual’s utility-maximizing policy to either the right or left of his ideal point by a fixed amount.
This is a consequence of the quadratic specification of \( \pi \). Let \( \overline{\pi}_g \) denote the expected ideal point
(or material payoff-maximizing policy) of a member of group $g$, so that

$$\overline{p}_g = \int_{i \in g} p_idF_g(p_i).$$

Similarly, let

$$\overline{p}^2_g = \int_{i \in g} p^2_idF_g(p_i)$$

and define $\overline{p}_N$ and $\overline{p}^2_N$ similarly. If individual $i$ identifies with $g^i$ then his utility is maximized at policy $n_i(g^i) = p_i + \gamma \sum_{g \neq g^i}(\overline{p}_{g^i} - \overline{p}_g)$. If an individual chooses a nationalistic identity then his utility is maximized at policy $n_i(N) = (p_i + \gamma \overline{p}_N)/1 + \gamma$. This implies that nationalistic identities will always shift individuals’ ideal points toward the mean of the state; conversely, ethnic identities will likely make groups appear more polarized.

Note that the variance in the distribution of ideal points of members of group $g$, written $\sigma^2_g$, equals $\overline{p}^2_g - (\overline{p}_g)^2$. Using the previous definitions of $\mu_g$ and $\mu_N$ we now get that if a pure-strategy equilibrium exists at a given institution $\rho$ it can be characterized by the following: \(^{17}\)

$$a^*_i = \begin{cases} 
N & \text{if } x^* \in \left[ \sum_{g \neq g^i} (\overline{p}_g - \overline{p}_{g^i}) + \overline{p}_N - K, \sum_{g \neq g^i} (\overline{p}_g - \overline{p}_{g^i}) + \overline{p}_N + K \right] \\
g^i & \text{otherwise,}
\end{cases}$$

(1)

where

$$K = \sqrt{\left[ \sum_{g \neq g^i} (\overline{p}_g - \overline{p}_{g^i}) - \overline{p}_N \right]^2 - \left[ \overline{p}^2_N - \overline{\tau} + \sigma^2_N + \sum_{g \neq g^i} ((c_{g^i} - c_g) - (\sigma^2_{g^i} + \overline{p}^2_{g^i}) + (\sigma^2_g + \overline{p}^2_g)) \right]}.$$
following section presents several observations that provide intuition for how this interval increases and decreases as a function of social context.

**Ethnic identification as a function of social context**

This section examines the dynamics of individual identity choice as a function of social context. For the moment I will leave institutions abstract in order to enable us to assess the feasibility of certain types of equilibria under any institution. The following observations follow immediately from this specification of the model (i.e. quadratic material payoffs and the assumed functional form of identity), and show that the parameterization of society in terms of the means, variances, sizes, and wealth of the existing groups will affect the types of equilibria that are possible. For example, under certain parameter values it will be impossible to induce an “all nationalistic” equilibrium under any political institution. Formalizations of these observations can be found in the Appendix.

**Observation 1** *It is not always possible to induce an “all nationalistic” equilibrium. It is always possible to produce a situation in which \( a_i = g^i \) for all \( i \in N \) (all individuals identify ethnically) provided that “undemocratic” policy outcomes may be realized.*

To see that it will not always be possible to construct an equilibrium in which every individual identifies with the nation, note that it is easy to construct examples in which members of a particular ethnic group will *never* identify with the nation (i.e. when the “K” interval for a group is not a real number). Such an example is provided in the Appendix.
Conversely, all members of a group will choose an ethnic identity if policy is outside of a closed and bounded interval of the real line. Since there are a finite number of groups there is an upper and lower bound of the real line beyond which all groups will pursue an ethnic identity. If one of these bounds lies within the policy space then an ethnic equilibrium can always be induced by fixing policy beyond that bound, although it may not be inducible through the use of a weighted median voter rule. This reflects the idea that if policy is unresponsive to the preferences of voters and extreme enough (in the sense of hurting all groups) then all individuals will identify ethnically. This could occur, for example, as the result of a negative political or economic shock such as a famine or war. The observation is consistent with recent work by Brancati (2007) who shows that natural disasters create and intensify within-state conflicts.

**Observation 2** *Individuals will be more likely to identify with their ethnic group as it becomes more homogenous, and as its rival groups become less homogenous (with homogeneity defined in terms of variance).*

This observation follows immediately from the equilibrium conditions defined in Equation 1. The interval of policies at which an individual $i$ will identify nationally shrinks as the variance of group $g^i$ decreases and shrinks as the variance of competing groups increases, ceteris paribus.\(^{18}\) This observation does not depend specifically on quadratic material payoff functions, but does depend on the concavity of these functions in ideal points $p_i$.\(^{19}\) With general concave functions then group homogeneity must be defined in terms of second order stochastic dominance for this observation to hold generally: it follows directly from the definition of a mean-preserving spread and Jensen’s
inequality. The following figure graphically depicts this observation for the case of two groups.

**Figure 1**

Figure 1 depicts a baseline situation in which there are two ethnic groups, $L$ and $R$ of the same size and same wealth ($c_L = c_R = 4$). The ideal points of members of both groups are distributed normally, with Group $L$ having mean $\bar{p}_L = -1$ and Group $R$ having mean $\bar{p}_R = 1$. The figure shows the intervals of policies at which each group will identify nationally while varying the variance of $R$. As $\sigma^2_R$ increases, there are more policies at which members of $R$ will identify nationally, and fewer policies at which members of $L$ will identify nationally. The darkly shaded regions represent intersections of the groups’ nationalistic identification intervals—policies at which members of both groups will identify nationally.

