# On the Measurement of Upstreamness and Downstreamness in Global Value Chains 

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## Overview

- Backdrop: Production processes are now global in nature, with intermediate inputs obtained from multiple countries and industries along global value chains (GVCs).
- Spurred an increased interest in understanding:
(i) Where are countries and industries located along GVCs?
(ii) What are the underlying determinants of country positioning along GVCs?


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- Backdrop: Production processes are now global in nature, with intermediate inputs obtained from multiple countries and industries along global value chains (GVCs).
- Spurred an increased interest in understanding:
(i) Where are countries and industries located along GVCs?
(ii) What are the underlying determinants of country positioning along GVCs?
- On (i): Recent work employing techniques and concepts from input-output analysis to provide descriptive answers.
(Fally 2012, Antràs et al. 2012, Antràs and Chor 2013, Alfaro et al. 2017, Miller and Temurshoev 2017, Wang et al. 2017)


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- Spurred an increased interest in understanding:
(i) Where are countries and industries located along GVCs?
(ii) What are the underlying determinants of country positioning along GVCs?
- On (ii): An emerging body of general equilibrium models, though not easy to structurally discipline these models.
(Yi 2003, Kohler 2004, Yi 2010, Harms et al. 2012, Baldwin and Venables 2013, Costinot et al. 2013, Antràs and Chor 2013, Fally and Hillberry 2014, Kikuchi et al. 2017, Tyazhelnikov 2017, Alexander 2017, Antràs and de Gortari 2017, de Gortari 2017)


## What we do

This paper: Attempts to provide a bridge between these two strands of work.

1. Review four measures that have been used to capture countries' and industries' GVC positioning (that are based on patterns of intermediate input and final-use purchases)
2. Document how these measures have evolved over time in the 1995-2011 World Input-Output Database (WIOD).

Will report several salient patterns and puzzling correlations
3. Develop an extension of Caliendo and Parro (2015) that can match all entries of a WIOD (i.e., the full pattern of intermediate input purchases and final-use expenditures)
4. Perform model-based counterfactuals to explore the role of: (i) trade cost movements; and (ii) changes in final consumption shares, in explaining the evolution of GVC positioning.

## Roadmap for this talk

1. Motivation and Introduction
2. Review of GVC Measures
3. The Evolution of GVC Positioning from 1995-2011
4. Proximate Explanations
5. Structural Model
6. Counterfactuals
7. Conclusion

# Measures of GVC Positioning 

## World Input-Output Table (WIOT)

GVC measures are defined with a WIOT in mind:

- Unit of analysis: Industry $r$ in country $i$
- J countries and $S$ industries/sectors
- JS by JS block of intermediate-use values
- JS by $J$ block of final-use values

|  |  |  | Input use \& value added |  |  |  |  |  |  | Final use |  |  | Total use |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Country 1 |  |  | $\cdots$ | Country J |  |  | Country 1 | ... | Country J |  |
|  |  |  | Industry 1 | ... | Industry $S$ | $\ldots$ | Industry 1 | $\cdots$ | Industry $S$ |  |  |  |  |
| Intermediate | Country 1 | Industry 1 | $Z_{11}^{11}$ | $\cdots$ | $Z_{11}^{1 S}$ | $\ldots$ | $Z_{1,}^{11}$ | $\cdots$ | $Z_{1,}^{1 S}$ | $F_{11}^{1}$ | $\cdots$ | $F_{1,}^{1}$ | $Y_{1}^{1}$ |
|  |  | $\cdots$ | $\cdots$ | $Z_{11}^{r s}$ | $\cdots$ | $\ldots$ | ... | $Z_{1,}^{r s}$ | $\cdots$ | $\ldots$ | $\cdots$ | $\cdots$ | $\cdots$ |
|  |  | Industry $S$ | $Z_{11}^{S 1}$ | $\cdots$ | $Z_{11}^{S S}$ | $\cdots$ | $Z_{1 . J}^{S 1}$ | $\cdots$ | $Z_{1 J}^{S S}$ | $F_{11}^{S}$ | $\cdots$ | $F_{1 . J}^{S}$ | $Y_{1}^{S}$ |
| inputs <br> supplied | ... | . $\quad$. | $\ldots$ | $\cdots$ | $\ldots$ | $Z_{i j}^{\text {rs }}$ | $\ldots$ | $\cdots$ | $\cdots$ | $\ldots$ | $F_{i j}^{r}$ | $\cdots$ | $Y_{i}^{r}$ |
|  | Country J | Industry 1 | $Z_{J 1}^{11}$ | $\cdots$ | $Z_{J 1}^{1 S}$ | $\bigcirc$ | $Z_{J J}^{11}$ | $\cdots$ | $Z_{J J}^{1 S}$ | $F_{J 1}^{1}$ | $\cdots$ | $F_{J J}^{1}$ | $Y_{J}^{1}$ |
|  |  | ... | $\cdots$ | $Z_{J 1}^{\text {rs }}$ | $\cdots$ | $\cdots$ | $\cdots$ | $Z_{J J}^{r s}$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ |
|  |  | Industry $S$ | $Z_{J 1}^{S 1}$ | $\cdots$ | $Z_{J 1}^{S S}$ | $\cdots$ | $Z_{J J}^{S 1}$ | $\ldots$ | $Z_{J J}^{S S}$ | $F_{J 1}^{S}$ | $\cdots$ | $F_{J, J}^{S}$ | $Y_{J}^{S}$ |
| Value added |  |  | $V A_{1}^{1}$ | $\cdots$ | $V A_{1}^{S}$ | $V A_{j}^{s}$ | $V A_{J}^{1}$ | $\cdots$ | $V A_{J}^{S}$ |  |  |  |  |
| Gross output |  |  | $Y_{1}^{1}$ | ... | $Y_{1}^{S}$ | $Y_{j}^{s}$ | $Y_{J}^{1}$ | $\cdots$ | $Y_{J}^{S}$ | $\ldots$ |  |  |  |

## World Input-Output Table (WIOT)

GVC measures are defined with a WIOT in mind:

- Rows: Uses of output from industry $r$ in country $i$
- Columns: Value-add and input-use in the production of industry $s$ in country $j$

|  |  |  | Input use \& value added |  |  |  |  |  |  | Final use |  |  | Total use |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Country 1 |  |  | $\cdots$ | Country J |  |  | Country 1 | $\cdots$ | Country J |  |
|  |  |  | Industry 1 | . $\cdots$ | Industry $S$ | $\cdots$ | Industry 1 | ... | Industry $S$ |  |  |  |  |
| Intermediate | Country 1 | Industry 1 | $Z_{11}^{11}$ | $\cdots$ | $Z_{11}^{1 S}$ | $\cdots$ | $Z_{1,}^{11}$ | $\cdots$ | $Z_{1 J}^{1 S}$ | $F_{11}^{1}$ | $\cdots$ | $F_{1,}^{1}$ | $Y_{1}^{1}$ |
|  |  | $\cdots$ | $\ldots$ | $Z_{11}^{\text {rs }}$ | ... | $\cdots$ | $\ldots$ | $Z_{1 J}^{\text {rs }}$ | $\ldots$ | $\ldots$ | $\cdots$ | ... | $\ldots$ |
|  |  | Industry $S$ | $Z_{11}^{S 1}$ | $\cdots$ | $Z_{11}^{S S}$ | $\cdots$ | $Z_{1 .}^{S 1}$ | $\cdots$ | $Z_{1 J}^{S S}$ | $F_{11}^{S}$ | $\cdots$ | $F_{1,}^{S}$ | $Y_{1}^{S}$ |
| inputs <br> supplied | $\ldots$ | ... | $\cdots$ | $\cdots$ | $\cdots$ | $Z_{i j}^{\text {rs }}$ | $\ldots$ | $\cdots$ | $\ldots$ | $\cdots$ | $F_{i j}^{r}$ | $\cdots$ | $Y_{i}^{r}$ |
|  | Country J | Industry 1 | $Z_{J 1}^{11}$ | $\cdots$ | $Z_{J 1}^{1 S}$ | $\cdots$ | $Z_{J J}^{11}$ | $\cdots$ | $Z_{J J}^{1 S}$ | $F_{J 1}^{1}$ | $\cdots$ | $F_{J J}^{1}$ | $Y_{J}^{1}$ |
|  |  | ... | $\cdots$ | $Z_{J 1}^{\text {rs }}$ | $\cdots$ | $\ldots$ | $\cdots$ | $Z_{J J}^{r s}$ | $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ | $\cdots$ |
|  |  | Industry $S$ | $Z_{J 1}^{S 1}$ | $\cdots$ | $Z_{J 1}^{S S}$ | $\cdots$ | $Z_{J J}^{S 1}$ | $\cdots$ | $Z_{J J}^{S S}$ | $F_{J 1}^{S}$ | $\cdots$ | $F_{J J}^{S}$ | $Y_{J}^{S}$ |
| Value added |  |  | $V A_{1}^{1}$ | $\cdots$ | $V A_{1}^{S}$ | $V A_{j}^{s}$ | $V A_{J}^{1}$ | $\cdots$ | $V A_{J}^{S}$ | $\cdots$ |  |  |  |
| Gross output |  |  | $Y_{1}^{1}$ | $\cdots$ | $Y_{1}^{S}$ | $Y_{j}^{s}$ | $Y_{J}^{1}$ | $\cdots$ | $Y_{J}^{S}$ |  |  |  |  |  |

## Upstreamness from Final Use

Define the direct requirements coefficient: $a_{i j}^{r s}=Z_{i j}^{r s} / Y_{j}^{s}$.

