

Electric field dependence of the effective dielectric constant in graphene materials



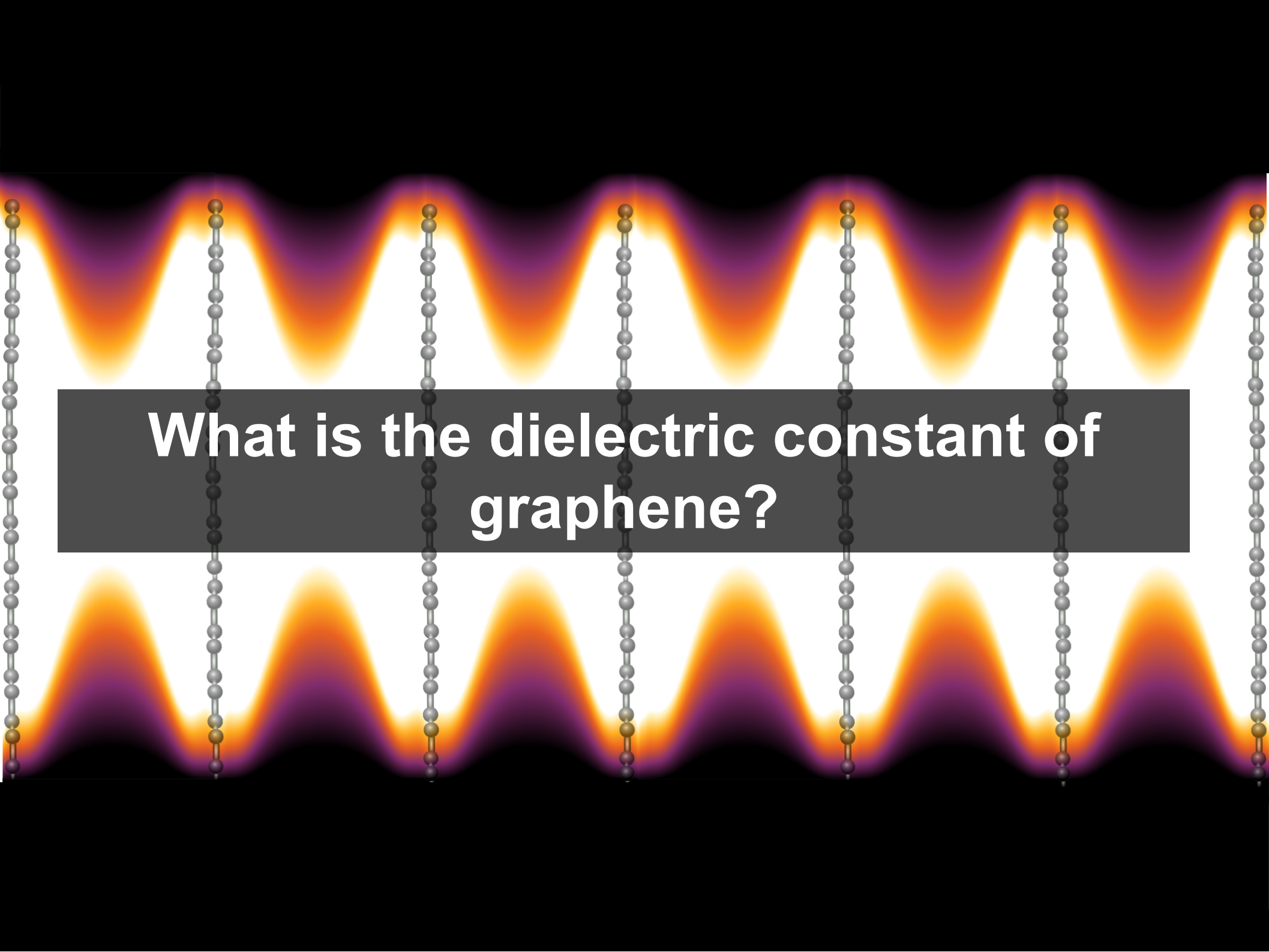
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Harvard University**

