

Measurements of $\sin 2\alpha$ from B-Factories



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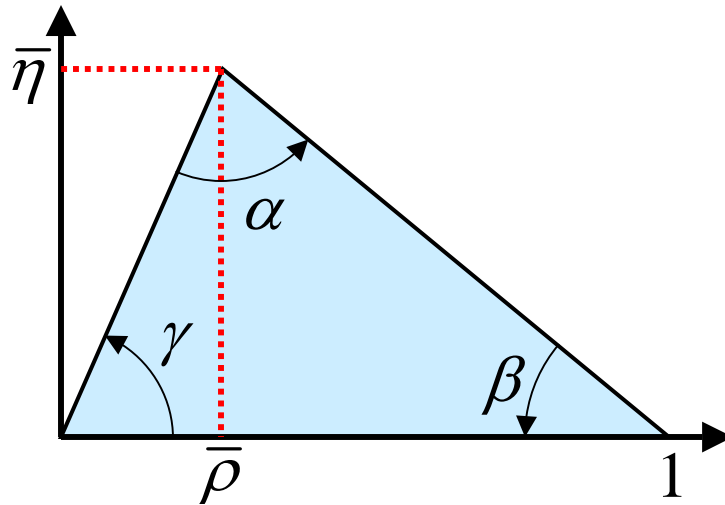
Harvard University

The BABAR Collaboration

BEACH 2002, Vancouver, June 25-29, 2002

Introduction

- CP violation in B^0 decays gives access to the angles of the Unitarity Triangle



$$\alpha = \phi_2 \equiv \arg \left(-\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right)$$

$$\beta = \phi_1 \equiv \arg \left(-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right)$$

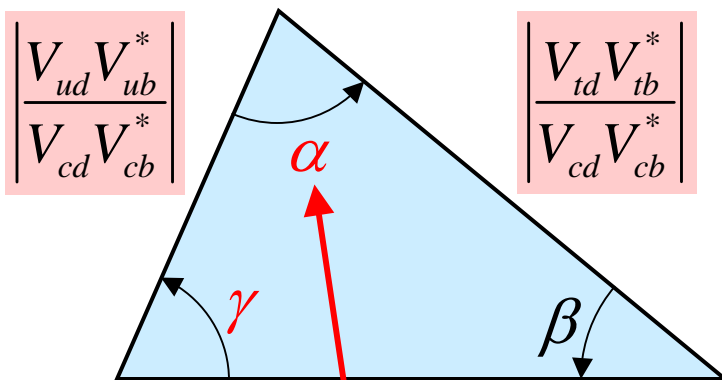
$$\gamma = \phi_3 \equiv \arg \left(-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$

- $\sin 2\beta$ measured to ± 0.08 dominated by $B^0 \rightarrow J/\psi K_S$
- Where does this leave us?

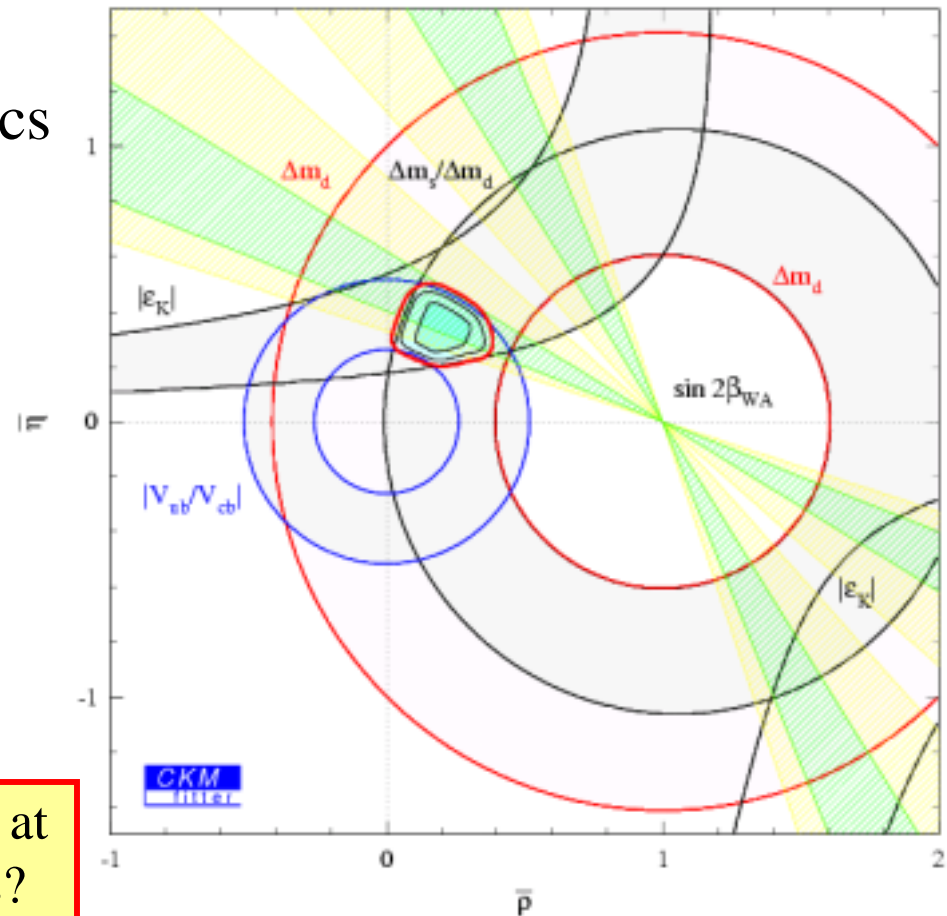
See D. Marlow's talk

Unitarity Triangle and $\sin 2\beta$

- Measured $\sin 2\beta$ agrees with indirect constraints
 - Shrinking $\sigma(\sin 2\beta)$ **alone** may not reveal new physics
- Must measure the sides and the other angles



Next possibility at the B Factories?



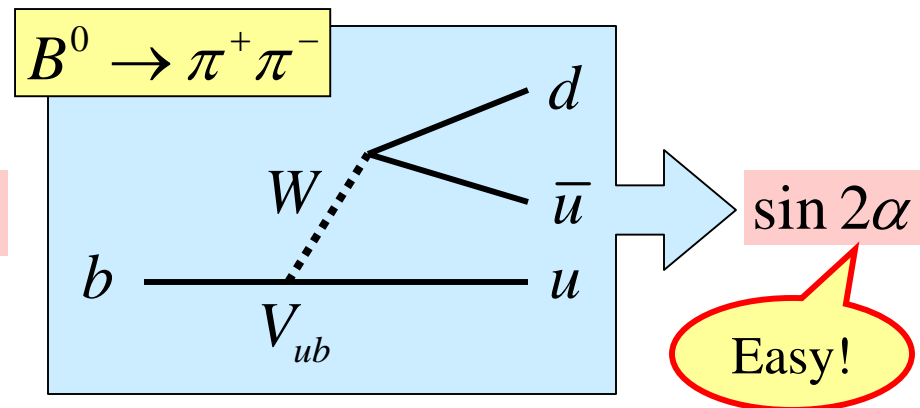
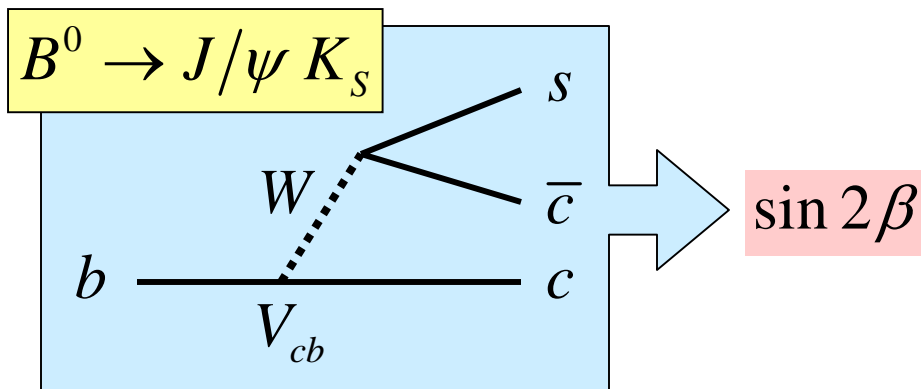
Measuring $\sin 2\alpha$