Observation 2 is consistent with a vast body of literature in social psychology, and in particular social identity theory, which posits that individuals value group identification more highly the more similar they are to other members of their group (Tajfel and Turner 1986). It could also be loosely interpreted as explaining the persistent finding that identification is less likely in large groups, which may be more heterogeneous. This observation also has interesting implications that could be applied to more strategic settings. It suggests that under certain circumstances groups may have an incentive to pretend that they are more cohesive than they actually are, in order to induce other groups to not identify ethnically by making those groups appear comparatively less cohesive.

The next observation considers situation in which the state as a whole becomes richer or poorer, while the relative wealth of all groups remains unchanged.
Observation 3 When groups are not too dissimilar in wealth then a uniform increase in national wealth decreases the likelihood that members of all groups will identify ethnically. When groups are very dissimilar then the effect of increasing national wealth is ambiguous.

Recall that the wealth of group \( g, c_g \), is simply an additive constant in the material payoff functions of all members of group \( g \). National wealth is the average of these terms: \( \bar{c} = \sum_g \alpha_g c_g \). It is clear from Equation 1 that if \( c_g = c_g \) for all groups \( g \) then the interval of policies at which individual \( i \) will identify nationally increases as \( \bar{c} \) increases. Because of the continuity of this interval in \( c^i_g \), this interval will still be increasing in \( \bar{c} \) when \( c_g \) are close for all \( g \). Again, the following figure demonstrates this observation for the case of two groups.

**Figure 2 here**

Figure 2 depicts the effect of increasing national wealth \( (\bar{c} = \frac{1}{2}c_L + \frac{1}{2}c_R) \) in two cases. Again, both groups are distributed normally with \( \bar{p}_L = -1, \bar{p}_R = 1 \), and \( \sigma^2_L = \sigma^2_R = 1 \). The left graph shows the effect of an increase in \( \bar{c} \) in the baseline case where the wealth of both groups is the same. The right graph shows the effect of increasing \( \bar{c} \) when the wealth of \( R \) is four times that of \( L \). In the former case the interval of policies at which each group identifies nationally is always increasing in \( \bar{c} \). In the latter case this interval is increasing for \( L \) and decreasing for \( R \). Ultimately, for a high enough \( \bar{c} \) this interval will disappear completely for group \( R \).

It is not difficult to precisely characterize how different these wealth terms can be for an increase in national wealth to reduce the likelihood of ethnic identification for all individuals. Let \( g \) be the richest group (i.e. \( c_g \geq c_h \) for all \( h \neq g \)). For all groups \( h \), let \( c_g = \beta_h \times c_h \). Since \( g \) is
the richest group, $\beta_h \geq 1$ for all $h$, and $\beta_g = 1$. Then a sufficient condition for an increase in $\bar{c}$ to increase the range of policies at which all individuals identify nationally is that $\alpha_h + 1 \geq \beta_h$ for all groups $h$.

This observation suggests that, in addition to utilizing political institutions as a means of promoting non-ethnic identification, it may also be beneficial to design economic institutions that equalize material advantage across groups and that increase the material advantage of all citizens. However, if ethnic groups are too unequal in wealth then increasing the overall wealth of the nation may actually incite ethnic identification. Thus, the effect of national wealth on ethnic identification will vary depending on wealth inequality across groups. Specifically, this is because an increase in the wealth of the nation benefits wealthier groups more in absolute terms than it does poorer groups. This result has a direct link to literature on modernization and relative deprivation. If we conceive of the wealth of a group as a measure of its degree of social mobilization (Deutsch 1961), or integration into the modern sector, then this observation provides one formalization of the claim by modernization scholars that different degrees of modernization among groups will exacerbate intergroup conflicts by multiplying the effects of existing social cleavages.\footnote{This observation also leads immediately to the following implication of the model.}

**Corollary 1** While political institutions are not always capable of inducing an “all nationalistic” equilibrium, certain economic institutions are.

This follows directly from the fact that when the wealth of all groups is equalized then the interval of policies on which each group identifies with the nation is increasing in the wealth of the nation, $\bar{c}$.\footnote{This result has a direct link to literature on modernization and relative deprivation. If we conceive of the wealth of a group as a measure of its degree of social mobilization (Deutsch 1961), or integration into the modern sector, then this observation provides one formalization of the claim by modernization scholars that different degrees of modernization among groups will exacerbate intergroup conflicts by multiplying the effects of existing social cleavages.\footnote{This observation also leads immediately to the following implication of the model.}}
Thus, a national identity can always be induced by equalizing wealth across groups and uniformly increasing the wealth of the state as a whole.

**Institutional design**

Using some of the intuition gained from the previous section we can characterize certain desirable properties of institutions in terms of the policies they produce. The particular property I will focus on is the robustness of individual identifications to policy shocks. For example, if an equilibrium is possible in which all individuals identify nationally we may want to ensure that we can stay at that equilibrium even if there is a small, exogenous shock to policy. The following informal definition of a *social point* captures this idea.

**Definition 3** Suppose that there exists an equilibrium in which \( a_i = N \) for all \( i \). Then the social point is a policy \( x^* \) that maximizes the distance that policy would need to shift before any individual would deviate to strategy \( a_i = g_i \).

In terms of the figures presented in the previous section, the social point is the midpoint of the interval of policies on which all groups choose to identify nationally. Indeed, the results from the previous section can be reinterpreted in terms of the social point and the weighted median voter rule that induces it, as the following observation demonstrates. A formalization of this observation can be found in the Appendix.

**Observation 4** In a two-group setting, a weighted median voter rule that induces the social point
will favor heterogeneous groups over homogeneous ones and poor groups over wealthy ones, ceteris paribus.

This observation follows immediately from Observations 2 and 3 and the fact that at any equilibrium $a^*$ such that $a_i^* = N$ for all $i$, the weighted median $x(a^*)$ is moving toward the point $x = \frac{\bar{p}_g + \gamma \bar{p}_N}{1+\gamma}$ (the median utility-maximizing policy of a member of $g$) as voting weight $\rho_g$ increases.