APS March Meeting 2013, March 20th 2013

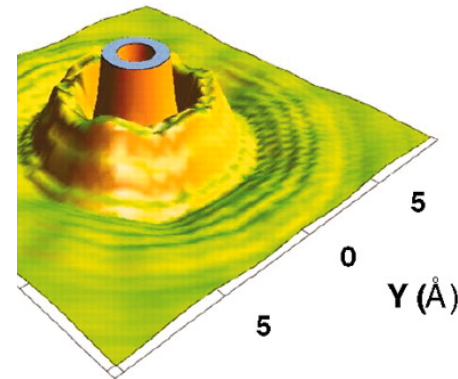


The background of the slide features a stylized representation of a graphene lattice, shown as a series of vertical chains of grey spheres. Overlaid on this lattice is a wavy, undulating pattern in shades of orange, yellow, and purple, which likely represents an electric field or a potential landscape. A dark grey rectangular box is centered horizontally across the middle of the image.

**What is the dielectric constant of
graphene?**

Debate in the literature

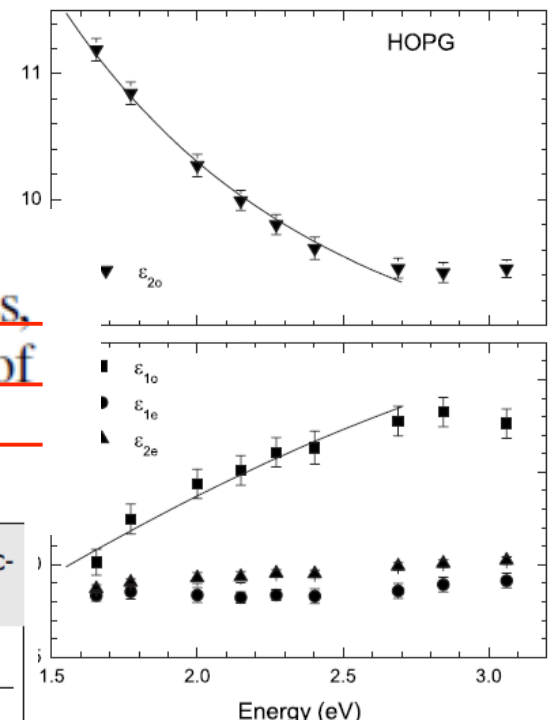
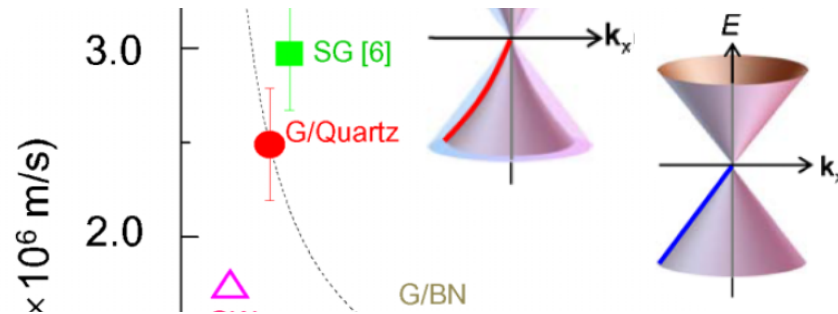
self-consistently, also within the random phase approximation. The value of ϵ_G has recently become a subject of considerable debate^{23–27}. Our data clearly show no anomalous screening, contrary to the recent report²⁷ that suggested $\epsilon_G \approx 15$, but in good agreement with measurements reported in ref. 28.



Reed et al. *Science* (2010) **330**, 805



Elias et al. *Nat. Physics*, (2011) **7**, 70



This value is of the same order of magnitude as previous studies, although the real dielectric constant of graphite is a source of controversy with measured values ranging from 2 to 13 (29).