- Time-dependent CP asymmetry in $B^0 \rightarrow f_{CP}$ is

$$\frac{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) - \Gamma(B_{phys}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) + \Gamma(B_{phys}^0(t) \rightarrow f_{CP})} = S_{f_{CP}} \sin(\Delta m_d t) + C_{f_{CP}} \cos(\Delta m_d t)$$

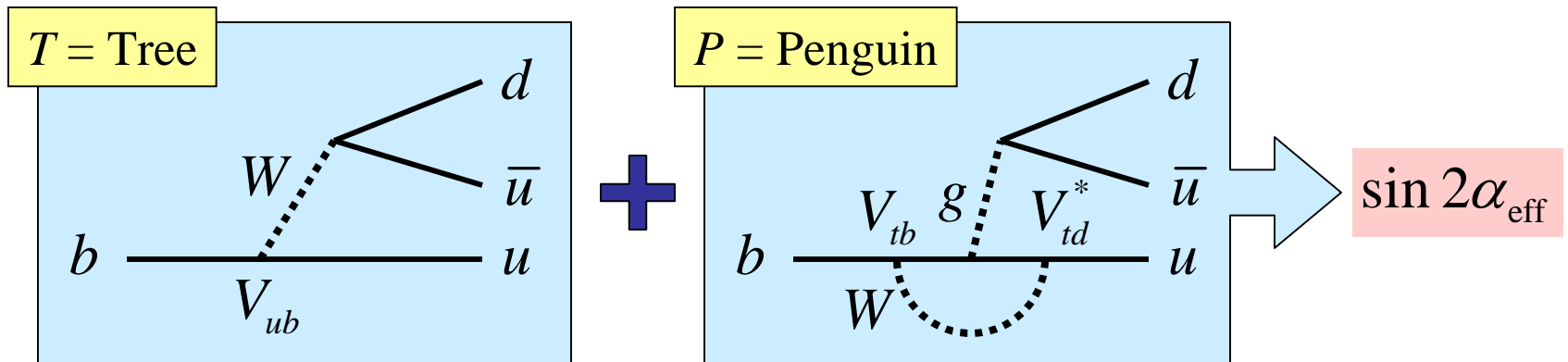
$$S_{f_{CP}} = -\frac{2\text{Im } \lambda}{1 + |\lambda|^2} \quad C_{f_{CP}} = \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \quad \lambda = \frac{q}{p} \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

CKM phase appears here



Penguin Pollution

- Unlike $J/\psi K_S$, $\pi^+\pi^-$ mode suffers from significant pollution from the penguin diagrams with a different weak phase

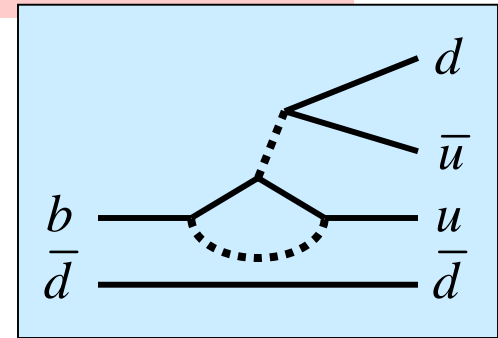
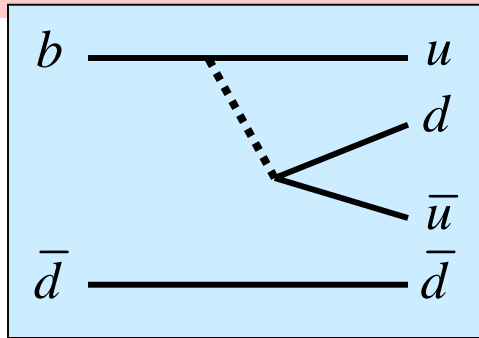
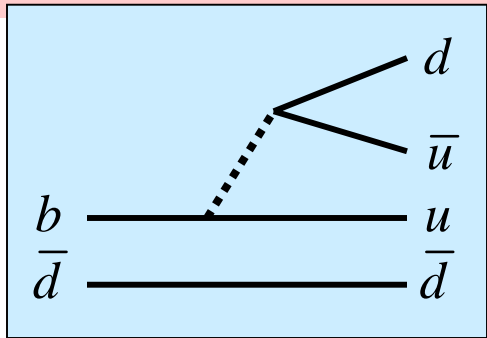


- To estimate $\alpha_{\text{eff}} - \alpha$, we need:
 - P/T ratio – about 1/3 from $BR(B \rightarrow K\pi)/BR(B \rightarrow \pi\pi)$
 - δ = strong phase difference between P and T

Taming Penguins

- Take advantage of the isospin symmetry

$$A = \alpha_T \cdot T + \alpha_C \cdot C + \alpha_P \cdot P$$

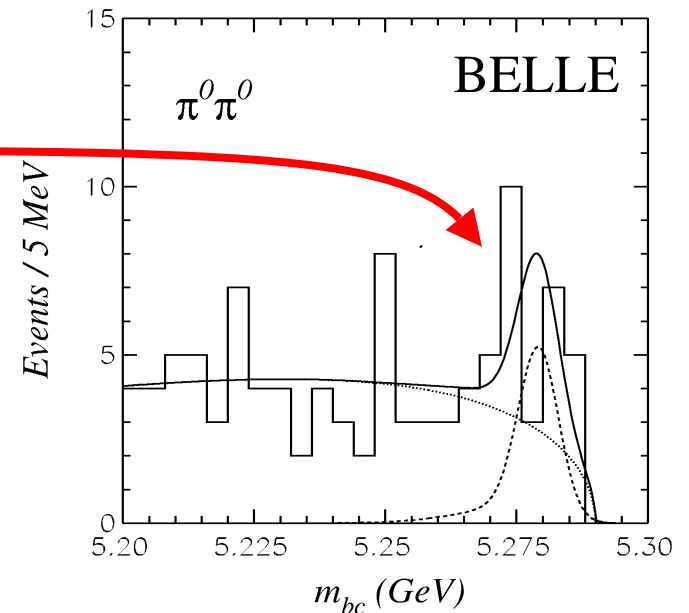


Mode	α_T	α_C	α_P	BABAR $BR \times 10^6$	Belle $BR \times 10^6$
$B^0 \rightarrow \pi^+ \pi^-$	$\sqrt{2}$	0	$\sqrt{2}$	$5.4 \pm 0.7 \pm 0.5$	$5.1 \pm 1.1 \pm 0.4$
$B^+ \rightarrow \pi^+ \pi^0$	1	1	0	$4.1^{+1.1}_{-1.0} \pm 0.8$	$7.0 \pm 2.2 \pm 0.8$
$B^0 \rightarrow \pi^0 \pi^0$	0	1	-1	< 3.3	< 5.6