- Start from the output accounting identity:

$$
\begin{equation*}
Y_{i}^{r}=\sum_{s=1}^{s} \sum_{j=1}^{J} a_{i j}^{r s} Y_{j}^{s}+F_{i}^{r} . \tag{1}
\end{equation*}
$$

- Iterate to obtain:

$$
\begin{equation*}
Y_{i}^{r}=F_{i}^{r}+\sum_{s=1}^{S} \sum_{j=1}^{J} a_{i j}^{r s} F_{j}^{s}+\sum_{s=1}^{s} \sum_{j=1}^{J} \sum_{t=1}^{S} \sum_{k=1}^{J} a_{i j}^{r s} a_{j k}^{s t} F_{k}^{t}+\ldots \tag{2}
\end{equation*}
$$

## Upstreamness from Final Use

Define the direct requirements coefficient: $a_{i j}^{r s}=Z_{i j}^{r s} / Y_{j}^{s}$.

- Start from the output accounting identity:

$$
\begin{equation*}
Y_{i}^{r}=\sum_{s=1}^{S} \sum_{j=1}^{J} a_{i j}^{r s} Y_{j}^{s}+F_{i}^{r} \tag{1}
\end{equation*}
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- Iterate to obtain:

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Y_{i}^{r}=F_{i}^{r}+\sum_{s=1}^{S} \sum_{j=1}^{J} a_{i j}^{r s} F_{j}^{s}+\sum_{s=1}^{s} \sum_{j=1}^{J} \sum_{t=1}^{s} \sum_{k=1}^{J} a_{i j}^{r s} a_{j k}^{s t} F_{k}^{t}+\ldots \tag{2}
\end{equation*}
$$

Simple measure: Final use share in gross output

$$
\begin{equation*}
F / G O=F_{i}^{r} / Y_{i}^{r} \tag{3}
\end{equation*}
$$

## Upstreamness from Final Use

Richer measure: Taking into account production-staging distance from final use

$$
\begin{equation*}
U_{i}^{r}=1 \times \frac{F_{i}^{r}}{Y_{i}^{r}}+2 \times \frac{\sum_{s=1}^{S} \sum_{j=1}^{J} a_{i j}^{r s} F_{j}^{s}}{Y_{i}^{r}}+3 \times \frac{\sum_{s=1}^{S} \sum_{j=1}^{J} \sum_{t=1}^{S} \sum_{k=1}^{J} a_{i j}^{r s} a_{j k}^{s t} F_{k}^{t}}{Y_{i}^{r}}+\ldots \tag{4}
\end{equation*}
$$

## Remarks:

- $U_{i}^{r} \geq 1$
- $U_{i}^{r}$ larger if use occurs on average more stages upstream from final demand
- Computation:
- Numerator $=[I-\mathbf{A}]^{-2} \mathbf{F}$
- Denominator $=[I-\mathbf{A}]^{-1} \mathbf{F}$
where $\mathbf{A}$ is the $J S$ by $J S$ matrix of the $a_{i j}^{r s}$ 's (direct requirements matrix); and $\mathbf{F}$ is the $J S$ by 1 vector of the $F_{i}^{r}$ 's.


## Upstreamness from Final Use

- An alternative recursive formulation:

$$
\begin{equation*}
\tilde{U}_{i}^{r}=1+\sum_{s=1}^{s} \sum_{j=1}^{J} b_{i j}^{r s} \tilde{U}_{j}^{s} \tag{5}
\end{equation*}
$$

so industries are upstream if they sell to industries that are themselves relatively upstream.

- Equivalence result from Antràs et al. (2012):

$$
\tilde{U}_{i}^{r}=U_{i}^{r}
$$

## Downstreamness from Primary Factors

Define: $b_{i j}^{r s}=Z_{i j}^{r s} / Y_{i}^{r}$.

- Output accounting identity from the perspective of sources of value-added:

$$
Y_{j}^{s}=\sum_{r=1}^{s} \sum_{i=1}^{J} b_{i j}^{r s} Y_{i}^{r}+V A_{j}^{s}
$$

- Iterate to obtain:

$$
Y_{j}^{s}=V A_{j}^{s}+\sum_{r=1}^{S} \sum_{i=1}^{J} b_{i j}^{r s} V A_{i}^{r}+\sum_{r=1}^{S} \sum_{i=1}^{J} \sum_{t=1}^{S} \sum_{k=1}^{J} b_{k i}^{t r} b_{i j}^{r s} V A_{k}^{t}+\ldots
$$

## Downstreamness from Primary Factors

Define: $b_{i j}^{\text {rs }}=Z_{i j}^{r s} / Y_{i}^{r}$.

- Output accounting identity from the perspective of sources of value-added:

$$
Y_{j}^{s}=\sum_{r=1}^{S} \sum_{i=1}^{J} b_{i j}^{r s} Y_{i}^{r}+V A_{j}^{s}
$$

- Iterate to obtain:

$$
Y_{j}^{s}=V A_{j}^{s}+\sum_{r=1}^{s} \sum_{i=1}^{J} b_{i j}^{r s} V A_{i}^{r}+\sum_{r=1}^{S} \sum_{i=1}^{J} \sum_{t=1}^{S} \sum_{k=1}^{J} b_{k i}^{t r} b_{i j}^{r s} V A_{k}^{t}+\ldots
$$

Simple measure: Value-added share in gross output

$$
\begin{equation*}
V A / G O=V A_{j}^{s} / Y_{j}^{s} \tag{6}
\end{equation*}
$$

## Downstreamness from Primary Factors

Richer measure:

$$
\begin{equation*}
D_{j}^{s}=1 \times \frac{V A_{j}^{s}}{Y_{j}^{s}}+2 \times \frac{\sum_{r=1}^{S} \sum_{i=1}^{J} b_{i j}^{r s} V A_{i}^{r}}{Y_{j}^{s}}+3 \times \frac{\sum_{r=1}^{S} \sum_{i=1}^{J} \sum_{t=1}^{S} \sum_{k=1}^{J} b_{k i}^{t r} b_{i j}^{r s} V A_{k}^{t}}{Y_{j}^{s}}+\ldots \tag{7}
\end{equation*}
$$

## Remarks:

- $D_{j}^{s} \geq 1$
- $D_{j}^{s}$ larger if use occurs on average more stages downstream from primary factors
- Computation:
- Numerator $=[I-\mathbf{B}]^{-2} \mathbf{V}$
- Denominator $=[I-\mathbf{B}]^{-1} \mathbf{V}$
where $\mathbf{B}$ is the $J S$ by $J S$ matrix of the $b_{i j}^{r s}$ 's (allocation matrix); and $\mathbf{V}$ is the $J S$ by 1 vector of the $V A_{j}^{s}$ 's.


## Downstreamness from Primary Factors

- Alternative recursive formulation:

$$
\begin{equation*}
\tilde{D}_{j}^{s}=1+\sum_{i=1}^{J} \sum_{r=1}^{s} a_{i j}^{r s} \tilde{D}_{i}^{r} \tag{8}
\end{equation*}
$$

so industries are downstream if they purchase inputs from industries that are themselves relatively downstream.

Result from Fally (2012) and Miller and Temurshoev (2017):

$$
\tilde{D}_{j}^{s}=D_{j}^{s}
$$

## Aggregation

Four GVC measures at the country-industry level: $F / G O, U, V A / G O, D$.
Two approaches to aggregate to the country level:
(i) Take a GO-weighted average of the country-industry GVC measures
(ii) Collapse the WIOT to a country-by-country I-O table, and compute the GVC measures

- Both approaches clearly equivalent for $F / G O$ and VA/GO.
- Not equivalent, but very highly correlated for $U$ and $D$.