Suppose there are two groups, $L$ and $R$, with $\bar{p}_N = 0$ and $\bar{p}_L < 0 < \bar{p}_R$. Equation 1 implies that the interval of policies at which group $L$ identifies nationally is always centered at $\bar{p}_R - \bar{p}_L$. Therefore, increasing the variance of group $L$ will shift the social point away from $\bar{p}_R - \bar{p}_L$ and toward $\bar{p}_L - \bar{p}_R$, as Figure 1 showed. This shift implies a shift toward the utility-maximizing point of the median member of $L$, and thus, will correspond to a higher voting weight $\rho_L$ given to Group $L$.

To see that the institution will favor poor groups over wealthy groups the same intuition can be used. Decreasing the wealth of $L$ will increase the size of the interval on which members of $L$ will identify nationally, and shrink the size of the interval on which members of $R$ will identify nationally. Again, this will correspond to a shift in the social point toward the utility-maximizing point of the median member of $L$. The following section provides a more applied look at the question of institutional design, focusing on recent institutional changes in Iraq.
An application to the case of Iraq

“Of all the changes that have swept Iraqi society since the American invasion almost three years ago, one of the quieter ones, yet also one of the most profound, has been the increased identification with one’s own sect.”

In January 2005 United Nations electoral specialist Carina Perelli decided upon a single-district list system of proportional representation for the first Iraqi legislative election. Perelli’s rationale was driven in large part by concerns that the new system fully represent Iraq’s ethnic diversity while not aggravating ethnic tensions. Perelli argued that a single district would reduce regional factions and tribalism while allowing for the possibility of historically repressed and displaced “communities of interest” to accumulate their votes (Iraqi Coalition Provisional Authority Briefing 2004). However, low Sunni turnout posed one challenge to the legitimacy of the election; the largest Sunni party received only 1.78% of the vote, while Sunnis are believed to comprise over 20% of the Iraqi population. For the second legislative election in December 2005 Iraq’s 230 legislative seats were apportioned among 18 provinces. The change from a single district to a system of 18 districts was carried out in the hope that Sunni Arabs would win a significant number of seats in those provinces in which they were a majority.

From a distributional standpoint the second election was a success; each of Iraq’s three major communities (Shiite, Sunni and Kurd)²² received shares of legislative seats that were roughly proportional to their group’s size.²³ However, it is unclear whether a more proportional allocation of legislative seats will translate into a more peaceful Iraq. Reports of Shiite death squads and a spate of bombings in early 2006 raised fears of renewed sectarian violence. Addressing reports of Shiite
death squads, Iraq’s American ambassador, Zalmay Khalilzad, said “We are not going to invest the resources of the American people to build forces run by people who are sectarian” (Tavernise and Worth 2006). A New York Times article printed three days earlier focused on an even more revealing issue concerning the state of intergroup relations in Iraq: intergroup marriage. While mixed marriages were always rare, they represented 3-5% of all unions in 2002. By late 2005 such marriages had virtually disappeared (Tavernise 2006). This section presents one explanation for the question of why a period of low Sunni representation in Iraqi government would dramatically increase sectarianism, and why a more proportional Iraqi parliament may not necessarily remedy the problem.

Specifically, I will apply the model to a case where there are three groups: Shiite, Sunni, and Kurd, that compose 60%, 20%, and 20% of the population, respectively. The policy dimension I consider consists of the degree of state secularism, with higher policies corresponding to greater preference for a national government run under Islamic law. While considering a single policy dimension is a simplification of a complicated situation in Iraq, this dimension captures clear differences in preferences across the three groups. Indeed, the relationship between religion and state has been a point of contention between the groups since the task of rebuilding Iraqi government began in 2003 (Cullinan 2003). In 2004, United Press International reported that “Iraq elections scheduled for January will be about religion vs. secularism...” (Potter 2004). And in an online story posted in 2005 about the Iraqi parliament’s failure to meet a deadline for drafting a new constitution, Aljazeera reported that “[t]he main sticking points ... were the role of Islam, federalism, and the distribution of national oil wealth.” (Aljazeera English 2005).
I will assume that the ideal points of members of each of the three groups are normally distributed over the policy space with variance equal to 1; the mean of the Kurds is \( p_K = -1 \), the mean of the Sunnis is \( p_{Su} = 0 \), and the mean of the Shiites is \( p_{Sh} = 1 \). Thus, the Kurds are most in favor of a secular government, followed by the Sunnis. The Shiites are the least in favor of a secular government. The ordering of the means of the three groups, rather than the actual numbers assigned to these means, will drive the intuition behind this example. This ordering is consistent with a Zogby International poll released in February 2005 asking “Should Iraq have an Islamic government, or should the government let everyone practice their own religion?” (Zogby International 2005).²⁴

The groups are assumed to be similarly wealthy: \( c_K = c_{Su} = c_{Sh} = 4 \). This is motivated by a recent report by the United Nations Development Programme finding income inequality in Iraq to be low compared to other nations in the region, with the Gini coefficient on income inequality being .36 (United Nations Development Programme 2005, p. 37). Moreover, this report also found perceived income inequality to be low. ²⁵ Last, \( \gamma \), the weight assigned to the “identity” component of individual utility functions, is assumed to be equal to 0.5.