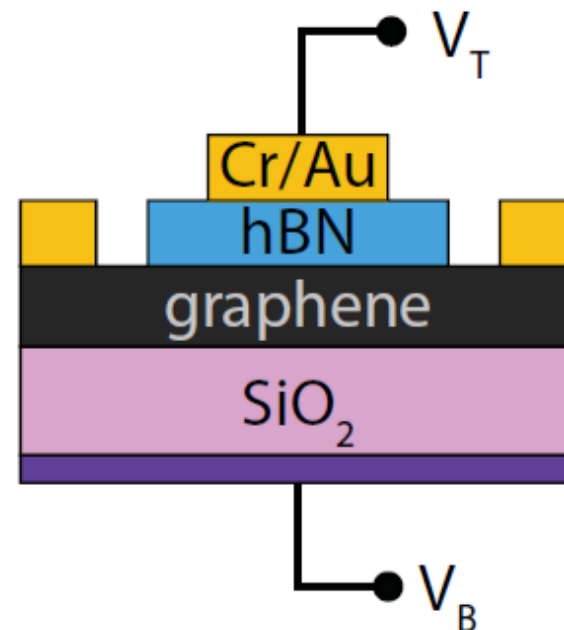
High-resolution angle-resolve photoemission spectroscopy
 $\epsilon \sim 7.0$

| Table 1 Fermi velocity (v_F), dielectric constant (ϵ), and fine structure constant (α) of graphene on each substrate | | | |
|--|-----------------------|-----------------|----------|
| Substrate | $v_F \times 10^6$ m/s | ϵ | α |
| Metals (LDA) | 0.85 | ∞ | - |
| SiC(000-1) | 1.15 ± 0.02 | 7.26 ± 0.02 | 0.35 |
| h-BN | 1.49 ± 0.08 | 4.22 ± 0.01 | 0.61 |
| Quartz | 2.49 ± 0.30 | 1.80 ± 0.02 | 1.43 |

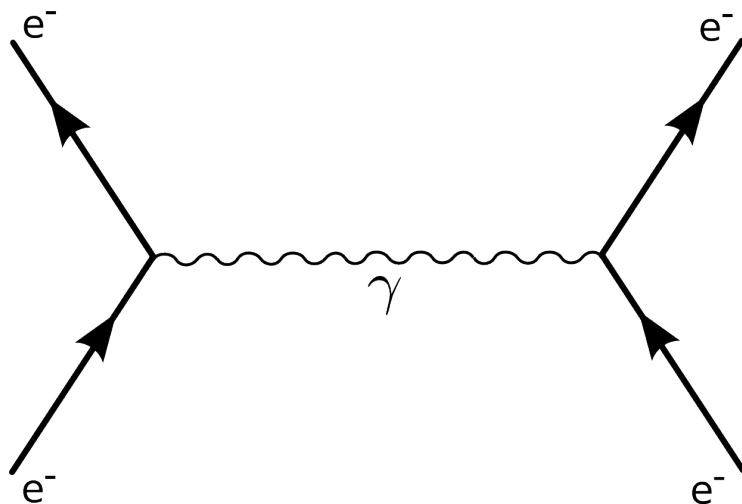
liposometric measurements
 $\epsilon \sim 2 - 13$

Dielectric constant is a fundamental quantity

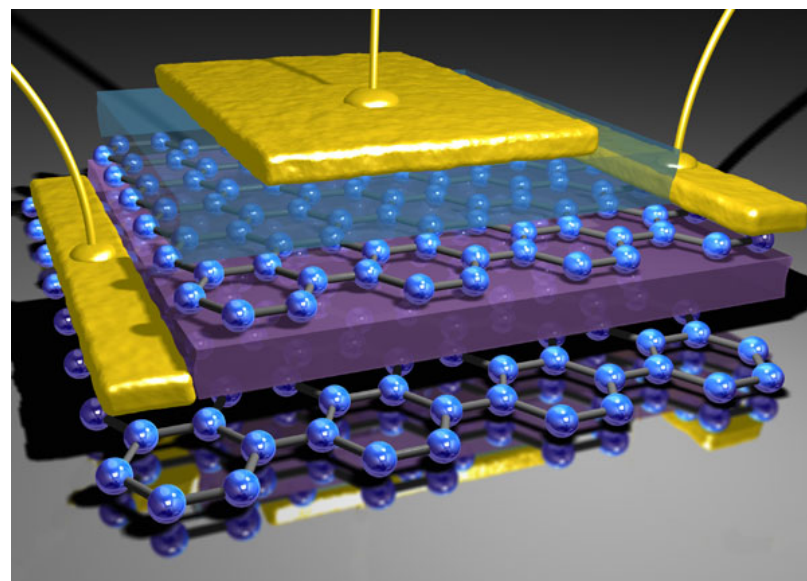
Capacitance, screening, electrical displacement, polarization, compressibility, etc.