## Aggregation

Four GVC measures at the country-industry level: $F / G O, U, V A / G O, D$.
Two approaches can be applied to aggregate to the world level as well:

- Both approaches clearly equivalent for $F / G O$ and VA/GO still.
- But at the world level, aggregate finale expenditures equal aggregate payments to primary factors, so:

$$
\bar{F} / \overline{G O}=\overline{V A} / \overline{G O}
$$

- Far less obvious, but $G O$-weighted $U$ and $D$ at the world level are also equal (Miller and Temurshoev 2017):

$$
\bar{U}=\bar{D}
$$

- Thus: At the world-level, view these more as measures of production complexity, rather than positioning.

GVC Positioning from 1995-2011 (from the World Input-Output Database)

## To the WIOD Data. . .

Use 2013 edition of the World Input-Output Database, c.f. Timmer et al. (2015)

- $J=41$ countries
- $S=35$ industries/sectors
- 16 years: 1995-2011
- A lot of data points!
$Z_{i j}^{\text {rs }}$ matrix in any year: $(35 \times 41)^{2}=2,059,225$
$F_{i j}^{r}$ matrix in any year: $35 \times 41^{2}=58,835$
- Computational detail: Apply a net inventories correction Antràs et al. (2012)

For the World as a whole...

- $\bar{F} / \overline{G O}$ and $\overline{V A} / \overline{G O}$ on the decline
- $\bar{U}$ and $\bar{D}$ on the rise
- Upshot: GVCs appear to be "lengthening"




## Country-level GVC Measures over Time

- Similar patterns present across different percentiles of the country-level distribution of the respective GVC measures



## Country-level GVC Measures over Time (cont.)

- Striking stability and persistence in rank order

| Rank: | F/GO (1995) |  | F/GO (2011) |  | Rank: | VA/GO (1995) |  | VA/GO (2011) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | China | 0.384 | Luxembourg | 0.296 | 1. | China | 0.373 | China | 0.325 |
| 2. | Luxembourg | 0.388 | China | 0.340 | 2. | Czech Rep. | 0.403 | Luxembourg | 0.362 |
| 3. | Slovakia | 0.394 | Korea | 0.377 | 3. | Slovakia | 0.416 | Korea | 0.372 |
|  | Czech Rep. | 0.408 | Taiwan | 0.396 | 4. | Estonia | 0.430 | Czech Rep. | 0.383 |
| 5. | Russia | 0.444 | Czech Rep. | 0.401 | 5. | Romania | 0.454 | Bulgaria | 0.401 |
| 37. | Denmark | 0.558 | Brazil | 0.557 | 37. | Austria | 0.563 | Brazil | 0.561 |
| 38. | Brazil | 0.572 | USA | 0.569 | 38. | Turkey | 0.575 | USA | 0.562 |
| 39. | Turkey | 0.605 | Mexico | 0.586 | 39. | Brazil | 0.575 | Mexico | 0.581 |
| 40. | Greece | 0.625 | Cyprus | 0.637 | 40. | Greece | 0.576 | Cyprus | 0.586 |
| 41. | Cyprus | 0.709 | Greece | 0.668 | 41. | Cyprus | 0.625 | Greece | 0.628 |
| Rank: | $\underline{\mathrm{U}}$ (1995) |  | $\underline{\mathrm{U}}$ (2011) |  | Rank: | D (1995) |  | $\underline{\mathrm{D}}$ (2011) |  |
| 1. | Cyprus | 1.451 | Greece | 1.546 | 1. | Cyprus | 1.662 | Greece | 1.657 |
| 2. | Greece | 1.611 | Cyprus | 1.617 | 2. | Brazil | 1.748 | Cyprus | 1.763 |
| 3. | Turkey | 1.666 | Mexico | 1.737 | 3. | Turkey | 1.758 | Mexico | 1.779 |
| 4. | Brazil | 1.755 | USA | 1.786 | 4. | Greece | 1.759 | Brazil | 1.806 |
| 5. | Denmark | 1.810 | Brazil | 1.824 | 5. | Austria | 1.800 | USA | 1.808 |
| 37. | Russia | 2.185 | Czech Rep. | 2.358 | 37. | Romania | 2.155 | Luxembourg | 2.348 |
|  | Luxembourg | 2.242 | Taiwan | 2.463 | 38. | Estonia | 2.209 | Bulgaria | 2.370 |
|  | Czech Rep. | 2.331 | Korea | 2.544 | 39. | Slovakia | 2.306 | Czech Rep. | 2.444 |
| 40. | Slovakia | 2.389 | Luxembourg | 2.581 |  | Czech Rep. | 2.344 | Korea | 2.534 |
| 41. | China | 2.535 | China | 2.819 | 41. | China | 2.591 | China | 2.900 |

## Country-industry GVC Measures over Time

- Focusing on the "pure" within-component of the variation:

Still find $F / G O$ and $V A / G O$ on the decline; $U$ and $D$ on the rise

$$
\begin{equation*}
G V C_{j, t}^{s}=\beta_{1} \text { Year }_{t}+F E_{j}^{s}+\epsilon_{j, t}^{s} . \tag{9}
\end{equation*}
$$

| Dependent variable: | $\mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ <br> (1) | $\mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ <br> (2) | $\mathrm{VA} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ <br> (3) | $\mathrm{VA} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ <br> (4) | $\begin{gathered} (\mathrm{U})_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ (5) \end{gathered}$ | $\begin{gathered} (U)_{j, t}{ }^{5} \\ (6) \end{gathered}$ | $\begin{gathered} (\mathrm{D})_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ (7) \end{gathered}$ | $\begin{gathered} (\mathrm{D})_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}} \\ (8) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | $\begin{aligned} & -0.0009^{*} \\ & {[0.0004]} \end{aligned}$ |  | $\begin{gathered} -0.0017^{* * *} \\ {[0.0005]} \end{gathered}$ |  | $\begin{aligned} & 0.0064^{* * *} \\ & {[0.0015]} \end{aligned}$ |  | $\begin{aligned} & 0.0084^{* * *} \\ & {[0.0017]} \end{aligned}$ |  |
| (Dum: Year=1996) |  | $\begin{gathered} -0.0002 \\ {[0.0025]} \end{gathered}$ |  | $\begin{gathered} -0.0012 \\ {[0.0026]} \end{gathered}$ |  | $\begin{gathered} -0.0060 \\ {[0.0083]} \end{gathered}$ |  | $\begin{gathered} 0.0019 \\ {[0.0079]} \end{gathered}$ |
| (Dum: Year=1997) |  | $\begin{gathered} -0.0015 \\ {[0.0020]} \end{gathered}$ |  | $\begin{gathered} -0.0024 \\ {[0.0020]} \end{gathered}$ |  | $\begin{gathered} 0.0026 \\ {[0.0068]} \end{gathered}$ |  | $\begin{gathered} 0.0061 \\ {[0.0062]} \end{gathered}$ |
| (Dum: Year=1998) |  | $\begin{aligned} & 0.0026^{* *} \\ & {[0.0010]} \end{aligned}$ |  | $\begin{gathered} 0.0002 \\ {[0.0015]} \end{gathered}$ |  | $\begin{gathered} -0.0129^{* * *} \\ {[0.0032]} \end{gathered}$ |  | $\begin{aligned} & -0.0085^{*} \\ & {[0.0043]} \end{aligned}$ |
| (Dum: Year=1999) |  | $\begin{aligned} & 0.0029^{* * *} \\ & {[0.0004]} \end{aligned}$ |  | $\begin{gathered} -0.0005 \\ {[0.0005]} \end{gathered}$ |  | $\begin{gathered} -0.0086^{* * *} \\ {[0.0010]} \end{gathered}$ |  | $\begin{gathered} -0.0073^{* * *} \\ {[0.0025]} \end{gathered}$ |
| (Dum: Year=2000) |  | $\begin{gathered} -0.0015 \\ {[0.0014]} \end{gathered}$ |  | $\begin{gathered} -0.0094^{* * *} \\ {[0.0016]} \end{gathered}$ |  | $\begin{aligned} & 0.0140^{* * *} \\ & {[0.0045]} \end{aligned}$ |  | $\begin{aligned} & 0.0311^{* * *} \\ & {[0.0044]} \end{aligned}$ |
| (Dum: Year=2001) |  | $\begin{gathered} -0.0022 \\ {[0.0020]} \end{gathered}$ |  | $\begin{aligned} & -0.0122^{* * *} \\ & {[0.0021]} \end{aligned}$ |  | $\begin{aligned} & 0.0182^{* *} \\ & {[0.0065]} \end{aligned}$ |  | $\begin{aligned} & 0.0394^{* * *} \\ & {[0.0053]} \end{aligned}$ |
| (Dum: Year=2002) |  | $\begin{gathered} -0.0010 \\ {[0.0024]} \end{gathered}$ |  | $\begin{gathered} -0.0091^{* * *} \\ {[0.0022]} \end{gathered}$ |  | $\begin{gathered} 0.0069 \\ {[0.0069]} \end{gathered}$ |  | $\begin{aligned} & 0.0218^{* * *} \\ & {[0.0054]} \end{aligned}$ |
| (Dum: Year=2003) |  | $\begin{gathered} -0.0033 \\ {[0.0027]} \end{gathered}$ |  | $\begin{gathered} -0.0102^{\star * *} \\ {[0.0022]} \end{gathered}$ |  | $\begin{aligned} & 0.0204^{* *} \\ & {[0.0082]} \end{aligned}$ |  | $\begin{aligned} & 0.0334^{* * *} \\ & {[0.0059]} \end{aligned}$ |
| (Dum: Year=2004) |  | $\begin{gathered} -0.0052 \\ {[0.0030]} \end{gathered}$ |  | $\begin{aligned} & -0.0135^{* * *} \\ & {[0.0025]} \end{aligned}$ |  | $\begin{aligned} & 0.0346^{* * *} \\ & {[0.0100]} \end{aligned}$ |  | $\begin{aligned} & 0.0490^{* * *} \\ & {[0.0079]} \end{aligned}$ |
| (Dum: Year=2005) |  | $\begin{aligned} & -0.0061^{*} \\ & {[0.0031]} \end{aligned}$ |  | $\begin{gathered} -0.0153^{* * *} \\ {[0.0032]} \end{gathered}$ |  | $\begin{aligned} & 0.0421^{* * *} \\ & {[0.0099]} \end{aligned}$ |  | $\begin{aligned} & 0.0657^{* * *} \\ & {[0.0101]} \end{aligned}$ |