The following table depicts equilibria of this model under three different scenarios: (1) When the Sunnis are monopolists over policy, with \( \rho_{Su} = 1 \) and \( \rho_K = \rho_{Sh} = 0 \), capturing the situation in Iraq before the American invasion; (2) When the Sunnis have no input in policy and seats are distributed proportionally between the Shiites and Kurds, with \( \rho_{Su} = 0, \rho_{Sh} = .75 \), and \( \rho_K = .25 \), capturing the situation after the January 2005 legislative election that was boycotted by the Sunnis;²⁶ And (3) when the seats are distributed proportionally across the three groups so that \( \rho_{Su} = \rho_K = \rho_{Sh} = }
.2 and $\rho_{Sh} = .6$, capturing the situation following the second legislative election in December 2005. A complete characterization of all equilibria as a function of seat share given to the Sunni is described in Figure 3 that follows. Note that in Case (3) two equilibria are possible.

Table 1: Ethnic identification in Iraq as a function of government type

<table>
<thead>
<tr>
<th>Government type</th>
<th>Distribution of seats</th>
<th>Equilibrium policy outcome</th>
<th>Equilibrium identities</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) Sunni control</td>
<td>Sunni = 100% Kurd = 0% Shītē = 0%</td>
<td>Strongly secular state ($x = 0.13$)</td>
<td>Sunni nationalistic Kurd nationalistic Shītē nationalistic</td>
</tr>
<tr>
<td>(2) Kurd / Shītē control</td>
<td>Sunni = 0% Kurd = 25% Shītē = 75%</td>
<td>Strongly Islamic state ($x = 2.07$)</td>
<td>Sunni ethnic Kurd nationalistic Shītē ethnic</td>
</tr>
<tr>
<td>(3) Proportional representation</td>
<td>Sunni = 20% Kurd = 20% Shītē = 60%</td>
<td>Islamic state ($x = 1.6$)</td>
<td>Sunni ethnic Kurd nationalistic Shītē ethnic</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Secular state ($x = 0.49$)</td>
<td>Sunni nationalistic Kurd nationalistic Shītē nationalistic</td>
</tr>
</tbody>
</table>

The following figure depicts all social identity equilibria as a function of the seat share allotted to the Sunnis. It assumes that at a fixed Sunni seat share the remainder of the legislative seats are allocated proportionally between the Kurds and Shītēs (i.e. according to a 1-to-3 ratio). The three equilibrium cases described in the table above are labeled on the graph.
The graph is read as follows. Sunni seat share is labeled on the $y$-axis and the policy space is labeled on the $x$-axis. Holding Sunni seat share fixed (say at 40%) we know that the Shiites receive 45% of the seats and that the Kurds receive 15% of the seats. To find the equilibria that this government produces, draw a horizontal line that intersects the $y$-axis at 40. This line will intersect two curves: the solid curve at $x = 0.36$ and the small-dash curve at $x = 0.59$. The solid curve corresponds to equilibria in which all individuals identify with the nation. The small-dash curve corresponds to equilibria in which only the Shiite identify ethnically. Thus, there are two equilibria for this particular government type: one in which all individuals identify with the nation and policy is $x = 0.36$, and another in which the Shiite identify ethnically (the Kurds and Sunni identify nationally) and policy is $x = 0.59$.

**Figure 3 here**

While highly stylized, this example provides one explanation for the increase in sectarian identification among Shiites and Sunnis following the legislative elections in January 2005. In this example, when the Sunni have monopolistic control over government then there is a unique equilibrium in which policy is strongly secular and all of the three groups identify along nationalistic, as opposed to ethnic, lines. This is because, of the three groups, the Sunni have the most moderate policy preferences with respect to the relationship between Islam and the state. However, when the seats are proportionally distributed between the Kurds and Shiites and the Sunni are excluded from government, a new (unique) equilibrium emerges. In this case the Shiites and Sunnis both switch their identities, identifying along ethnic, rather than nationalistic, lines. While this change
in identification moves the median Sunni slightly to the left (from 0.13 to 0), it moves the median Shiite far to the right (from 0.8 to 2.5). This change in Shiite identity is accompanied by policy that is far more extreme, as Shiites have 75% of the seat share. In this example, disenfranchising the Sunni has a dramatic effect on sectarian identification, causing Shiites and Sunnis to suddenly identify along ethnic lines and bringing about a large divergence in their policy preferences.

Lastly, when seats are distributed proportionally across the three groups then two equilibria are possible. The first is an equilibrium in which the Shiites and Sunnis identify along ethnic lines and the Kurds identify nationally. The second is an equilibrium in which all three groups identify along nationalistic lines. Thus, there is no guarantee that a more proportional government will spark the formation of an Iraqi national identity within all groups. However, both of these equilibria yield policy outcomes that are more moderate than the outcome yielded when the Sunni were granted no legislative seats. Furthermore, an “all nationalistic” equilibrium is, at the minimum, achievable under a government in which each of the groups is represented fairly.

**Equilibrium selection**

Last, I will briefly discuss the problem of equilibrium selection in this model. As just discussed, a proportional distribution of legislative seats is capable of inducing two possible equilibria in this model: one in which members of all three groups identify as “Iraqi” and one in which the Shiites and Sunnis identify along ethnic lines. Thus, the question of equilibrium selection is important because even simple specifications of the model can generate multiple equilibria. The multiplicity of equilibria may be one explanation for a number of inconsistent findings in studies on the effect
of ethnic context on group conflict and prejudice. V. O. Key’s “threat hypothesis” predicts that large concentrations of ethnic minorities inspire hostility and prejudice among members of a dominant group by threatening competition for scarce resources (Key 1949). Alternatively, Allport’s “contact hypotheses” predicts the opposite: that increased contact between groups reduces inter-group tension and conflict by breaking down ingrained stereotypes (Allport 1954). Cain, Citrin and Wong (2000) argue that the mixed support for both hypotheses may reflect the fact that racial attitudes appear to be more a product of the social and political backgrounds of individuals rather than the ethnic composition of their communities. This paper makes a different observation: the mixed support for both hypotheses may occur because the identity choices of individuals depend on an interaction between social context and political outcomes (modeled as the current policy induced by an institution). Looking at equilibria solely as a function of context will often not yield a unique prediction in this model.