A. F. Young et al. *PRB* (2012), **85**, 235458



Electron-electron interactions

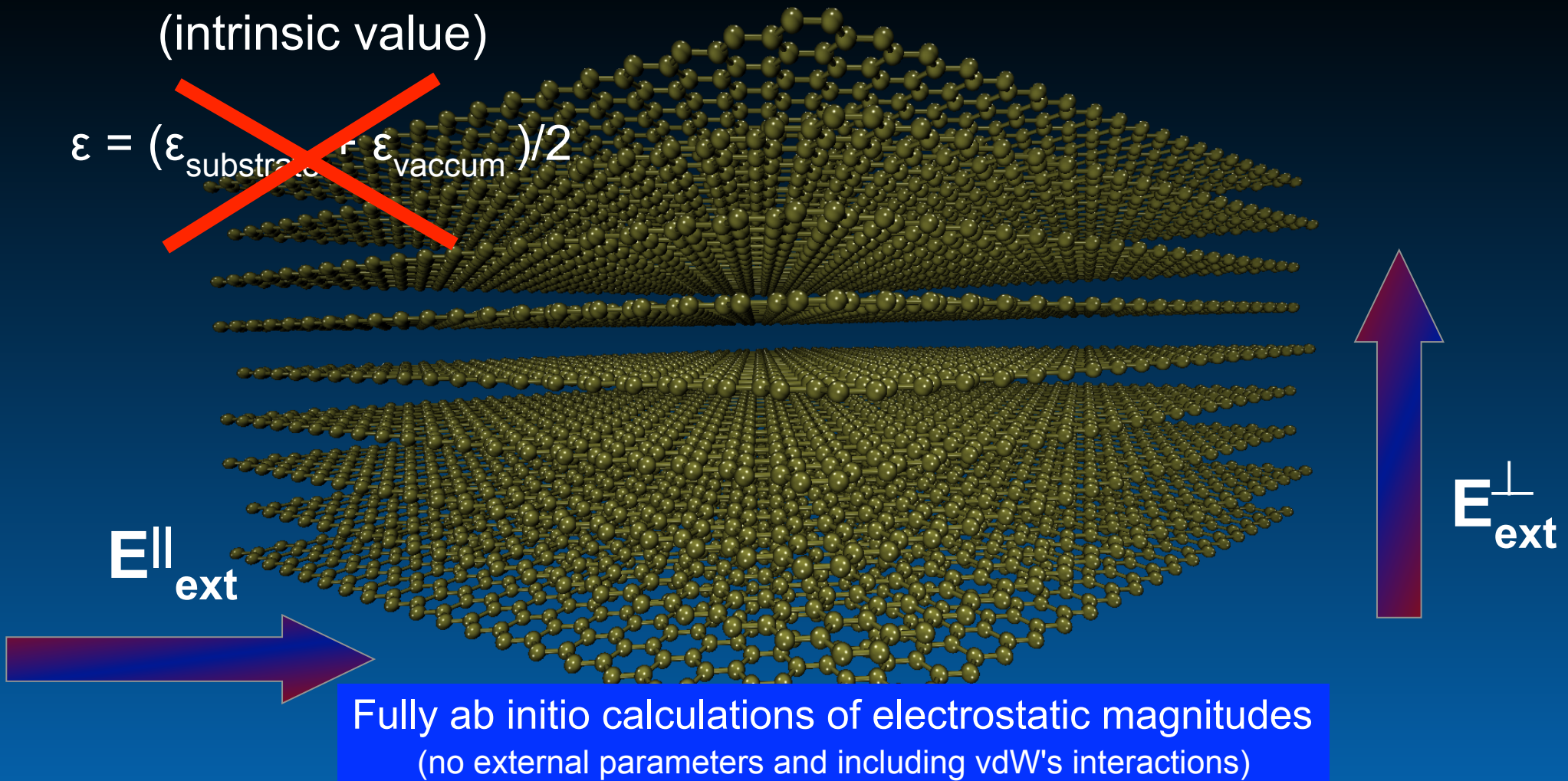


L. Britnell et al. *Science* (2012) **335**, 947

Our approach: capacitor model

No substrate
(intrinsic value)

