## The Size-Power Tradeoff in HAR Inference: Supplement

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This supplement provides additional figures and Monte Carlo results.

Figures S.1 plots the implied mean kernel for the Fourier, cosine, Legendre, and SS basis functions for B = 8 and T = 200. The Fourier transforms of these implied mean kernels, that is, the frequency-domain implied mean kernel, are plotted in Figure S.2 at the frequencies  $2\pi j/T$ , j = 1, ..., 32. The EWP (Fourier) estimator is the only one of these four that has an exact kernel representation, and its frequency-domain kernel is the familiar flat (Daniell) kernel that gives equal weight to the first B/2 periodogram ordinates. The remaining three implied mean kernels in the frequency domain also concentrate their mass at low frequencies.

Figure S.3 shows the power difference, as a function of the standardized local alternative  $\delta$ , between the EWP and QS test, for B = 8 for EWP and b for QS chosen so that the two tests have the same size-adjusted power. This curve is computed using the expression in Theorem 3 and Remark 6.

Figure S.4 shows additional Monte Carlo results for different values of *T* for 6 tests: QS, EWP, Cos (type II cosine basis function), NW, Legendre basis function, and SS.

Figure S.5 shows the spectral density for the AMA(2,1) process. The parameters are calibrated so that  $\omega^{(2)} = 4$  and with a spectral density approximately symmetric around  $\pi/2$ , with a minimum at  $\pi/2$  (the coefficients are  $\rho_1 = 0.048$ ,  $\rho_2 = 0.248$ ,  $\theta = -0.064$ ).

Figure S.6 shows results for the ARMA(2,1) disturbances, m = 1.

Figures S.7 and S.8 show additional results for m = 2.

Figure S.9 shows results in the location model, feasible higher-order corrected critical values, ARMA(2,1) errors.

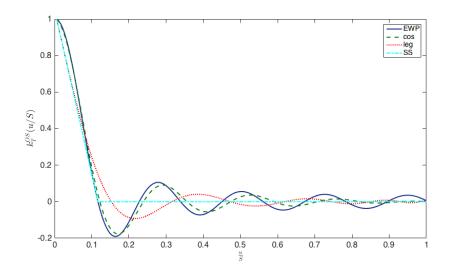


Figure S.1. Implied mean kernel of basis function estimators with B = 8, time domain: Fourier/EWP (dark blue, solid), cosine (light blue, dash), Legendre (red, dot), and split-sample (teal, dash-dot).

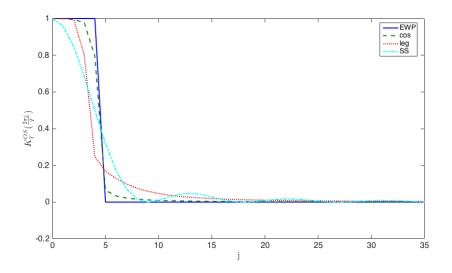


Figure S.2. Implied mean kernel of basis function estimators with B = 8, frequency domain: Fourier/EWP (dark blue, solid), cosine (light blue, dash), Legendre (red, dot), and split-sample (teal, dash-dot). The frequency domain kernel is normalized to 1 at  $\omega = 0$  and computed over the periodogram ordinates (so the horizontal axis value j corresponds to  $2\pi j/T$ , etc.)

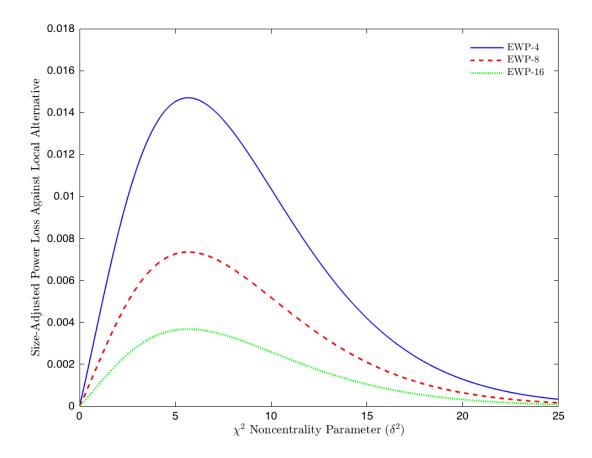


Figure S.3. Small-*b* approximation to power loss for EWP test, compared to QS test, for different values of *B* in the EWP test and with *b* for the QS test chosen so that the EWP and QS test have the same higher-order size when evaluated using fixed-*b* critical values. The figure plots the final expression in (45) as a function of  $\delta$ . Gaussian location model, *m*=1, 5% significance level.