**Conclusions**

Political institutions may be invoked for many different reasons. While all institutions serve to govern human interaction in some fundamental way, the goals of different institutions may be as disparate as limiting the ability of a ruler to plunder an economy, containing civil unrest, and promoting bureaucratic efficiency. This paper considers the role that political institutions can play in inducing or subduing ethnic identities, focusing on the question of whether institutions are capable of creating a national identity, or sense of state attachment. I provide an analytic framework for
modeling identity choice as a function of both political institutions and the composition of society, and obtain results concerning the optimal representation of groups within society needed in order to induce individuals to identify with the state. The results emphasize that well-designed institutions may favor heterogeneous groups over homogeneous groups and poor groups over wealthy ones.

Many interesting avenues for future research remain. A straightforward extension of the model could incorporate strategic players as a means of refining the set of equilibria. Examples of such players could include one or more political entrepreneurs seeking to incite or quell ethnic conflict (as in Posner (2004)), or a government seeking to reduce racial or ethnic disparity through the use of affirmative action or monetary transfers. Alternatively, the model could be extended to consider richer institutional mechanisms such as federal systems and republics. More fundamental, however, is the question of how institutions can arise and endure when identities are malleable. While this paper takes institutions as fixed and then compares the performance of various institutional forms, a more general approach would not only examine the effect of institutions on identity, but also identity on institutions.

Real-world institutions are created endogenously, and may reflect many aspects of the society being governed. One cannot simply write a constitution and have it work. In comparing the effect of different institutional forms on identity, this paper is purely a normative exercise. However, it brings us one step closer to the important goal of understanding the interplay between identity and institutions both normatively and positively, by considering a baseline situation in which individuals only care about outcomes and not about institutions per se. In other words, the results in this
paper are established without appealing directly to assumptions about individual preferences over institutional forms (such as symbolic representation, for example). While this may be an empirical weakness of the paper it is an important theoretical starting point, because a different assumption would result in problems of endogeneity and observational equivalence: for example, does identity drive a desire for symbolic representation, or does symbolic representation strengthen the identities of those groups being represented? Does identity emerge because of symbolic representation \textit{per se}, or is symbolic representation correlated with policy outcomes that induce ethnic identification?

A last and related question that remains for future research is one of institutional feasibility. An important underlying assumption of this paper is that institutions are legitimate and work. However, if our goal is to examine the effect of identity on the endogenous implementation of institutions, then we need to consider why individuals choose to follow institutional rules. Do people respect the rules of an institution when the rules are perceived of as procedurally legitimate, or when people are materially advantaged by the institution? While clearly beyond the scope of this paper, these are important questions that must be addressed if we seek to gain a fuller understanding of the link between institutions and the societies they govern.
Appendix

The proof of Theorem 1 proves existence for a more general form of the model than is presented in the body of this paper. In particular, I will prove that an equilibrium will exist whenever the following six conditions hold:

1. Policy space $X \subset \mathbb{R}^M$ is compact and convex.

2. There are a finite number of types of players (where “type” denotes the collection of all groups an individual belongs to), and the distribution of ideal points for individuals of a particular type is continuous over $\mathbb{R}^M$.

3. Utility functions are continuous functions of a material payoff function and a group status function.

4. Material payoff functions are continuous and of the same functional form for all players, $\pi(p, x)$, where $p$ is the player’s ideal point and $x$ is the policy outcome.

5. Identification with group $g$ grants an individual a group-specific payoff, $R(g, x)$, where $g$ is the group and $x$ is the policy outcome.

6. The political institution is continuous in the strategies of individuals (with respect to the topology of weak convergence).

**Theorem 1** There exists a social identity equilibrium, possibly in mixed strategies.
Proof: I will first prove existence for a different game of incomplete information with a finite number of players. I will then show that equilibria of this game can be reinterpreted as equilibria of my model.

Let the new set of players be denoted $T \cup q$, where $T = \{1, ..., |T|\}$, with generic player $t \in T$. Thus, all individuals of a particular type are now represented by a single player $t$. Each player $t \in T$ observes his ideal point, $p_t$ drawn from distribution $f_t$ over $\mathbb{R}^M$. After observing his own ideal point, each player chooses an action in $A_t$, where $A_t$ denotes the collection of actions available to individuals of type $t$. $A_t$ represents the collection of groups that an individual of type $t$ may identify with.

As defined in Milgrom and Weber (1985), a distributional strategy for a Player $t$ is a joint density $\mu_t$ over $\mathbb{R}^M \times A_t$ for which the marginal density of $\mathbb{R}^M$ is $f_t$. A collection of distributional strategies for each player in $T$ is denoted $\mu = \{\mu_1, ..., \mu_{|T|}\}$. Let $S_t$ be the set of Player $t$’s distributional strategies. Let $S$ be the space of all distributional strategy profiles for Players 1 through $|T|$.

The institution is represented functionally by a single non-strategic player, $q$. Player $q$ chooses a policy according to a fixed function, $\xi: S \rightarrow X$, where $\xi$ is assumed to be continuous in $\mu$. In words, Player $q$ chooses a policy in $X$ depending on the strategy profile of Players 1 through $|T|$. An action profile is denoted $a = (a_1, ..., a_{|T|}, a_q)$.