## Correlations in GVC Measures across Countries

- In an autarkic world, aggregate $F$ and VA would be equal as a national accounting identity.
$\Rightarrow$ Would expect a perfect positive correlation in $F / G O$ and VA/GO across countries
- Conversely, would expect that as trade costs fall and production becomes more fragmented, this tight correlation between $F / G O$ and VA/GO would weaken.
- Logic should carry over to correlation between $U$ and $D$ as well, since $F / G O$ and $U$ are negatively correlated (as are VA/GO and $D$ )


## Puzzling Correlations

- Correlation between $F / G O$ and $V A / G O$ (as well as between $U$ and $D$ ) shows no signs of weakening!






## Puzzling Correlations

- Correlation between $F / G O$ and VA/GO (as well as between $U$ and $D$ ) shows no signs of weakening!



## Puzzling Correlations

- Correlation between $F / G O$ and VA/GO (as well as between $U$ and $D$ ) shows no signs of weakening!



## Puzzling Correlations (at the country-industry level)

- Positive slope coefficient even in the country-industry GVC measures

$$
\begin{equation*}
F / G O_{j, t}^{s}=\beta_{1} V A / G O_{j, t}^{s}+F E_{j}+F E^{s}+\epsilon_{j, t}^{s}, \tag{10}
\end{equation*}
$$

| Dependent variable: | $\begin{gathered} \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ 1995 \end{gathered}$ <br> (1) | $\begin{gathered} \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ 1995 \\ (2) \end{gathered}$ | $\begin{gathered} \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ 1995 \\ \text { (3) } \end{gathered}$ | $\begin{gathered} \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ 2011 \end{gathered}$ <br> (4) | $\begin{gathered} \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}} \\ 2011 \\ (5) \end{gathered}$ | $\begin{gathered} {\mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}^{\mathrm{s}}}_{2011} \end{gathered}$ <br> (6) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{VA} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\text {s }}$ | $\begin{aligned} & 0.5438^{* * *} \\ & {[0.1815]} \end{aligned}$ | $\begin{aligned} & 0.5196^{* *} \\ & {[0.1924]} \end{aligned}$ | $\begin{gathered} 0.0775 \\ {[0.0543]} \end{gathered}$ | $\begin{aligned} & 0.6543^{* * *} \\ & {[0.1647]} \end{aligned}$ | $\begin{aligned} & 0.6373^{* * *} \\ & {[0.1740]} \end{aligned}$ | $\begin{aligned} & 0.2647^{* * *} \\ & {[0.0527]} \end{aligned}$ |
| Country FE? <br> Industry FE? | $\begin{aligned} & \mathrm{N} \\ & \mathrm{~N} \end{aligned}$ | $\begin{aligned} & \mathrm{Y} \\ & \mathrm{~N} \end{aligned}$ | $\begin{aligned} & Y \\ & Y \end{aligned}$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{~N} \end{aligned}$ | $\begin{aligned} & \mathrm{Y} \\ & \mathrm{~N} \end{aligned}$ | $\begin{aligned} & Y \\ & Y \end{aligned}$ |
| Observations $\mathrm{R}^{2}$ | $\begin{gathered} 1,417 \\ 0.1285 \end{gathered}$ | $\begin{gathered} 1,417 \\ 0.1488 \end{gathered}$ | $\begin{gathered} 1,417 \\ 0.8392 \end{gathered}$ | $\begin{gathered} 1,414 \\ 0.1927 \end{gathered}$ | $\begin{gathered} 1,414 \\ 0.2033 \end{gathered}$ | $\begin{gathered} 1,414 \\ 0.8479 \end{gathered}$ |
| Dependent variable: | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{~b}} \\ 1995 \\ (7) \end{gathered}$ | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{t}}^{\mathrm{t}} \\ 1995 \\ \text { (8) } \end{gathered}$ | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{~b}} \\ 1995 \\ (9) \end{gathered}$ | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{~s}} \\ 2011 \\ (10) \end{gathered}$ | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{t}} \\ 2011 \\ (11) \end{gathered}$ | $\begin{gathered} \mathrm{U}_{\mathrm{j}, \mathrm{t}}^{\mathrm{t}} \\ 2011 \\ (12) \end{gathered}$ |
| $\mathrm{D}_{\mathrm{j}, \mathrm{t}^{\text {e }}}$ | $\begin{aligned} & 0.5308^{* * *} \\ & {[0.1640]} \end{aligned}$ | $\begin{aligned} & 0.4820^{\star} \\ & {[0.1902]} \end{aligned}$ | $\begin{aligned} & 0.2413^{* * *} \\ & {[0.0604]} \end{aligned}$ | $\begin{aligned} & 0.6213^{* * *} \\ & {[0.1454]} \end{aligned}$ | $\begin{aligned} & 0.5707^{* *} \\ & {[0.1698]} \end{aligned}$ | $\begin{aligned} & 0.3772^{* * *} \\ & {[0.0617]} \end{aligned}$ |
| Country FE? <br> Industry FE? | $\begin{aligned} & \mathrm{N} \\ & \mathrm{~N} \end{aligned}$ | Y | Y | N N | Y N | Y |
| Observations $\mathrm{R}^{2}$ | $\begin{gathered} 1,435 \\ 0.1350 \end{gathered}$ | $\begin{gathered} 1,435 \\ 0.1742 \end{gathered}$ | $\begin{gathered} 1,435 \\ 0.8264 \end{gathered}$ | $\begin{gathered} 1,435 \\ 0.1946 \end{gathered}$ | $\begin{gathered} 1,435 \\ 0.2232 \end{gathered}$ | $\begin{gathered} 1,435 \\ 0.8325 \end{gathered}$ |

## Two Candidate Explanations

## 1. Trade Costs

- Could be that trade costs remain high in absolute levels
- Use the Head-Reis index to get an empirical handle on this:

$$
\begin{align*}
\tau_{i j}^{r s} & =\left(\frac{Z_{i j}^{r s} Z_{j i}^{r s}}{Z_{i i}^{r s} Z_{j j}^{r s}}\right)^{-\frac{1}{2 \theta}}, \text { and }  \tag{11}\\
\tau_{i j}^{r F} & =\left(\frac{F_{i j}^{r} F_{j i}^{r}}{F_{i i}^{r} F_{j j}^{r}}\right)^{-\frac{1}{2 \theta}} \tag{12}
\end{align*}
$$

(Assume either: (i) $\theta=5$; or (ii) use Caliendo-Parro (2015) sectoral-level estimates.)