All preliminary

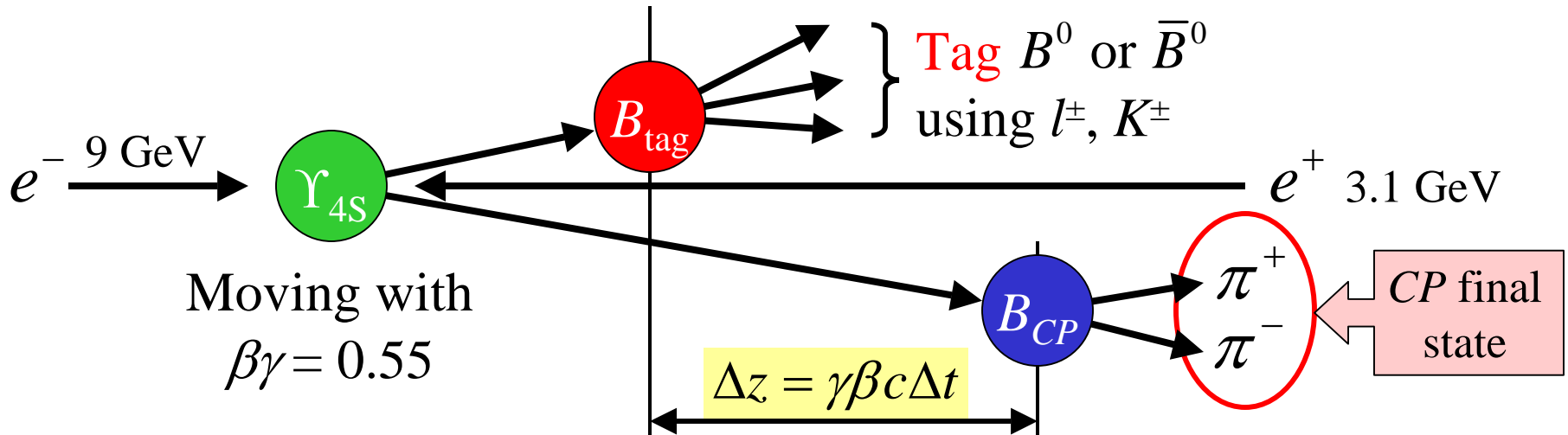
$B^0 \rightarrow \pi^0 \pi^0$ Branching Ratio

- BABAR: Preliminary 54 fb^{-1}
 - $BR(\pi^0 \pi^0) < 3.3 \times 10^{-6}$ (90% CL)
- Belle: Preliminary 31.7 M BB
 - 2.2σ “bump” in the signal
 - Fitted $BR = (2.9 \pm 1.5 \pm 0.6) \times 10^{-6}$
 - $BR(\pi^0 \pi^0) < 5.6 \times 10^{-6}$ (90% CL)
- CLEO: 9.13 fb^{-1}
 - $BR(\pi^0 \pi^0) < 5.7 \times 10^{-6}$ (90% CL)



Expect first observation in the near future

CP Asymmetry in $B^0 \rightarrow \pi^+\pi^-$



- Same method as $\sin 2\beta$ measurements
 - Difference: the direct CP term cannot be neglected

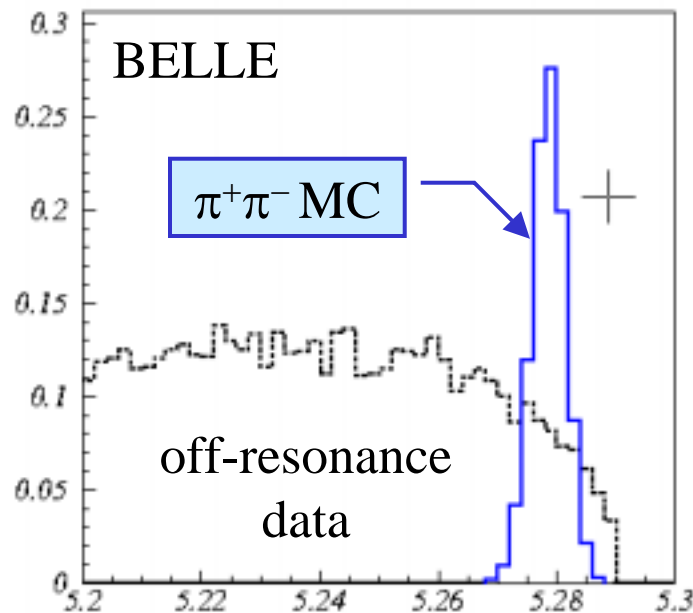
$$\frac{N(B_{tag}^0) - N(\bar{B}_{tag}^0)}{N(B_{tag}^0) + N(\bar{B}_{tag}^0)} = S_{\pi\pi} \sin(\Delta m_d \Delta t) - C_{\pi\pi} \cos(\Delta m_d \Delta t)$$

of events with B^0/\bar{B}^0 tag

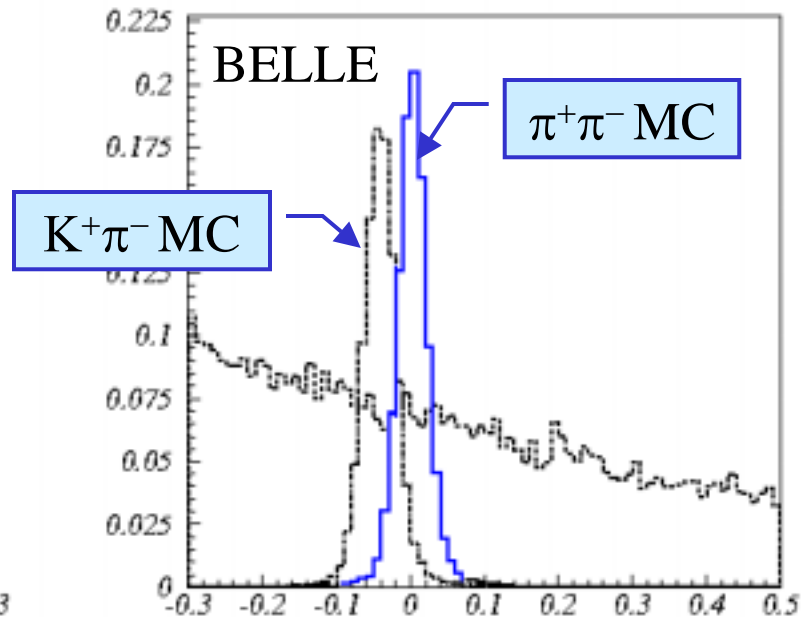
Challenges

- Specific to $B^0 \rightarrow \pi^+ \pi^-$
 - Topology $B^0 \rightarrow h^+ h^-$ simple to reconstruct
 - **Particle ID** must separate π^\pm from K^\pm $BR(\pi^+ \pi^-) < BR(K^+ \pi^-)$
 - DIRC (BABAR) and Aerogel (Belle)
 - Significant **background from continuum**
 - Event-shape variables \rightarrow Fisher discriminant
- Common with other CP measurements
 - Flavor tagging
 - Vertex reconstruction
- And, of course, as much $\int \mathcal{L} dt$ as possible

B⁰ Reconstruction



$$m_{bc} = \sqrt{(E_{CM}/2)^2 - (\mathbf{p}_{\pi^+} + \mathbf{p}_{\pi^-})^2}$$

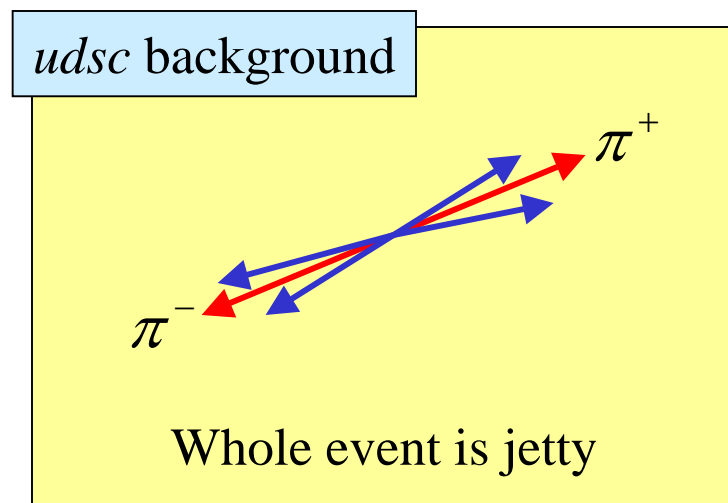
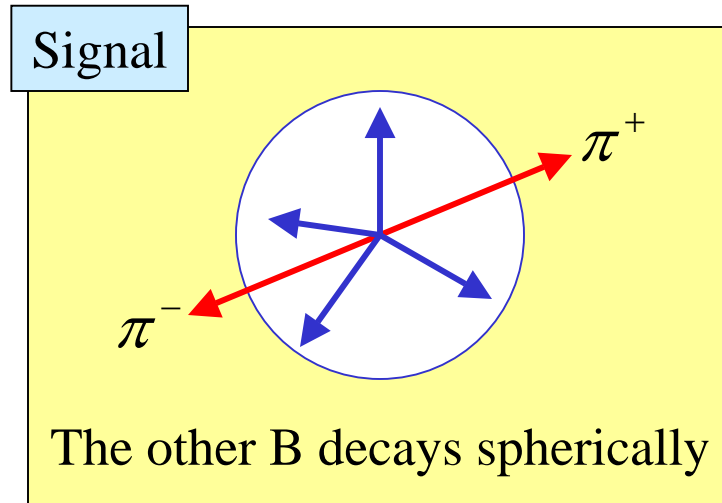


$$\Delta E = E_{\pi^+} + E_{\pi^-} - E_{CM}/2$$

- m_{bc} (or m_{ES}) and ΔE peak cleanly for the two-body signal
 - $K\pi$ and KK peaks shifted in $\Delta E \rightarrow$ Additional discrimination