~~$$\epsilon = (\epsilon_{\text{substrate}} + \epsilon_{\text{vacuum}})/2$$~~



Dielectric constant, $\epsilon(\mathbf{k}, \omega)$



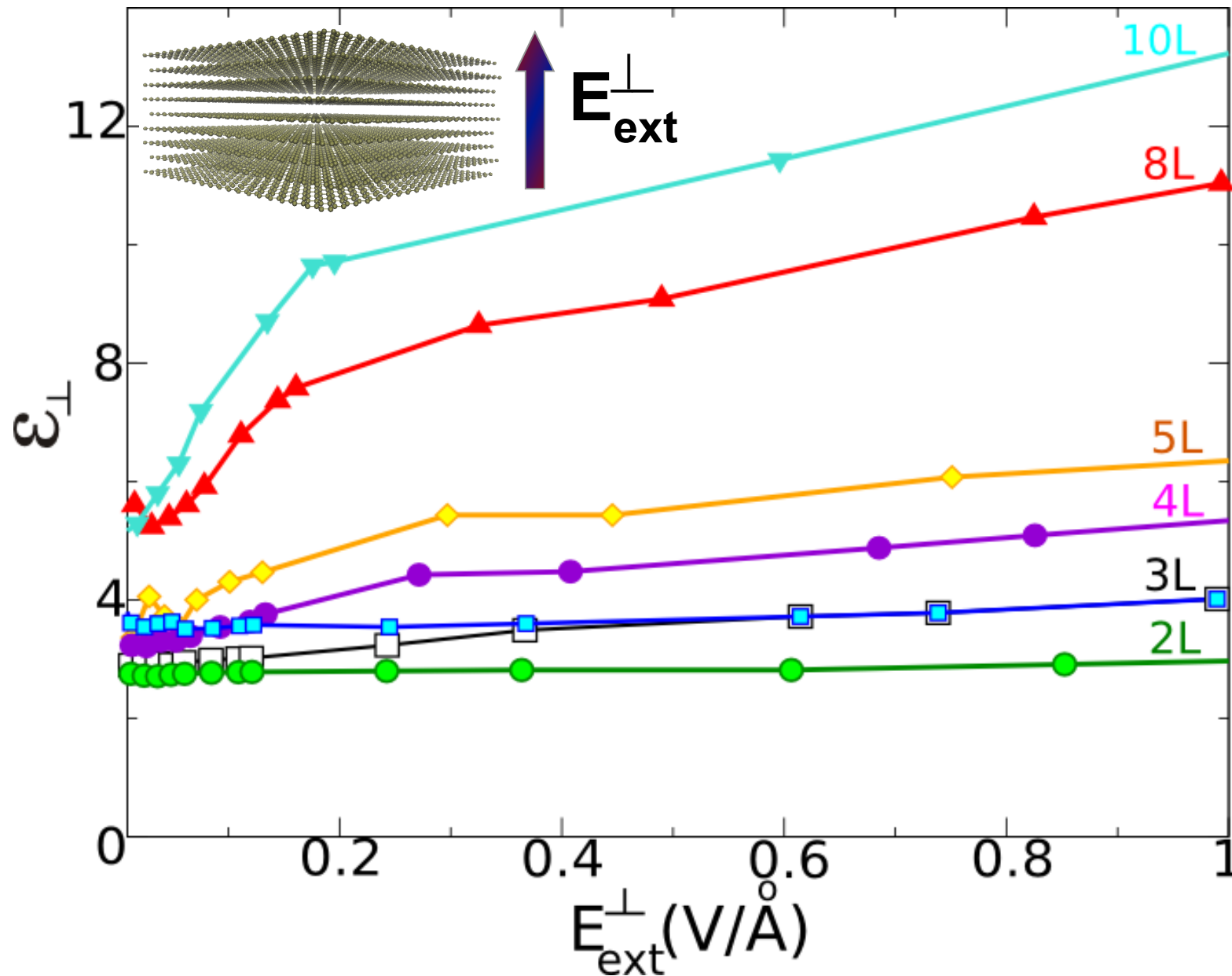
Effective dielectric constant, ϵ_G

Fine-structure constant, $\alpha(\mathbf{k}, \omega)$



Effective fine-structure constant,
 $\alpha_G = U/K = e^2/\epsilon_G \hbar v_F \sim 2.2/\epsilon_G$