## 1. Trade Costs

- Average $\tau$ remains high at the end of the period...
- However: Clear overall downward trend particularly in the earlier half of the period



## 1. Trade Costs

- Decline in trade costs borne out robustly in regressions

$$
\begin{equation*}
\ln \tau_{i j, t}^{r s}=\beta_{0} Y_{e a r}+F E_{i j}^{r s}+\epsilon_{i j, t}^{r s}, \text { and } \tag{13}
\end{equation*}
$$

| Dependent variable: | log Trade Costs for Intermediate Inputs |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (3) | (4) |
| Industries: | All | All | Goods | Goods | Services | Services |
| Year | $\begin{gathered} -0.0164^{* * *} \\ {[0.0022]} \end{gathered}$ |  | $\begin{gathered} -0.0181^{* * *} \\ {[0.0024]} \end{gathered}$ |  | $\begin{gathered} -0.0150 * * * \\ {[0.0026]} \end{gathered}$ |  |
| Dum: Year=1996 |  | $\begin{gathered} -0.0052 \\ {[0.0093]} \end{gathered}$ |  | $\begin{aligned} & -0.0211^{*} \\ & {[0.0108]} \end{aligned}$ |  | $\begin{gathered} 0.0085 \\ {[0.0142]} \end{gathered}$ |
| Dum: Year=1997 |  | $\begin{gathered} -0.0782^{* * *} \\ {[0.0048]} \end{gathered}$ |  | $\begin{gathered} -0.0982^{* * *} \\ {[0.0075]} \end{gathered}$ |  | $\begin{gathered} -0.0609^{* * *} \\ {[0.0061]} \end{gathered}$ |
| Dum: Year=1998 |  | $\begin{gathered} -0.1108^{* * *} \\ {[0.0039]} \end{gathered}$ |  | $\begin{gathered} -0.1503^{* * *} \\ {[0.0077]} \end{gathered}$ |  | $\begin{gathered} -0.0768^{* * *} \\ {[0.0055]} \end{gathered}$ |
| Dum: Year=1999 |  | $\begin{gathered} -0.1129^{* * *} \\ {[0.0048]} \end{gathered}$ |  | $\begin{gathered} -0.1598^{* * *} \\ {[0.0074]} \end{gathered}$ |  | $\begin{gathered} -0.0725^{* * *} \\ {[0.0063]} \end{gathered}$ |
| Dum: Year=2000 |  | $\begin{gathered} -0.1562^{* * *} \\ {[0.0056]} \end{gathered}$ |  | $\begin{gathered} -0.1850^{\star * *} \\ {[0.0079]} \end{gathered}$ |  | $\begin{gathered} -0.1313^{* * *} \\ {[0.0086]} \end{gathered}$ |
| Dum: Year=2001 |  | $\begin{gathered} -0.1653^{* * *} \\ {[0.0067]} \end{gathered}$ |  | $\begin{gathered} -0.2021^{* * *} \\ {[0.0093]} \end{gathered}$ |  | $\begin{gathered} -0.1336^{* * *} \\ {[0.0099]} \end{gathered}$ |
| Dum: Year=2002 |  | $\begin{gathered} -0.1594^{* * *} \\ {[0.0064]} \end{gathered}$ |  | $\begin{gathered} -0.1936^{* * *} \\ {[0.0079]} \end{gathered}$ |  | $\begin{gathered} -0.1299^{* * *} \\ {[0.0107]} \end{gathered}$ |
| Dum: Year=2003 |  | $\begin{gathered} -0.1778^{* * *} \\ {[0.0100]} \end{gathered}$ |  | $\begin{gathered} -0.2141^{* * *} \\ {[0.0123]} \end{gathered}$ |  | $\begin{gathered} -0.1465^{* * *} \\ {[0.0154]} \end{gathered}$ |
| Dum: Year=2004 |  | $\begin{gathered} -0.2019^{* * *} \\ {[0.0097]} \end{gathered}$ |  | $\begin{gathered} -0.2219^{* * *} \\ {[0.0115]} \end{gathered}$ |  | $\begin{gathered} -0.1846^{* * *} \\ {[0.0155]} \end{gathered}$ |
| Dum: Year=2005 |  | $\begin{gathered} -0.2239^{* * *} \\ {[0.0109]} \end{gathered}$ |  | $\begin{gathered} -0.2558^{* * *} \\ {[0.0147]} \end{gathered}$ |  | $\begin{gathered} -0.1965^{* * *} \\ {[0.0159]} \end{gathered}$ |

## 1. Trade Costs

- Decline in trade costs borne out robustly in regressions



## 2. Sectoral Composition

- Key observation: Services tend to feature a higher share of output going straight to final demand, as well as a higher share of use of primary factors In other words: Services are in "short chains", while goods are in "long chains" >Details
- If some countries are more specialized in goods and others in industries, this can account for the positive cross-country correlation between $F / G O$ and VA/GO (as well as between $U$ and $D$ )
- Could be consistent with a decline in trade costs, if this decline reinforces pre-existing patterns of specialization


## 2. Sectoral Composition

- A secular rise over time in service share of gross output. . .
- BUT: Some signs that patterns of specialization in services have become more concentrated over time




## 2. Sectoral Composition

- At the country-industry level: Positive slope coefficient between GVC measures is driven by services



## 2. Sectoral Composition

- At the country-industry level: Positive slope coefficient between GVC measures is driven by services



## 2. Sectoral Composition

- Share of services in final expenditures has been on the rise, while that for goods has fallen

$$
\begin{equation*}
\ln \alpha_{j, t}^{s}=\beta_{0} \text { Year }_{t}+F E_{j}^{s}+\epsilon_{j, t}^{s} \tag{15}
\end{equation*}
$$

| Dependent variable: | $\boldsymbol{l o g}$ Expenditure Shares, $\alpha_{j}^{\text {s }}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) |
|  | All | All | Goods | Goods | Services | Services |
| Year | -0.0038 |  | -0.0127*** |  | 0.0037 |  |
|  | [0.0025] |  | [0.0037] |  | [0.0025] |  |
| Dum: Year=1996 |  | 0.0016 |  | -0.0087 |  | 0.0104 |
|  |  | [0.0148] |  | [0.0183] |  | [0.0200] |
| Dum: Year=1997 |  | -0.0078 |  | -0.0230* |  | 0.0050 |
|  |  | [0.0117] |  | [0.0127] |  | [0.0137] |
| Dum: Year=1998 |  | -0.0139 |  | -0.0493*** |  | 0.0160** |
|  |  | [0.0081] |  | [0.0158] |  | [0.0059] |
| Dum: Year=1999 |  | -0.0070*** |  | -0.0633*** |  | $0.0405^{* * *}$ |
|  |  | [0.0022] |  | [0.0077] |  | [0.0036] |
| Dum: Year=2000 |  | 0.0028 |  | $-0.0497 * * *$ |  | 0.0470*** |
|  |  | [0.0060] |  | [0.0130] |  | [0.0086] |
| Dum: Year=2001 |  | -0.0013 |  | -0.0718*** |  | $0.0582^{* * *}$ |
|  |  | [0.0099] |  | [0.0119] |  | [0.0155] |
| Dum: Year=2002 |  | -0.0123 |  | -0.0991*** |  | 0.0609** |
|  |  | [0.0144] |  | [0.0104] |  | [0.0231] |
| Dum: Year=2003 |  | -0.0192 |  | -0.1171*** |  | $0.0633^{* *}$ |
|  |  | [0.0159] |  | [0.0134] |  | [0.0222] |
| Dum: Year=2004 |  | -0.0165 |  | $-0.1130^{* * *}$ |  | $0.0648^{* *}$ |
|  |  | [0.0185] |  | [0.0250] |  | [0.0212] |
| Dum: Year=2005 |  | -0.0136 |  | -0.1123*** |  | $0.0697 * * *$ |
|  |  | [0.0216] |  | [0.0344] |  | [0.0232] |

## 2. Sectoral Composition

- Share of services in input purchases has been on the rise, while that for goods has fallen

$$
\begin{equation*}
\ln \gamma_{j, t}^{r s}=\beta_{0} \text { Year }_{t}+F E_{j}^{r s}+\epsilon_{j, t}^{r s} \tag{16}
\end{equation*}
$$



## Model

## Recap: Caliendo-Parro (2015)

General equilibrium model of cross-country production and trade with inter-sectoral linkages, that builds on the Eaton-Kortum machinery

## Setup:

- $i$ and $j$ denote countries; $i j$ subscript indicates a shipment from $i$ to $j$
- $r$ and $s$ denote industries; $r$ superscript indicates a shipment from $r$ to $s$