Continuum Background

- Most of the background come from continuum

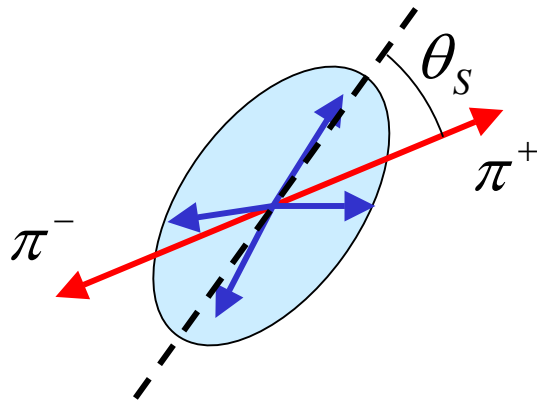


- Use event shape variables that represent “jettiness” to suppress them

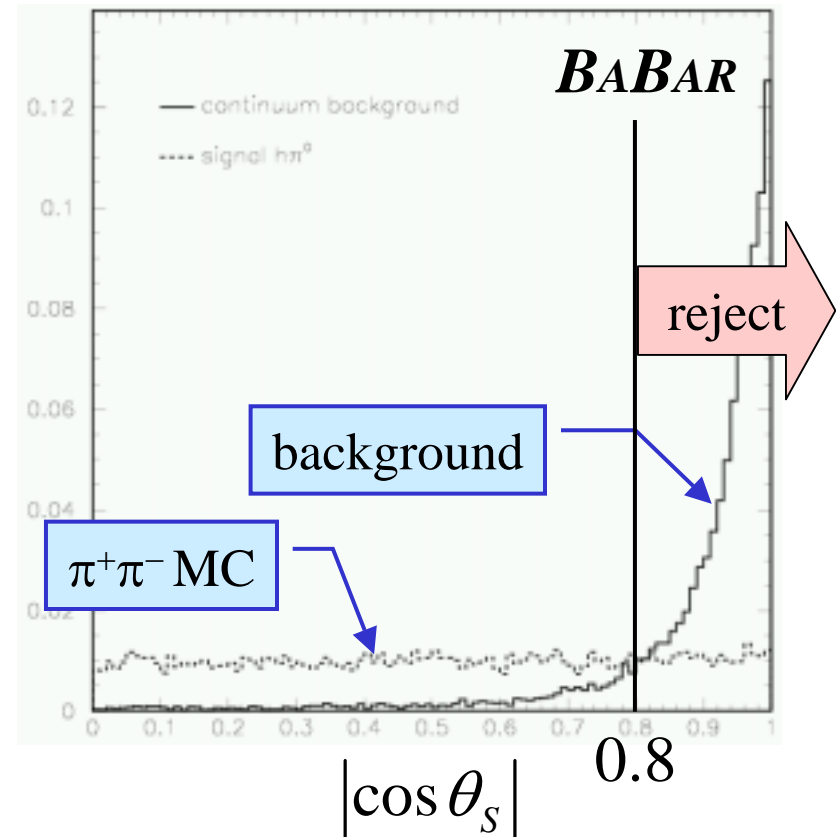
Examples

Sphericity Angle

- Angle θ_s between the sphericity axes of the B candidate and the rest of the event

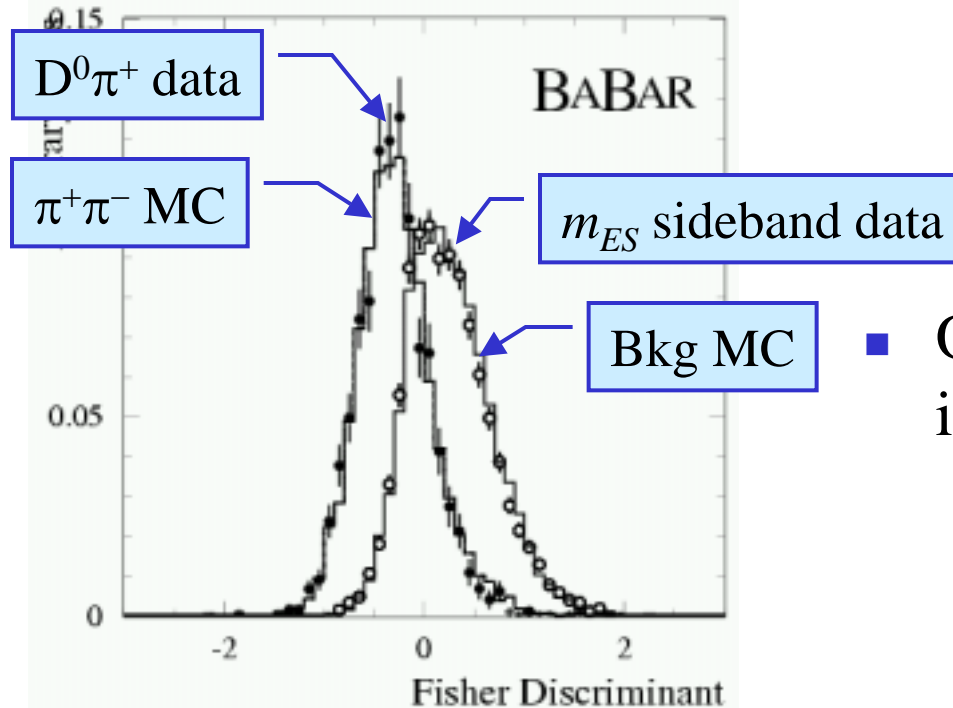
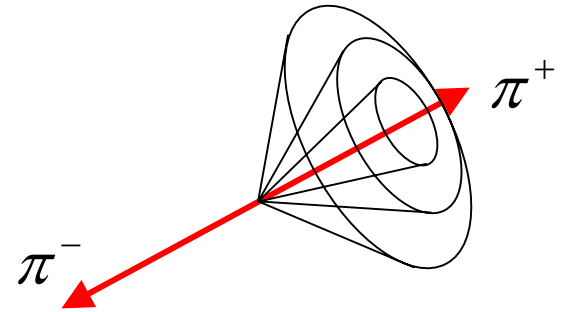