Each player $t$’s payoff depends upon his own ideal point realization and the action profile in the following way: $U_t: \mathbb{R}^M \times A \times X \rightarrow \mathbb{R}$ such that $U_t(p_t, a) = w(p_t, a_q, a_t)$. Player $q$ receives no payoff.
When the players adopt distributional strategies \((\mu_1, \ldots, \mu_{|T|}, \xi)\) then the expected payoff to Player \(t\) is:

\[
EU_t(p_t, a) = \int_{M \times A} w(p_t, a_q, a_t) d\mu_1 \ldots d\mu_{|T|},
\]

where \(a_q = \xi(\mu)\). An equilibrium is a fixed point in a correspondence \(C\) from \(S \times X\) into itself, with:

\[
C(\mu, a_q) = (\text{argmax}_{\mu'_1 \in S_1} \int_{M \times A} w(p_1, a_q, a_1) d\mu'_1, \ldots, \text{argmax}_{\mu'_{|T|} \in S_{|T|}} \int_{M \times A} w(p_{|T|}, a_q, a_{|T|}) d\mu'_{|T|}, \xi(\mu)).
\]

Because the action spaces of players \(t\) are finite (and thus compact), each player’s set of distributional strategies \(S_t\) is a tight set of probability measures. By Prohorov’s Theorem, the sets of distributional strategies are compact with respect to the topology of weak convergence. They are also convex, trivially. Similarly, recall that policy space \(X\) is compact and convex.

Also note that \(EU_t(p_t, a) = \int_{M \times A} w(p_t, a_q, a_t) d\mu_t\) is linear (and thus quasiconcave) in \(\mu_t\) which implies that the players’ best response correspondences are convex-valued. Continuity of the players’ utility functions implies that their best response correspondences are upper semi-continuous. This, along with compactness of the strategy space, implies that the best response correspondences are compact-valued. Function \(\xi\) is continuous (and hence upper semi-continuous) in \(\mu\) by assumption. By Kakutani’s fixed point theorem, an equilibrium exists.

Last, we must show that the equilibrium distributional strategies found in the modified game correspond to equilibrium strategies of the original game. Let the function \(w(p_t, a_q, a_t)\) equal \(u(\pi(p_t, a_q), R(a_t, a_q))\) and let \(\mu^*\) be a collection of equilibrium distributional strategies. For each type \(t \in T\), and for all \(i \in t\) let \(s^*_i = \mu^*_i(\cdot|p_i)\), or \(\mu^*_i\) conditional on ideal point realization \(p_i\).
Suppose that for a collection of individuals of measure greater than zero $s^*_i$ is not a social identity equilibrium. Since there are a finite number of types this implies that $s^*_i$ is not a best response to $s^*_t$ for a collection of individuals of type $t$ with measure greater than zero. However, this contradicts the fact that $\mu^*_t$ was a best response for Player $t$ in the modified game. Thus, $s^*_i$ is out-of-equilibrium behavior for a collection of players that is at most of measure zero.

Finally, note that because expected utility (Equation 2) and institution $\xi$ are invariant to changes in $\mu_t$ on any set of measure zero, and because a best response always exists at any policy for any ideal point realization, existence of an equilibrium for a set of individuals of full measure implies existence of an equilibrium for all individuals. Thus, there exists a social identity equilibrium. □

**Equilibrium condition when individuals care about the absolute status, and not relative status, of their subgroup:** Suppose that we assume that ethnic identification implies that individuals care about the level status of their group, and not the relative status (i.e., that $v_i(x, g^i) = \pi_i(x) + \gamma \mu g^i(x)$). Then the equilibrium condition for any group with $\overline{p} g^i \geq \overline{p}_N$, or mean above the national mean, is

$$a_i^* = \begin{cases} N & \text{if } x^* \geq \frac{c_g^i - \overline{p} + \sigma_p^2 + \overline{p} \sigma^2_g - \overline{p}^2 g^i}{2(\overline{p}_N - \overline{p} g^i)} \\ g^i & \text{otherwise.} \end{cases}$$

Similarly, the equilibrium condition for groups with $\overline{p} g^i \leq \overline{p}_N$ is the same, but with the $\geq$ sign reversed. It is clear from these conditions that it is impossible to induce a policy outcome at which all individuals choose to identify with the state, except in the case where all groups have the same distribution of members’ ideal points.
Formalization of Observation 1: To see that it will not always be possible to construct an “all nationalistic” equilibrium, consider the case where there are two equally-sized groups, \( g \) and \( h \), that differ only in wealth. Let \( \overline{p}_g = \overline{p}_h = 0 \), and let \( \sigma^2_g = \sigma^2_h = 1 \). As an extreme example, let \( c_g = 100 \) and \( c_h = 0 \). Then members of \( g \) will identify nationalistically on an interval of size \( 2 \times \sqrt{-51} \), which is clearly not a real number. In this example, members of \( g \) will never identify with the nation.

There is, however, always a policy at which every individual will identify ethnically. Let
\[
x_{\text{eth}} = \arg\max_g \sum_{h \neq g} (\overline{p}_h - \overline{p}_g) + \overline{p}_N + \sqrt{\left[ \sum_{h \neq g} (\overline{p}_g - \overline{p}_h) - \overline{p}_N \right]^2 - \left[ \overline{p}_N - \overline{c} + \sigma^2_N + \sum_{h \neq g} ((c_g - c_h) - (\sigma^2_g + \overline{p}_g^2) + (\sigma^2_h + \overline{p}_h^2)) \right]}.
\]

Then, by Equation 1, at any \( x > x_{\text{eth}} \) all individuals will identify ethnically. Note, however, that it may be impossible to induce such extreme policies under a democratic institution such as the weighted median voter rule. □

Formalization of Observation 2: Let
\[
\sigma^2_N = \sum_g [\alpha_g (\sigma_g^2 + (\overline{p}_g)^2)] + (\sum_g \alpha_g \overline{p}_g)^2.
\]