Preferences: Cobb-Douglas

$$
\begin{equation*}
u\left(C_{j}\right)=\prod_{s=1}^{s}\left(C_{j}^{s}\right)^{\alpha_{j}^{s}} \tag{17}
\end{equation*}
$$

where $C_{j}^{s}$ is a sector-s composite over a unit measure of varieties (see below)

## Recap: Caliendo-Parro (2015)

General equilibrium model of cross-country production and trade with inter-sectoral linkages, that builds on the Eaton-Kortum machinery

## Setup:

- $i$ and $j$ denote countries; $i j$ subscript indicates a shipment from $i$ to $j$
- $r$ and $s$ denote industries; $r s$ superscript indicates a shipment from $r$ to $s$

Production: Cobb-Douglas over labor and intermediates from all sectors

$$
\begin{equation*}
y_{j}^{s}\left(\omega^{s}\right)=z_{j}^{s}\left(\omega^{s}\right)\left(l_{j}^{s}\left(\omega^{s}\right)\right)^{1-\sum_{r=1}^{S} \gamma_{j}^{r s}} \prod_{r=1}^{S}\left(\mathcal{M}_{j}^{r s}\left(\omega^{s}\right)\right)^{\gamma_{j}^{r s}} \tag{18}
\end{equation*}
$$

where $z_{j}^{s}\left(\omega^{s}\right)$ are iid draws from a Fréchet distribution: $\exp \left\{-T_{j}^{s} z^{-\theta^{s}}\right\}$.

## Recap: Caliendo-Parro (2015)

General equilibrium model of cross-country production and trade with inter-sectoral linkages, that builds on the Eaton-Kortum machinery

## Setup:

- $i$ and $j$ denote countries; $i j$ subscript indicates a shipment from $i$ to $j$
- $r$ and $s$ denote industries; $r$ superscript indicates a shipment from $r$ to $s$

CES aggregator for $C_{j}^{s}$ and $\mathcal{M}_{j}^{\text {sr }}$ composites:

$$
\begin{equation*}
Q_{j}^{s}=\left(\int q_{j}^{s}\left(\omega^{s}\right)^{1-1 / \sigma^{s}} d \omega^{s}\right)^{\sigma^{s} /\left(\sigma^{s}-1\right)} \tag{19}
\end{equation*}
$$

Iceberg trade costs: $\tau_{i j}^{r} \geq 1$.

## Caliendo-Parro (2015): Equilibrium System

$$
\begin{align*}
& \pi_{i j}^{s}=\frac{T_{i}^{s}\left(c_{i}^{s} \tau_{j}^{s}-\theta^{-\theta^{s}}\right.}{\sum_{k=1}^{J} T_{k}^{s}\left(c_{k}^{s} \tau_{k j}^{s}\right)^{-\theta^{s}}}  \tag{20}\\
& c_{j}^{s}=\Upsilon_{j}^{s} w_{j}^{1-\sum_{r=1}^{s} \gamma_{j}^{s}} \prod_{r=1}^{s}\left(P_{j}^{f}\right)^{\gamma_{j}^{s}}  \tag{21}\\
& P_{j}^{r}=A^{r}\left[\sum_{i=1}^{J} T_{i}^{r}\left(c_{i}^{r} \tau_{i j}^{r}\right)^{-\theta^{r}}\right]^{-1 / \theta^{r}}  \tag{22}\\
& x_{j}^{s}=\sum_{r=1}^{s} \underbrace{\sum_{i=1}^{J} x_{i}^{r} \pi_{j i}^{r}}_{\gamma_{j}^{s_{j}^{r}}}+\alpha_{j}^{s}\left(w_{j} L_{j}+D_{j}\right)  \tag{23}\\
& \sum_{s=1}^{s} X_{j}^{s}=\sum_{s=1}^{s} \sum_{i=1}^{J} X_{j}^{s} \pi_{i j}^{s}=\sum_{s=1}^{s} \sum_{i=1}^{J} X_{i}^{s} \pi_{j i}^{s}+D_{j} \tag{24}
\end{align*}
$$

## Limitation

- Trade shares $\pi_{i j}^{s}$ do not differ by the identity of the purchaser, i.e., whether this is used to meet final demand or as an intermediate input.
- When mapping to the data:

$$
\begin{equation*}
\pi_{i j}^{r}=\frac{\tilde{F}_{i j}^{r}}{\sum_{k=1}^{J} \tilde{F}_{k j}^{r}}=\frac{\tilde{Z}_{i j}^{r s}}{\sum_{k=1}^{J} \tilde{Z}_{k j}^{r s}} \text { for } j=1, \ldots, J \tag{25}
\end{equation*}
$$

- Would not be satisfied for a generic WIOT
- Why this matters: As GVC measures are computed from final-use and intermediate-use shares, desirable to have a model that can match these shares exactly


## A More Flexible Model

Consider trade costs from country $i$ to $j$ in industry $r$ :

- Now allow these to differ by identity of the purchasing entity.
- If used as an input by another industry $s$ : $\tau_{i j}^{\text {rs }}$
- If used to meet final demand: $\tau_{i j}^{r F}$
- Implies that trade share expressions (and hence price indices) will depend on the identity of the purchaser.

New equilibrium system:

$$
\begin{align*}
\pi_{i j}^{r s} & =\frac{T_{i}^{r}\left(c_{i}^{r} \tau_{i j}^{r s}\right)^{-\theta^{r}}}{\sum_{k=1}^{J} T_{k}^{r}\left(c_{k}^{r} \tau_{k j}^{r s}\right)^{-\theta^{r}}}  \tag{26}\\
\pi_{i j}^{r F} & =\frac{T_{i}^{r}\left(c_{i}^{r} \tau_{i j}^{r F}\right)^{-\theta^{r}}}{\sum_{k=1}^{J} T_{k}^{r}\left(c_{k}^{r} \tau_{k j}^{r F}\right)^{-\theta^{r}}} \tag{27}
\end{align*}
$$

## A More Flexible Model

$$
\begin{gather*}
c_{j}^{s}=\Upsilon_{j}^{s} w_{j}^{1-\sum_{r=1}^{S} \gamma_{j}^{r s}} \prod_{r=1}^{s}\left(P_{j}^{r s}\right)^{\gamma_{j}^{r s}}  \tag{28}\\
P_{j}^{r s}=A^{r}\left[\sum_{i=1}^{J} T_{i}^{r}\left(c_{i}^{r} \tau_{i j}^{r s}\right)^{-\theta^{r}}\right]^{-1 / \theta^{r}}  \tag{29}\\
P_{j}^{r F}=A^{r}\left[\sum_{i=1}^{J} T_{i}^{r}\left(c_{i}^{r} \tau_{i j}^{r F}\right)^{-\theta^{r}}\right]^{-1 / \theta^{r}}  \tag{30}\\
P_{j}^{F}=\prod_{s=1}^{S}\left(P_{j}^{s F} / \alpha_{j}^{s}\right)^{\alpha_{j}^{s}}  \tag{31}\\
Y_{j}^{s}=\sum_{k=1}^{J} \pi_{j k}^{s F} \alpha_{k}^{s}\left(w_{k} L_{k}+D_{k}\right)+\sum_{r=1}^{S} \sum_{k=1}^{J} \pi_{j k}^{s r} \gamma_{k}^{s r} Y_{k}^{r}  \tag{32}\\
\sum_{i=1}^{S} \sum_{r=1}^{S} \sum_{s=1}^{s} \pi_{i j}^{s r} \gamma_{j}^{s r} Y_{j}^{r}+w_{j} L_{j}=\sum_{i=1}^{S} \sum_{r=1}^{S} \sum_{s=1}^{S} \pi_{j i}^{s r} \gamma_{i}^{s r} Y_{i}^{r}+\sum_{s=1}^{S} \sum_{i=1}^{s} \pi_{j i}^{s F} \alpha_{i}^{s}\left(w_{i} L_{i}+D_{i}\right) \tag{33}
\end{gather*}
$$

## Mapping to the WIOD

- Recover final expenditure share and input use share parameters in a standard way:

$$
\begin{gather*}
\gamma_{j}^{r s}=\frac{\sum_{i=1}^{J} \tilde{Z}_{i j}{ }^{s}}{\tilde{Y}_{j}^{s}}  \tag{34}\\
\alpha_{j}^{s}=\frac{\sum_{i=1}^{J} \tilde{F}_{j}^{s}}{\sum_{r=1}^{s} \widetilde{V A}_{j}^{\prime}+\tilde{D}_{j}} \tag{35}
\end{gather*}
$$

## Mapping to the WIOD

- Recover final expenditure share and input use share parameters in a standard way:

$$
\begin{gather*}
\gamma_{j}^{r s}=\frac{\sum_{i=1}^{J} \tilde{Z}_{i j}^{r s}}{\tilde{Y}_{j}^{s}}  \tag{34}\\
\alpha_{j}^{s}=\frac{\sum_{i=1}^{J} \tilde{F}_{i j}^{s}}{\sum_{r=1}^{S} \widetilde{V A}_{j}^{r}+\tilde{D}_{j}} \tag{35}
\end{gather*}
$$

- Theoretical result: Suppose that these and all other underlying model parameters - other than the trade costs - are given. Then, there exist a unique set of values of $\tau_{i j}^{r s}$ and $\tau_{i j}^{r F}$ that will exactly match the observed $\tilde{Z}_{i j}^{r s}$ 's and $\tilde{F}_{i j}^{s}$.
- Upshot: The more flexible model can now exactly match all entries of a WIOT.