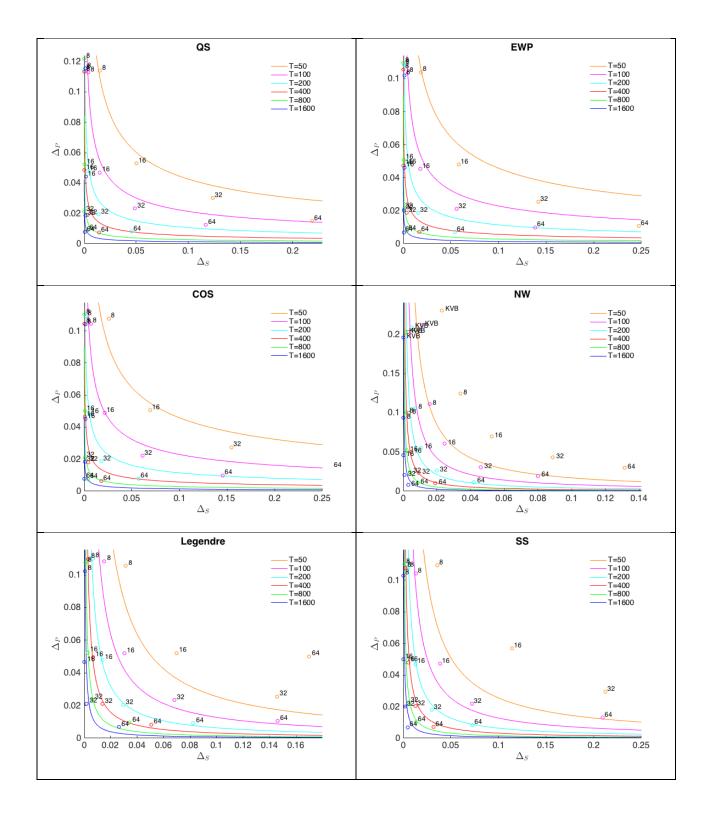


Figure S.4. Location model, AR(1), m = 1,  $\rho = 0.5$ Theoretical size distortion/power loss trade-off curves for each estimator with Monte Carlo results for *T* ranging from 50 to 1600.

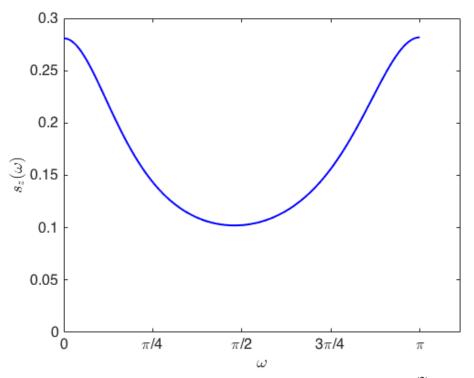


Figure S.5. Spectral density of calibrated ARMA(2,1),  $\omega^{(2)} = 4$ 

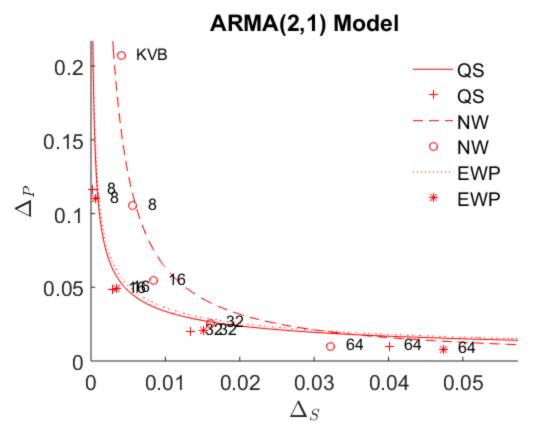


Figure S.6. Location model, ARMA(2,1), m = 1, T = 200Theoretical size distortion/power loss trade-off curves for QS, Newey-West, and EWP estimators with Monte Carlo results. ARMA(2,1) parameters fixed such that  $\omega^{(2)} = 4$ , equivalent to AR(1) with  $\alpha = 0.5$  (parameter values as in Figure S.5)