- Cut at 0.8 removes 83% of the continuum background



Fisher Discriminant

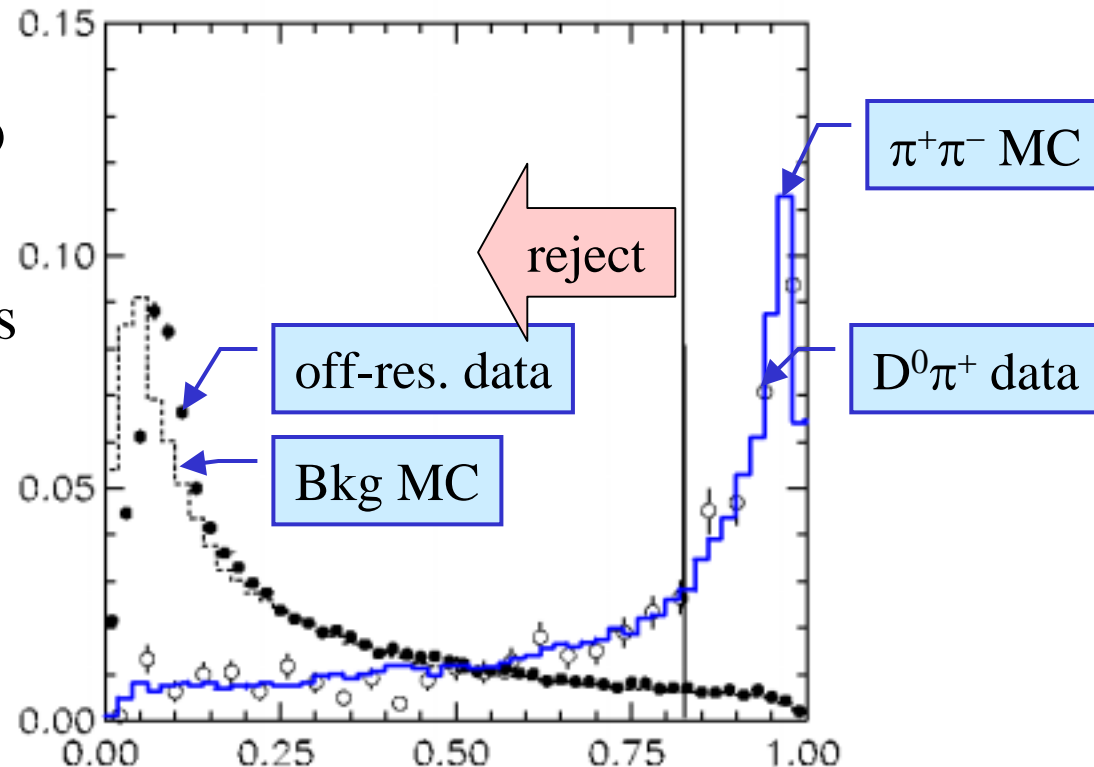
- BABAR uses the “CLEO” Fisher
 - Momentum flow in 9 cones around the candidate axis



- Output of Fisher goes into the likelihood fit

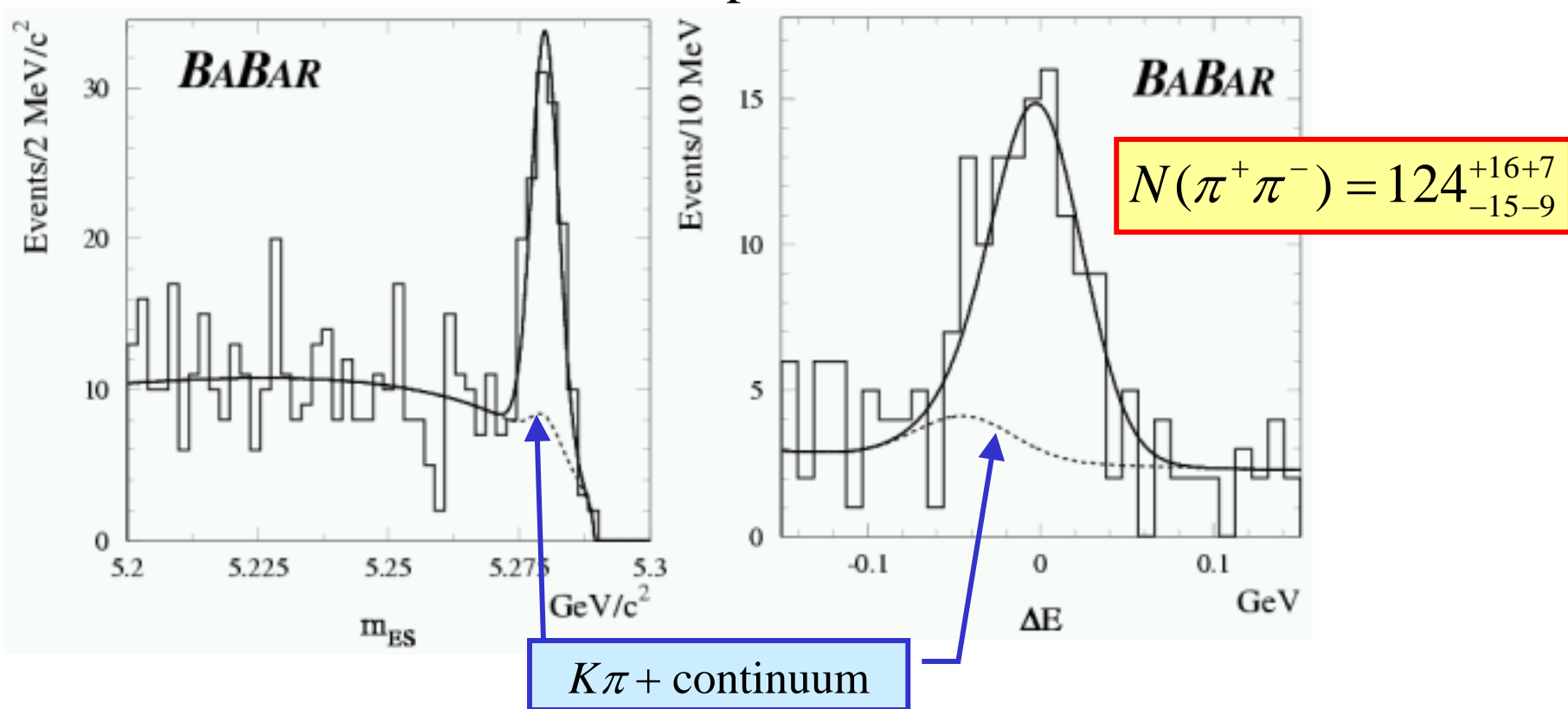
Fisher Discriminant

- Belle's Fisher discriminant uses:
 - Modified Fox-Wolfram moments
 - B flight direction
- Output is turned into a likelihood ratio R
 - Cut at 0.825 removes 95% of continuum background