## Counterfactual Changes via the "Hat Algebra"

- Caveat: While the set of $\tau_{i j}^{r s}$ 's and $\tau_{i j}^{r F}$ 's exist that fully match a WIOT, these are computationally not easy to back out.
- Instead: Turn to "hat-algebra" techniques.

Re-express the equilibrium system of equations in changes, following Dekle et al. (2008) and Caliendo and Parro (2015).

- Denote change in variable $X$ by $X^{\prime}$; and percentage changes by $\hat{X}=X^{\prime} / X$.
- To evaluate counterfactual changes, need only:
(i) the initial trade shares, $\pi_{i j}^{r s}$ and $\pi_{i j}^{r F}$;
(ii) the demand and technological Cobb-Douglas parameters $\gamma_{j}^{\text {rs }}$ and $\alpha_{j}^{s}$;
(iii) a vector of $\theta^{r}$ 's.


## Counterfactual Changes via the "Hat Algebra"

$$
\begin{gather*}
\hat{\pi}_{i j}^{r s}=\left(\frac{\hat{c}_{i}^{r} \hat{T}_{i j}^{r s}}{\hat{P}_{j}^{r s}}\right)^{-\theta^{r}}  \tag{36}\\
\hat{\pi}_{i j}^{r F}=\left(\frac{\hat{c}_{r}^{r} \hat{T}_{i j}^{r f}}{\hat{P}_{j}^{r F}}\right)^{-\theta^{r}}  \tag{37}\\
\hat{c}_{j}^{s}=\left(\hat{w}_{j}\right)^{1-\sum_{r=1}^{s} \gamma_{j}^{r s}} \prod_{r=1}^{s}\left(\hat{P}_{j}^{r s}\right)^{\gamma_{j}^{r s}}  \tag{38}\\
\hat{P}_{j}^{r s}=\left[\sum_{i=1}^{J} \pi_{i j}^{r s}\left(\hat{c}_{i}^{r} r_{i j}^{r s}\right)^{-\theta^{r}}\right]^{-1 / \theta^{r}}  \tag{39}\\
\hat{P}_{j}^{r F}=\left[\sum_{i=1}^{J} \pi_{i j}^{r f}\left(\hat{c}_{i}^{r} \hat{\tau}_{i j}^{r F}\right)^{-\theta^{r}}\right]^{-1 / \theta^{r}} \tag{40}
\end{gather*}
$$

## Counterfactual Changes via the "Hat Algebra"

$$
\begin{align*}
&\left(Y_{j}^{s}\right)^{\prime}=\sum_{k=1}^{J}\left(\pi_{j k}^{s F}\right)^{\prime}\left(\alpha_{k}^{s}\right)^{\prime}\left(\hat{w}_{k} w_{k} L_{k}+D_{k}\right)+\sum_{r=1}^{S} \sum_{k=1}^{J}\left(\pi_{j k}^{s r}\right)^{\prime} \gamma_{k}^{s r}\left(Y_{k}^{r}\right)^{\prime}  \tag{41}\\
& \sum_{i=1}^{J} \sum_{r=1}^{S} \sum_{s=1}^{S}\left(\pi_{i j}^{s r}\right)^{\prime} \gamma_{j}^{s r}\left(Y_{j}^{r}\right)^{\prime}+\hat{w}_{j} w_{j} L_{j}= \sum_{i=1}^{J} \sum_{r=1}^{S} \sum_{s=1}^{S}\left(\pi_{j i}^{s r}\right)^{\prime} \gamma_{i}^{s r}\left(Y_{i}^{r}\right)^{\prime}  \tag{42}\\
&+\sum_{s=1}^{S} \sum_{i=1}^{J}\left(\pi_{j i}^{s F}\right)^{\prime}\left(\alpha_{i}^{s}\right)^{\prime}\left(\hat{w}_{i} w_{i} L_{i}+D_{i}\right)
\end{align*}
$$

## Counterfactuals

## Two exercises

1. Initialize to 1995 and - holding deficits constant - evaluate whether changes in the $\tau$ 's and/or changes in the $\alpha$ 's can explain observed evolution of GVC measures
2. Initialize to 2011 - holding deficits constant - explore how changes in the $\tau$ 's and/or changes in the $\alpha$ 's are projected to affect the future movements in country GVC positioning

Note: Not meant to be a definitive decomposition.

- Put aside changes in the $T$ 's, since harder to discipline this empirically
- Also: "hat algebra" in the current Cobb-Douglas framework not equipped to handle changes in $\gamma$ 's.


## 1. Changes from 1995 to 2011

- Consider $\hat{\tau}_{i j}^{r s}$ 's and $\hat{\tau}_{i j}^{r F}$ 's from 1995-2011 (from Head-Reis, for goods vs services).
- Consider actual changes in the final-use shares for the $\alpha$ 's.
- Set: $\theta=5$.

| A: Country-level GVC measures | Mean FIGO | Mean VAIGO | Correlation F/GO, VA/GO | Mean U | Mean D | Correlation U, D | Real wage change (Min, Mean, Max) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1995 baseline (from data) | 0.507 | 0.503 | 0.825 | 1.976 | 1.987 | 0.868 | --- |
| 2011 baseline (from data) | 0.484 | 0.487 | 0.925 | 2.085 | 2.070 | 0.912 | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | 0.518 | 0.502 | 0.612 | 1.940 | 1.984 | 0.666 | (1.003, 1.104, 1.512) |
| Change expenditure shares | 0.516 | 0.513 | 0.857 | 1.945 | 1.953 | 0.889 | (0.993, 1.001, 1.017) |
| Both changes | 0.525 | 0.511 | 0.660 | 1.917 | 1.952 | 0.705 | (1.002, 1.093, 1.434) |
| B: Country-industry GVC measures | $\begin{aligned} & \text { Regress } \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}} \text { on } \mathrm{VA} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}^{5}}{ }^{\mathbf{5}} \\ & \text { (Coefficient on VA/GO} \mathrm{j}_{\mathrm{j}, \mathrm{t}}{ }^{5} \text {. } \end{aligned}$ |  |  | Regress $\mathrm{U}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ <br> (Coefficient on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ ) |  |  |  |
| 1995 baseline (from data) | $0.5434^{* * *}$ | $0.5184^{* *}$ | 0.0851 | $0.5337^{* * *}$ | 0.4839** | $0.2564^{* * *}$ | --- |
| 2011 baseline (from data) | $0.6543^{* * *}$ | $0.6373^{* * *}$ | $0.2647^{* * *}$ | $0.6286^{* * *}$ | $0.5785^{* *}$ | 0.4156 *** | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | $0.5534 * * *$ | $0.5321^{* * *}$ | 0.1101* | $0.5270^{* * *}$ | $0.4844^{* *}$ | $0.2474^{* * *}$ | --- |
| Change expenditure shares | $0.5942^{* * *}$ | 0.5760 *** | 0.1029* | $0.5930 * * *$ | $0.5540^{* *}$ | $0.2753^{* * *}$ | --- |
| Both changes | $0.6009^{* * *}$ | $0.5854^{* * *}$ | $0.1193^{* *}$ | $0.5856^{* * *}$ | $0.5512^{* * *}$ | $0.2609^{* * *}$ | --- |
| Country FE? | N | Y | Y | N | Y | Y | --- |
| Industry FE? | N | N | Y | N | N | Y | --- |