Plugging this into the equations below, this observation follows immediately from the fact that
\[
\frac{\partial}{\partial \sigma^2_g} \sqrt{\left[ \sum_{g \neq g^i} (\overline{p}_{g^i} - \overline{p}_g) - \overline{p}_N \right]^2 - \left[ \overline{p}_N - \overline{c} + \sigma^2_N + \sum_{g \neq g^i} ((c_{g^i} - c_g) - (\sigma^2_{g^i} + \overline{p}_{g^i}^2) + (\sigma^2_g + \overline{p}_g^2)) \right]} \geq 0
\]
and the fact that for any \( g \neq g^i \),
\[
\frac{\partial}{\partial \sigma^2_g} \sqrt{\left[ (\overline{p}_{g^i} - \overline{p}_g) - \overline{p}_N \right]^2 - \left[ \overline{p}_N - \overline{c} + \sigma^2_N + \left( (c_{g^i} - c_g) - (\sigma^2_{g^i} + \overline{p}_{g^i}^2) + (\sigma^2_g + \overline{p}_g^2) \right) \right]} \leq 0.
\]
Thus, by Equation 1, individuals identify with the nation on a larger policy interval as their ethnic group’s variance increases, and as the variance of rival groups decreases. □

**Formalization of Observation 3:** Specifically, I will show that a sufficient condition for an increase in $\sigma$ to increase the range of policies at which all individuals identify nationally is that $\frac{\alpha_h+1}{\beta_h} \geq 1$ for all groups $h$. Suppose that $g$ is the wealthiest ethnic group. Let $\beta_h$ be a constant such that $c_g = \beta_h c_h$ (defined for each ethnic group $h$). By definition, $\bar{c} = \alpha_g c_g + \sum_{h \neq g} \alpha_h c_h$. Defining $c_g$ as a function of $c_h$, we get $\bar{c} = \alpha_g + \sum_{h \neq g} \alpha_h \frac{c_g}{\beta_h}$. Thus, $c_g = \frac{\bar{c}}{\sum_{h \neq g} \frac{\alpha_h}{\beta_h}}$ and $c_h = \frac{c_g}{\beta_h}$.

Recall that the $K$ term in Equation 1 characterizes the size of the interval on which members of group $g$ will identify with the nation. Using the work above, we can define both $c_g$ and $c_h$ in terms of $\bar{c}$ in this $K$ term. For group $g$, $\frac{\partial K}{\partial c}$ is positive whenever $\sum_h \frac{\alpha_h}{\beta_h} + \sum_h \frac{1}{\beta_h} - k > 0$, where $k$ is the total number of ethnic groups. Reducing, we get that a sufficient condition for $K$ to be increasing in $\bar{c}$ for all groups is that $\frac{\alpha_h+1}{\beta_h} \geq 1$ for all groups $h$. □

**Formalization of Corollary 1:** For any particular group $g$, the size of the interval $2K$ defined in Equation 1 approaches $\infty$ as $\bar{c} \to \infty$ when all groups are equally wealthy. Formally,

$$\lim_{\bar{c} \to \infty} \sqrt{\left[ \sum_{g \neq g} (p_{gi} - p_g) - p_N \right]^2 - \left[ p_N^2 - \bar{c} + \sigma^2_N + \sum_{g \neq g} \left( - (\sigma^2_{gi} + p_{gi}^2) + (\sigma^2_g + p_g^2) \right) \right]} = \infty.$$ 

Thus, the size of the interval on which any group identifies with the nation is approaching infinity as the wealth of the nation approaches infinity. It follows that by equalizing the wealth of the groups and increasing the wealth of the nation it will be possible to induce an equilibrium in which
all groups identify with the state. □

**Formalization of Observation 4:** Assume that there are two groups $g$ and $h$, with $\overline{p}_N$ normalized to 0 and $\overline{p}_g \geq \overline{p}_h$. From Equation 1 we know that the center of the interval on which $g$ identifies with the nation is $\overline{p}_h - \overline{p}_g$. Thus, increasing the size of the interval of policies on which $g$ identifies with the nation, or decreasing the size of this interval for group $h$, moves the social point toward the center of this interval for group $h$, or toward $\overline{p}_g - \overline{p}_h$. By Observations 2 and 3, the social point will move toward $p_g - p_h$ when $g$ is more heterogeneous than $h$ and when $g$ is poorer than $h$, *ceteris paribus*.

When both groups identify with the nation, then, as the voting weight $\rho_g$ assigned to group $g$ increases, the weighted median $x(a^*)$ moves toward the point $x = \frac{\overline{p}_g}{1+\gamma}$, (the median utility-maximizing policy of a member of $g$). So long as the social point is smaller than $\frac{\overline{p}_g}{1+\gamma}$, this increased voting weight for $g$ will imply a policy move toward $\overline{p}_g - \overline{p}_h$, because $\frac{\overline{p}_g}{1+\gamma} \leq p_g - p_h$. When the social point is equal to $\frac{\overline{p}_g}{1+\gamma}$ then the institution that induces it gives $g$ 100% of the voting weight. When the social point is greater than $\frac{\overline{p}_g}{1+\gamma}$ then it cannot be induced by any weighted median voter rule. □
Notes

1The moderation-inducing properties of the alternative vote have been the topic of a lively debate (Fraenkel and Grofman 2006ab; Horowitz 2006).

2Sweden, South Africa, France and Belgium all utilize gender quotas in public elections.

3Parliamentary seats are reserved for the Maori in New Zealand, and for scheduled tribes and castes in India.

4Batasuna, a Basque party with ties to the terrorist group ETA, has been banned in Spain since 2003.

5Laitin (1985) argues that British colonial rule fostered and solidified ethnic identities; Marx (1998) describes how a legal framework of racism in the U.S. and South Africa consolidated previously rival elite groups in the making of the modern state; Lijphart (1977) argues that the institutional elements of consociational democracy provide the best means of achieving democracy in the face of ethnic conflict; and Brancati (2006) examines the link between political decentralization, regional parties, and ethnic conflict.