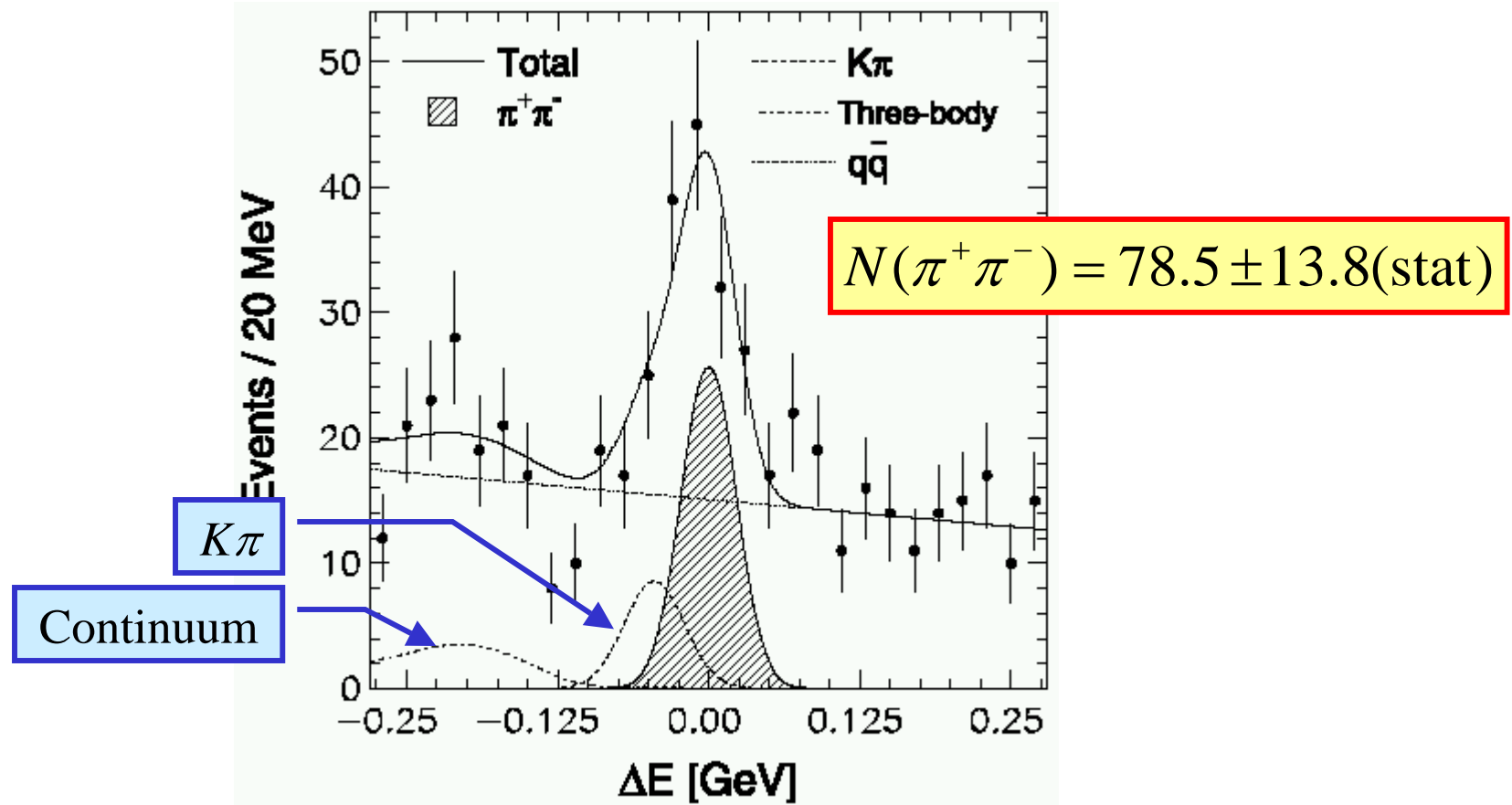
Event Sample – BABAR

- BABAR 55.6 fb⁻¹ preliminary
 - $\pi^+\pi^-$ enhanced for these plots with a cut on Fisher



Event Sample – Belle

- Belle 41.8 fb⁻¹



Maximum Likelihood Fit

- Start from the physics function:

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} \left[1 \pm S_{\pi\pi} \sin(\Delta m_d \Delta t) \mp C_{\pi\pi} \cos(\Delta m_d \Delta t) \right]$$

$$\begin{array}{l} + B^0 \text{ tag} \\ - \bar{B}^0 \text{ tag} \end{array}$$

- Fold in Δt resolution and mis-tag probabilities
- Multiply by PDFs for m_{ES} , ΔE
- BABAR uses particle ID and Fisher in the fit
 - Belle uses these variables in event selection
- Add PDFs for background ($K\pi$, KK , continuum)
- Feed the candidates and turn the crank...

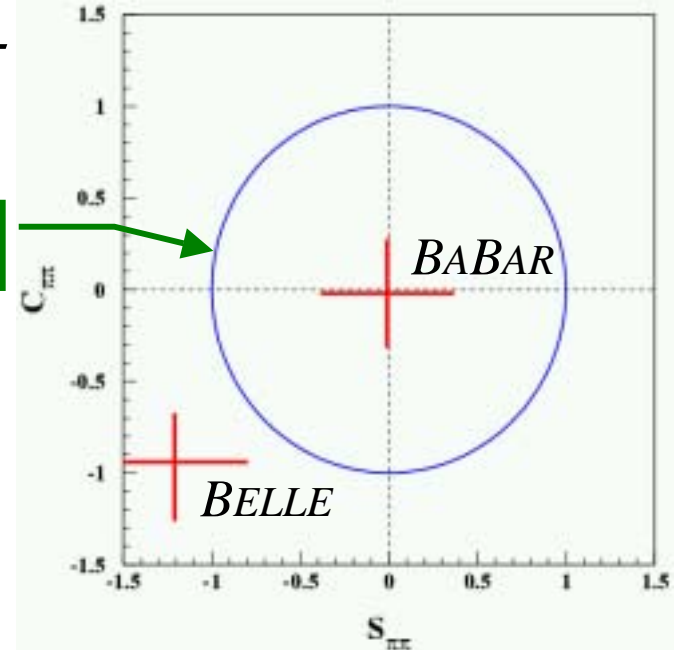
CP Fit Results

	BABAR (preliminary)	Belle (hep-ex/0204002)
$S_{\pi\pi}$	$-0.01 \pm 0.37 \pm 0.07$	$-1.21^{+0.38+0.16}_{-0.27-0.13}$
$C_{\pi\pi}$	$-0.02 \pm 0.29 \pm 0.07$	$-0.94^{+0.31}_{-0.25} \pm 0.09$

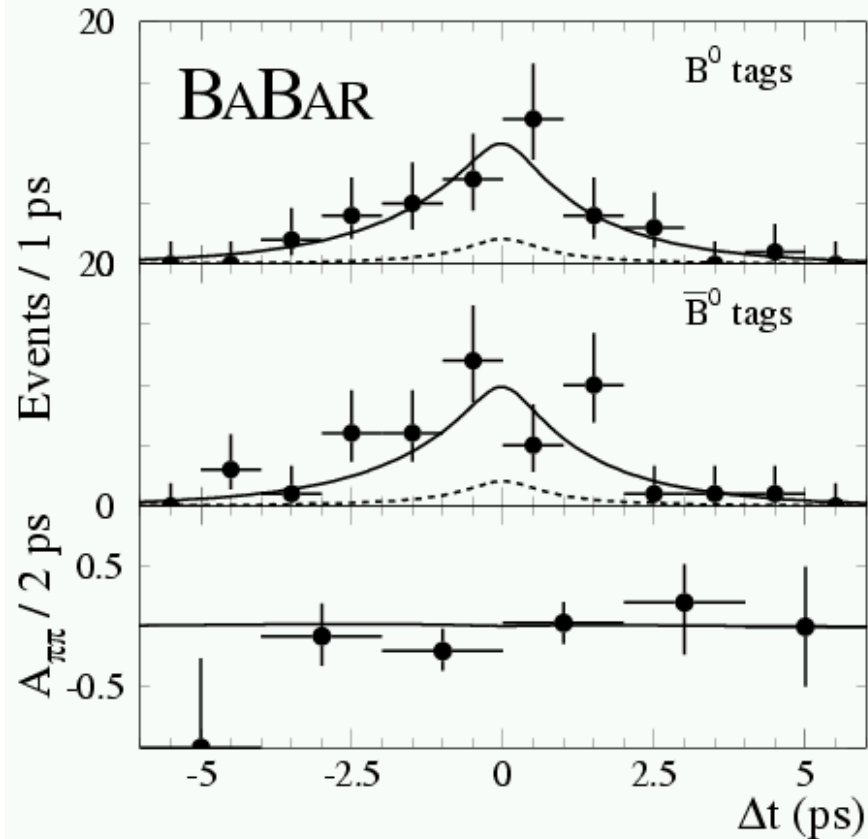
Belle uses
 $A_{\pi\pi} \equiv -C_{\pi\pi}$