## 1. Changes from 1995 to 2011

- Observed trade costs tend to weaken the key cross-country correlation between $F / G O$ and VA/GO (as well as that between $U$ and $D$ )
- Conversely, rise in importance of services (relative to goods) moves these correlations in the opposite direction

| A: Country-level GVC measures | Mean FIGO | Mean VAIGO | $\begin{aligned} & \text { Correlation } \\ & \text { F/GO, VA/GO } \end{aligned}$ | Mean U | $\begin{gathered} \text { Mean } \\ \text { D } \end{gathered}$ | Correlation U, D | Real wage change (Min, Mean, Max) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1995 baseline (from data) | 0.507 | 0.503 | 0.825 | 1.976 | 1.987 | 0.868 | --- |
| 2011 baseline (from data) | 0.484 | 0.487 | 0.925 | 2.085 | 2.070 | 0.912 | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | 0.518 | 0.502 | 0.612 | 1.940 | 1.984 | 0.666 | (1.003, 1.104, 1.512) |
| Change expenditure shares | 0.516 | 0.513 | 0.857 | 1.945 | 1.953 | 0.889 | (0.993, 1.001, 1.017) |
| Both changes | 0.525 | 0.511 | 0.660 | 1.917 | 1.952 | 0.705 | (1.002, 1.093, 1.434) |
| B: Country-industry GVC measures | Regress $\mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ on VA/GO $\mathrm{j}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}}$ <br> (Coefficient on VA/GO $\mathrm{j}, \mathrm{t}^{5}$ ) |  |  | Regress $\mathrm{U}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ <br> (Coefficient on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ ) |  |  |  |
| 1995 baseline (from data) | $0.5434^{\star * *}$ | $0.5184^{* *}$ | 0.0851 | $0.5337^{* * *}$ | $0.4839^{* *}$ | $0.2564^{* * *}$ | --- |
| 2011 baseline (from data) | $0.6543^{* * *}$ | $0.6373^{* * *}$ | $0.2647^{* * *}$ | $0.6286 * * *$ | $0.5785^{* * *}$ | $0.4156 * * *$ | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | $0.5534^{* * *}$ | $0.5321^{* * *}$ | 0.1101* | $0.5270^{* * *}$ | $0.4844^{* *}$ | $0.2474^{* * *}$ | --- |
| Change expenditure shares | $0.5942^{* * *}$ | $0.5760 * * *$ | 0.1029* | $0.5930^{* * *}$ | 0.5540 *** | $0.2753^{* * *}$ | --- |
| Both changes | $0.6009^{* * *}$ | $0.5854^{* * *}$ | $0.1193 * *$ | $0.5856^{* * *}$ | $0.5512^{* * *}$ | $0.2609 * * *$ | --- |
| Country FE? | N | Y | Y | N | Y | Y | --- |
| Industry FE? | N | N | Y | N | N | Y | --- |

## 1. Changes from 1995 to 2011

- Lower panel: These two forces go some way towards accounting for the rise in the slope-coefficient between the country-industry GVC measures

| A: Country-level GVC measures | Mean FIGO | Mean VAIGO | Correlation F/GO, VA/GO | $\begin{gathered} \text { Mean } \\ \mathbf{U} \end{gathered}$ | Mean D | Correlation U, D | Real wage change (Min, Mean, Max) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1995 baseline (from data) | 0.507 | 0.503 | 0.825 | 1.976 | 1.987 | 0.868 | --- |
| 2011 baseline (from data) | 0.484 | 0.487 | 0.925 | 2.085 | 2.070 | 0.912 | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | 0.518 | 0.502 | 0.612 | 1.940 | 1.984 | 0.666 | $(1.003,1.104,1.512)$ |
| Change expenditure shares | 0.516 | 0.513 | 0.857 | 1.945 | 1.953 | 0.889 | (0.993, 1.001, 1.017) |
| Both changes | 0.525 | 0.511 | 0.660 | 1.917 | 1.952 | 0.705 | (1.002, 1.093, 1.434) |
| B: Country-industry GVC measures | $\begin{aligned} & \text { Regress } \mathrm{F} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}}{ }^{\mathrm{s}} \text { on } \mathrm{VA} / \mathrm{GO}_{\mathrm{j}, \mathrm{t}^{5}}{ }^{\mathbf{5}} \\ & \text { (Coefficient on VA/GO} \mathrm{j}_{\mathrm{j}, \mathrm{t}}{ }^{5} \text {. } \end{aligned}$ |  |  | Regress $\mathrm{U}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ <br> (Coefficient on $\mathrm{D}_{\mathrm{j}, \mathrm{t}}{ }^{5}$ ) |  |  |  |
| 1995 baseline (from data) | $0.5434^{* * *}$ | $0.5184^{* *}$ | 0.0851 | $0.5337^{* * *}$ | $0.4839^{* *}$ | $0.2564^{* * *}$ | --- |
| 2011 baseline (from data) | $0.6543^{* * *}$ | $0.6373^{* * *}$ | $0.2647^{* * *}$ | $0.6286^{* * *}$ | 0.5785*** | 0.4156 *** | --- |
| 1995 to 2011 Shifts |  |  |  |  |  |  |  |
| Change trade costs | $0.5534 * * *$ | $0.5321^{* * *}$ | 0.1101* | $0.5270^{* * *}$ | $0.4844^{* *}$ | $0.2474^{* * *}$ | --- |
| Change expenditure shares | $0.5942^{* * *}$ | 0.5760 *** | 0.1029* | $0.5930 * * *$ | $0.5540^{* * *}$ | $0.2753^{* * *}$ | --- |
| Both changes | $0.6009^{* * *}$ | $0.5854^{* * *}$ | $0.1193^{* *}$ | $0.5856^{* * *}$ | $0.5512^{* * *}$ | $0.2609^{* * *}$ | --- |
| Country FE? | N | Y | Y | N | Y | Y | --- |
| Industry FE? | N | N | Y | N | N | Y | --- |

## 2. Forward Projections

- Consider a further decline in trade costs and/or the $\alpha$ 's for another 16 years, based on per annum rate of change from earlier regression estimates
- Interestingly: a decline in trade costs that is biased towards services appears to induce greater specialization in services for countries with pre-existing comparative advantage...
and this actually strengthens the correlation between $F / G O$ and $V A / G O$ (and between $U$ and $D$ )

| Country-level measures | Mean <br> F/GO | Mean <br> VA/GO | Correlation <br> F/GO, VA/GO | Mean <br> U | Mean <br> D | Correlation <br> U, D |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Real wage change |  |  |  |  |  |  |
| (Min, Mean, Max) |  |  |  |  |  |  |

## 2. Forward Projections

Changes in individual countries' GVC positioning ( $U$ and $D$ ) from a further trade cost decline:



## Concluding Remarks

## Conclusion

- Documented the evolution of GVC positioning of countries and industries, in the 1995-2011 WIOD
- Uncovered several salient facts and puzzling correlations:
- Countries (and country-industries) that are far removed from final demand also have a high production-staging distance from primary factors
- Explored the possible role of two forces: (i) declines in trade costs; and (ii) the rising importance of services in final consumption shares.
- Done through the lens of a model (extending Caliendo-Parro), that fully rationalizes all the entries of a WIOT, and thus provides a more flexible basis for counterfactual exercise on countries' GVC positioning.


## Supplementary Slides

## Summary Statistics

|  | 10th | Median | 90th | Mean | Std Dev | N |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| F/GO |  |  |  |  |  |  |
| All industries |  |  |  |  |  |  |
| Goods industries only | 0.125 | 0.444 | 0.901 | 0.473 | 0.271 | 24,076 |
| Service industries only | 0.076 | 0.373 | 0.700 | 0.379 | 0.240 | 11,105 |
|  |  | 0.496 | 0.956 | 0.553 | 0.270 | 12,971 |
| VA/GO |  |  |  |  |  |  |
| All industries | 0.279 | 0.456 | 0.738 | 0.489 | 0.186 | 24,395 |
| Goods industries only | 0.247 | 0.360 | 0.499 | 0.371 | 0.118 | 11,152 |
| Service industries only | 0.378 | 0.575 | 0.812 | 0.589 | 0.175 | 13,243 |
|  |  |  |  |  |  |  |
| $\underline{\text { U }}$ |  |  |  |  |  |  |
| All industries | 1.153 | 2.126 | 2.914 | 2.098 | 0.649 | 24,395 |
| Goods industries only | 1.523 | 2.298 | 3.048 | 2.291 | 0.605 | 11,152 |
| Service industries only | 1.055 | 1.982 | 2.771 | 1.936 | 0.640 | 13,243 |
|  |  |  |  |  |  |  |
| D |  |  |  |  |  |  |
| All industries | 1.502 | 2.141 | 2.624 | 2.092 | 0.450 | 24,395 |
| Goods industries only | 2.033 | 2.381 | 2.728 | 2.376 | 0.316 | 11,152 |
| Service industries only | 1.356 | 1.846 | 2.363 | 1.852 | 0.404 | 13,243 |