6An important type of “situation” that I don’t consider is the strategic behavior of political elites seeking personal gain, as in Posner (2004). While this sort of behavior is beyond the scope of this paper, it represents a potential direction for future extensions of the model.

7Throughout I will use the phrase “national identity” to be synonymous with “identification with the state.” “National identity” as described in this paper differs from the term “nationalism” as it is commonly used in political science. Barrington (1997) provides precise definitions of “nationalism” and “nation,” and argues that “nation” is not synonymous with “state.” A nation is a collection of people united by shared cultural features, while a state is political unit corresponding to a relatively static population and a set of governing institutions. In examining the effect of institutions on identity, this paper deals with states, not nations.

8The results that follow do not depend specifically on a quadratic specification of $\pi$, but do depend on the concavity of this function.

9This theory has been borne out in experiments showing that individuals will sacrifice personal and group gain in order to achieve a positive difference between the economic gain of their group relative to other groups. These
experiments suggest that social comparisons, stemming from a desire for a positive social identity, may be an important cause of ingroup bias that is distinct from more instrumental causes (Turner et al. 1979).

10 The interested reader can refer to the Appendix for a derivation of the equilibrium conditions in the case when ethnic identification implies a common fate conception of bias.

11 The model presented in this paper is essentially one of endogenous preference: when individuals choose identities, they choose utility functions. In this sense, this model is indirectly related to the “optimal expectations” model of Brunnermeier and Parker (2005) in which individuals optimistically bias their beliefs in order to gain higher anticipatory utility. However, while the subjective beliefs of agents in their model are constrained by a true probability distribution over states of the world, in this model agents are constrained by the exogenous collection of identities that they can choose from. The tractability of this model depends on such a constraint, and pushing the limits of this constraint remains a topic for future research.

12 Note that while mixed strategies are allowed in this framework—and are necessary in order to prove the existence of an equilibrium—my later analytic results will focus solely on pure strategy equilibria (i.e. instances in which individuals only identify with a single group), in cases when such equilibria exist. This is done only to make the analysis of the game more transparent.

13 Adding the status of another nation (or nations) to the model as an additional parameter would be a simple extension that could generate interesting comparative statics of its own. It would not change any of the findings of this paper, however.

14 The addition of an identity term to individuals’ utility functions is mathematically equivalent to “valence” models of politics, in which voter preferences contain a personal spatial component and a valence term generally representing the quality of the vote choice. Similar models (in a more general context) are studied by Adams & Merrill (2003), Schofield (2004), and Ansolabehere & Snyder (2000), among many others. Here the valence term corresponds to the status an individual receives from identification with a particular group. This term is endogenous, as the status of a given group varies with the policy outcome. In considering endogenous valence, this model is related to the “activist valence” models studied by Miller and Schofield (2003) and Schofield (2006).
This is because for any identity $s_i$ chosen by Player $i$, $i$’s utility function is a linear combination of concave functions. Thus, $i$’s utility function is concave.

Note that $i$’s utility-maximizing policy is different than his ideal point. Player $i$’s ideal point maximizes his material payoff function, irrespective of $i$’s identity choice. His utility-maximizing policy maximizes his utility conditional upon a choice of identity.

The equilibrium condition for the case where ethnic identification implies that individuals care only about the absolute, and not relative, status of their group can be found in the Appendix.

When showing this it is necessary to recall that $\sigma_N^2 = \sum_g \alpha_g (\sigma_g^2 + (\mu_g)^2) + (\sum_g \alpha_g \mu_g)^2$. This is because the total distribution of ideal points is a mixture of the group distributions.

The assumption that material payoff $\pi$ is concave in $p_i$ may seem strange because it is typically assumed that utility is instead concave in policy $x$. However, if $\pi$ is symmetric in $p_i$ and $x$ (i.e. is invariant to permutations of $p_i$ and $x$) then concavity in $p_i$ implies concavity in $x$. This symmetry will hold when, for example, utility is a function of the distance between $p_i$ and $x$, as distance functions are symmetric.

In particular, when $\mu = 0$ then $c_L = c_R = 0$, when $\mu = 2$ then $c_L = \frac{4}{5}$ and $c_R = \frac{16}{5}$ and when $\mu = 4$ then $c_L = \frac{8}{5}$ and $c_R = \frac{32}{5}$.

This general point is made by Melson and Wolpe (1970) in Proposition 2 of their article.

While until this point this paper has considered “ethnic identification,” it should be noted that Sunnis, Shiites and Kurds are ethno-religious groups rather than simply ethnic groups. Arabs and Kurds are different ethnic groups; Shiites and Sunnis are ethno-religious groups.

The Sunni Arabs and the Kurds each received slightly more than 20% of the 230 total legislative seats. The Shiites received slightly more than 50% of the total seats (Katzman 2006).

This poll found that 49% of the Shiite, 28% of the Sunni, and 5% of the Kurds favored an Islamic state.

The report shows that in 17 of Iraq’s 18 provinces the mode response to a question about the comparative “situation” of individuals within the province was “We are neither rich nor poor.” (United Nations Development Programme 2005, p. 40).
In this election Kurds won slightly fewer than 30% of the legislative seats and Shiites won slightly fewer than 70% of the seats.

Again, note that the “median Sunni policy” is the median utility-maximizing policy for a Sunni. This is different than the median ideal point of a Sunni. See Note 16.

Note that players are indifferent with respect to the action choices of the other players, aside from Player $q$.

A family of probability measures $S$ on a general metric space $X$ is tight if for every $\epsilon > 0$ there exists a compact set $K$ in $X$ such that $P(K) > 1 - \epsilon$ for all $P$ in $S$.

See Billingsley (1968), p. 240.
References


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Figure 1: Ethnic identification as the variance of Group R increases
Figure 2: Increasing $\bar{c}$ when group wealth is equal and unequal
Figure 3: Equilibria as a function of Sunni seat share