- BABAR and Belle disagree by $>2\sigma$
- Belle 1.2σ outside the physical boundary
- Is there any problem?
 - Crosscheck systematics

$$S_{\pi\pi}^2 + C_{\pi\pi}^2 = 1$$

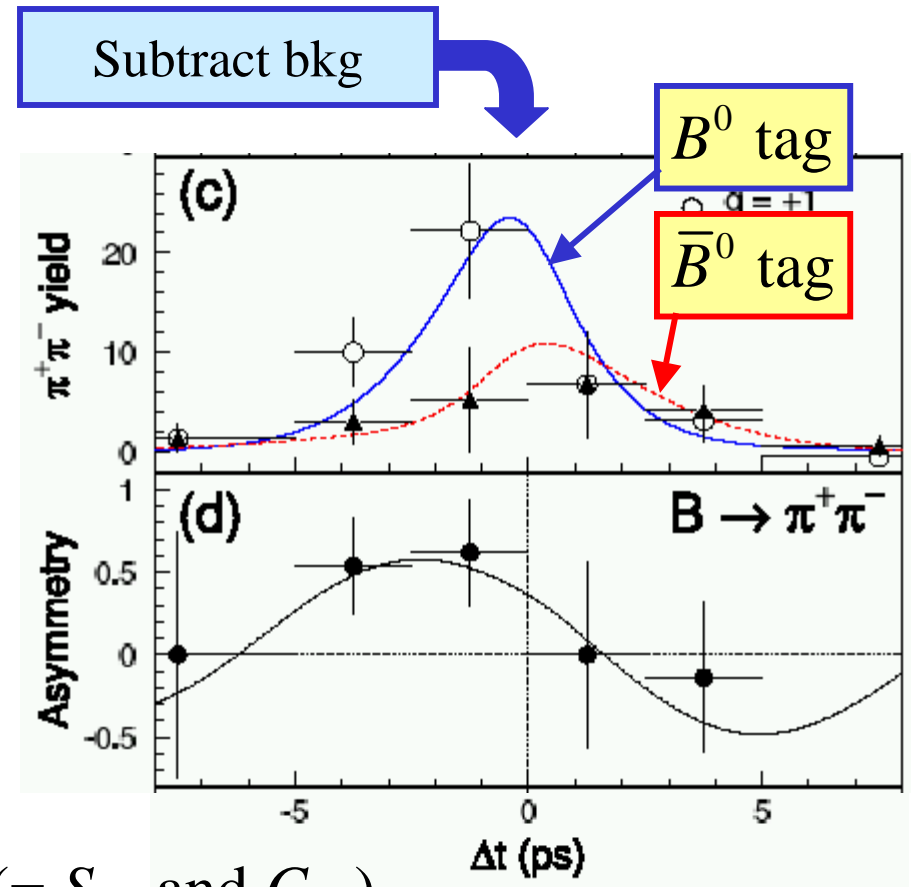
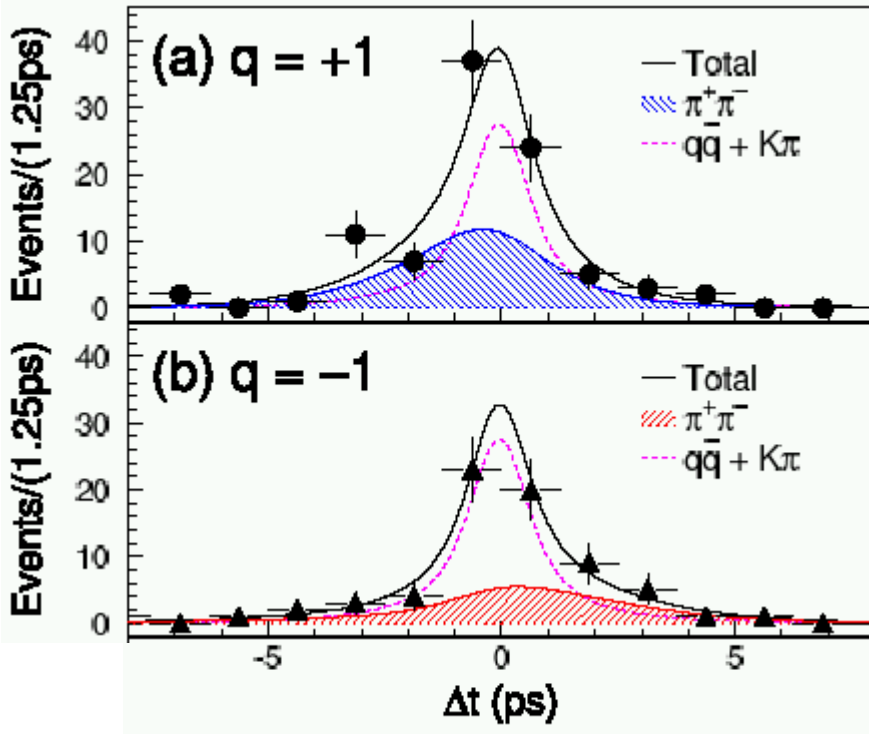


CP Asymmetries – BABAR



- $\pi^+\pi^-$ enhanced for these plots with a cut on Fisher
- No significant asymmetry

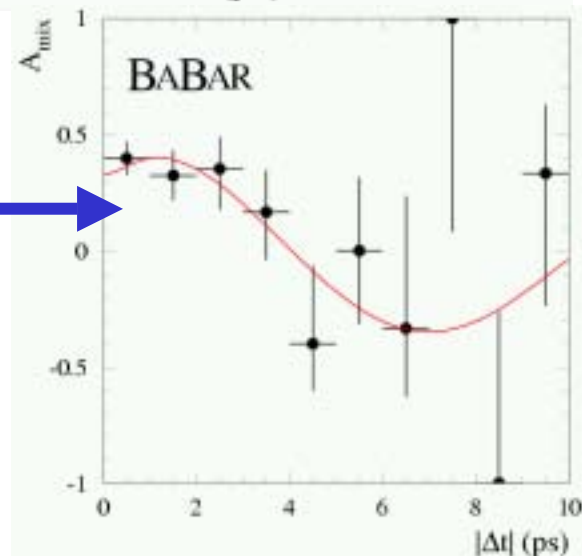
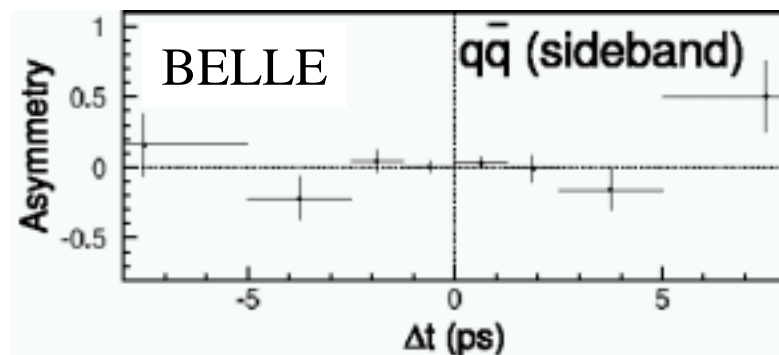
CP Asymmetries – Belle



- Rate difference ($= C_{\pi\pi}$)
- Δt -dependent asymmetry ($= S_{\pi\pi}$ and $C_{\pi\pi}$)

Crosschecks

- Both experiment made extensive crosschecks, e.g.
 - Asymmetry in background?
 - Look for asymmetries in $K\pi$ or mass sideband
 - Vertex resolution of the 2-body decays?
 - Measure B lifetime with $\pi\pi, K\pi$
 - Measure mixing with $K\pi$
 - Likelihood values and errors?
 - Toy Monte Carlo studies