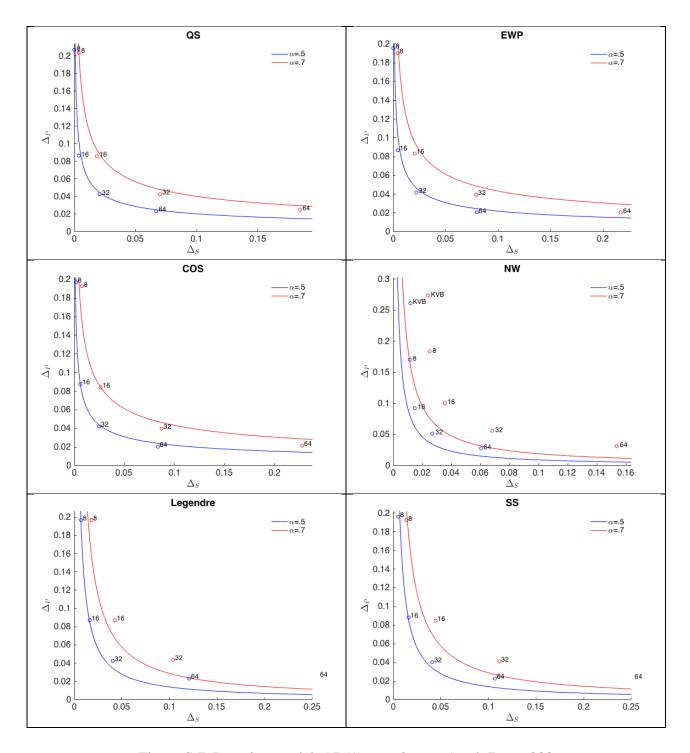


Figure S.7. Location model, AR(1), m = 2,  $\rho = .5$  and .7, T = 200Theoretical size distortion/power loss trade-off curves for each estimator and Monte Carlo results (dots)

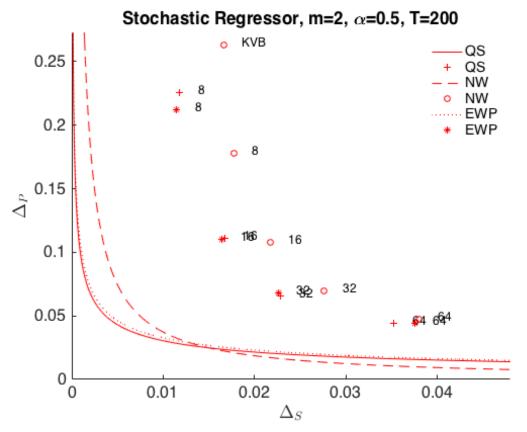


Figure S.8. Stochastic regressor, AR(1), m = 2,  $\rho = 0.5$ , T = 200Theoretical size distortion/power loss trade-off curves for QS, Newey-West, and EWP estimators with Monte Carlo results. *Note*: curves are for the Gaussian location model.

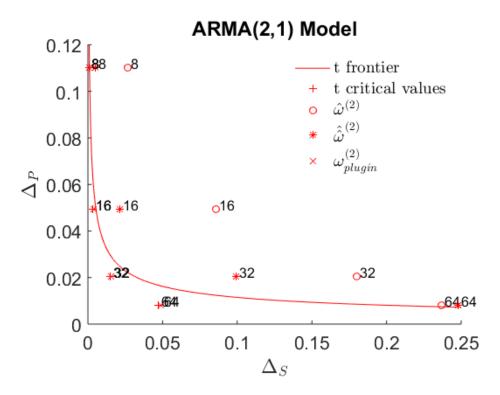


Figure S.9. Theoretical (lines) and Monte Carlo (symbols) size distortion/power loss curves for the EWP estimator using feasible higher-order adjusted critical values: Location model, m = 1, ARMA(2,1), parameter values as in Figure S.5, T = 200.