Monte Carlo Fit Test

- Generate ~ 1000 “toy” experiments

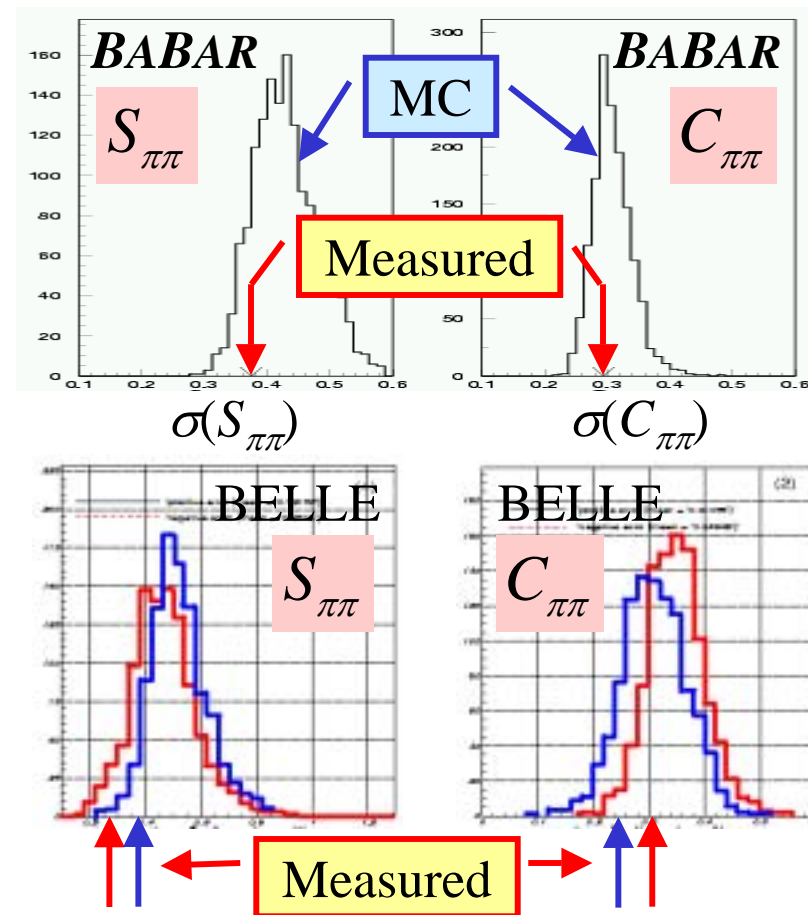
- Belle used $(-0.7, -0.7)$ for the central values

- Fit and compare:

- Likelihood values
- Pull distributions
- Errors

- Lowest probability: 5.4%

Everything looks reasonable



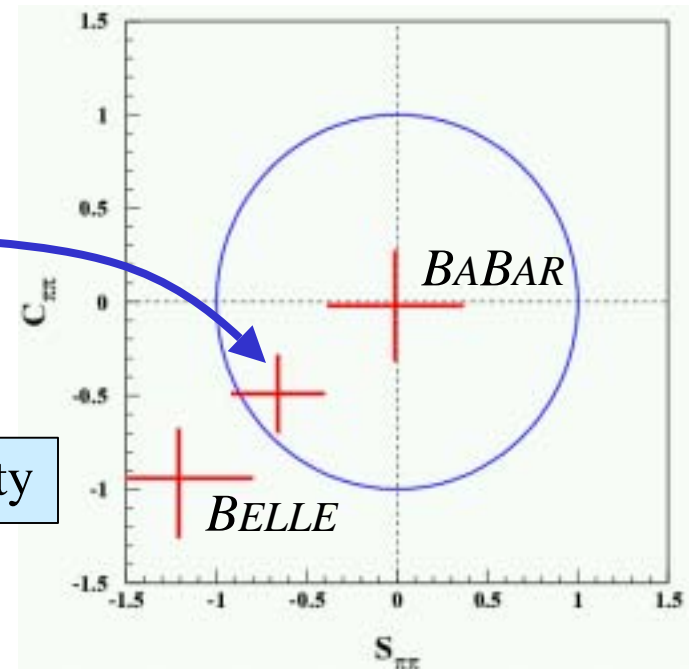
Interpretation

	BABAR (preliminary)	Belle (hep-ex/0204002)	Average*
$S_{\pi\pi}$	$-0.01 \pm 0.37 \pm 0.07$	$-1.21^{+0.38+0.16}_{-0.27-0.13}$	-0.66 ± 0.26
$C_{\pi\pi}$	$-0.02 \pm 0.29 \pm 0.07$	$-0.94^{+0.31}_{-0.25} \pm 0.09$	-0.49 ± 0.21

- How well do we know α ?
(*Gronau and Rosner, PRD65, 093012)

- Average BABAR and Belle
- Assume $\beta = 26^\circ$, $P/T = 0.28$

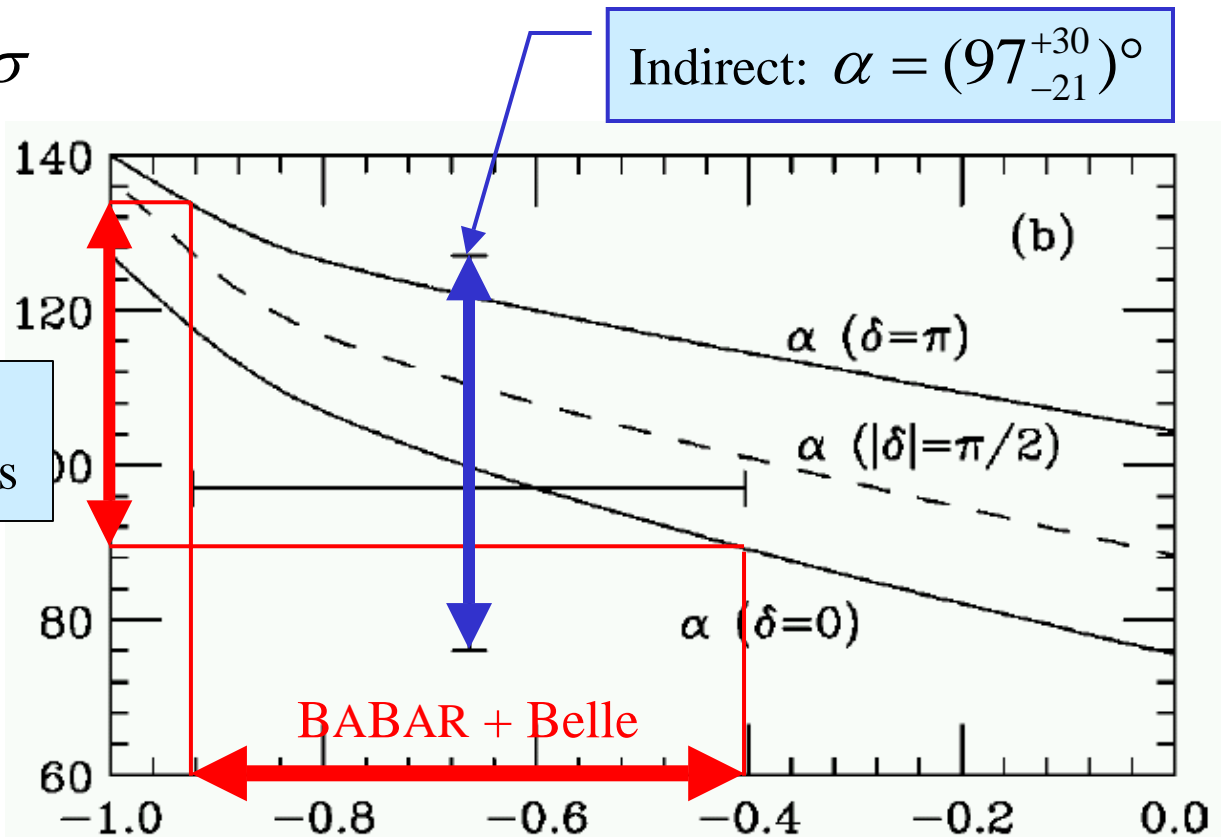
NB: Large uncertainty



Interpretation

- Measured $S_{\pi\pi} \pm 1\sigma$ corresponds to $\alpha \in [89^\circ, 138^\circ]$

Accuracy comparable to the indirect constraints



We are starting to *measure* α

$S_{\pi\pi}$

Gronau and Rosner
PRD65, 093012

Summary

- BABAR and Belle measured $\sin 2\alpha_{\text{eff}}$ using $B^0 \rightarrow \pi^+ \pi^-$

	BABAR (preliminary)	Belle (hep-ex/0204002)
$S_{\pi\pi}$	$-0.01 \pm 0.37 \pm 0.07$	$-1.21^{+0.38+0.16}_{-0.27-0.13}$
$C_{\pi\pi}$	$-0.02 \pm 0.29 \pm 0.07$	$-0.94^{+0.31}_{-0.25} \pm 0.09$

- Direct constraint on α is reaching useful accuracy
- Things to watch out for:
 - $\sin 2\alpha_{\text{eff}}$ with higher statistics \rightarrow Resolve “discrepancy”
 - $BR(B^0 \rightarrow \pi^0 \pi^0) \rightarrow$ Better bound on $\alpha_{\text{eff}} - \alpha$