Graphene dielectric constant is electric field dependent

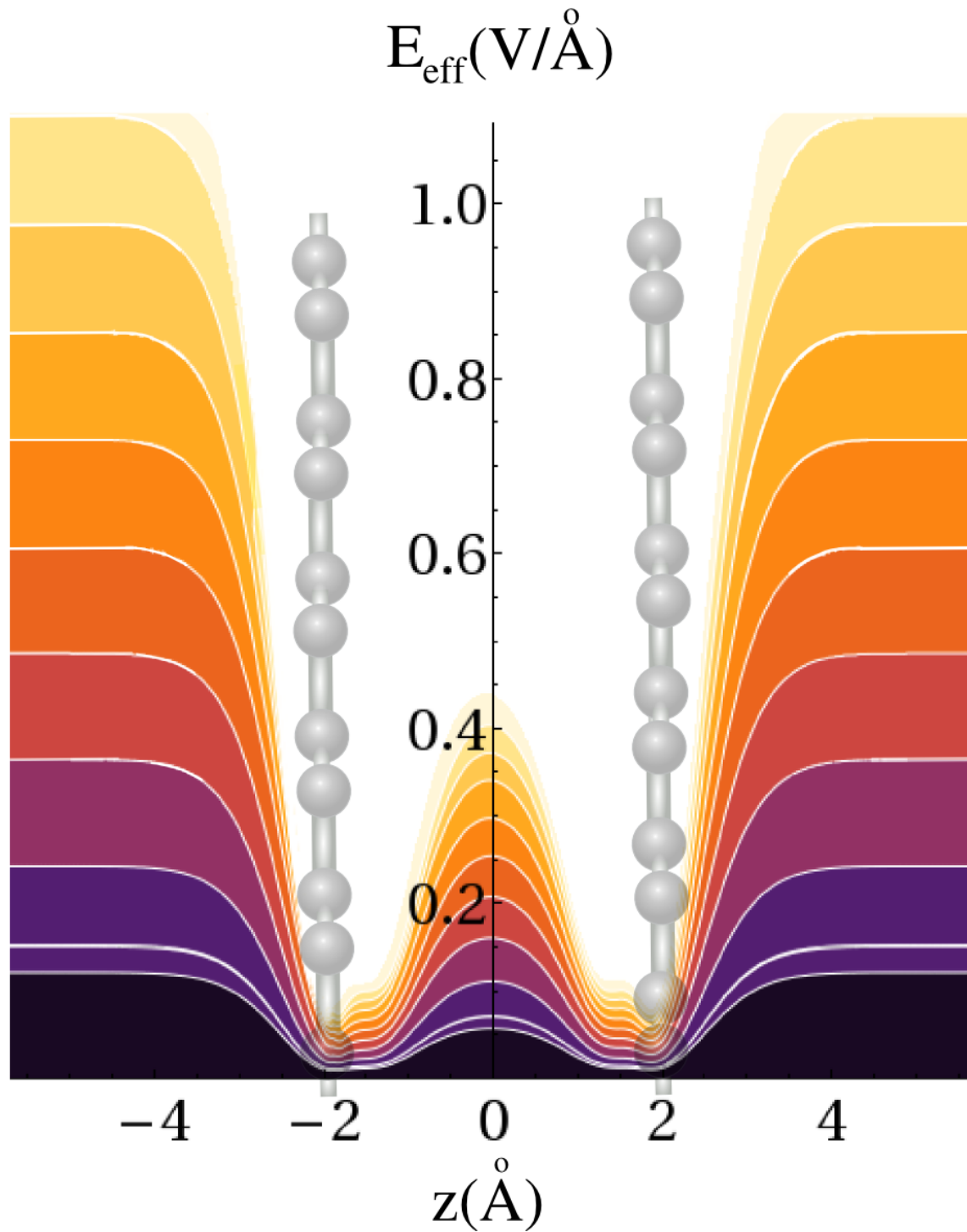


The thicker the structure (more layers) the stronger is the modulation

Modifications even at low fields < 0.10 V/Å.

Implications on other quantities, e.g. fine-structure constant $\alpha \sim 2.2/\epsilon_G$

Interlayer electric field is not constant

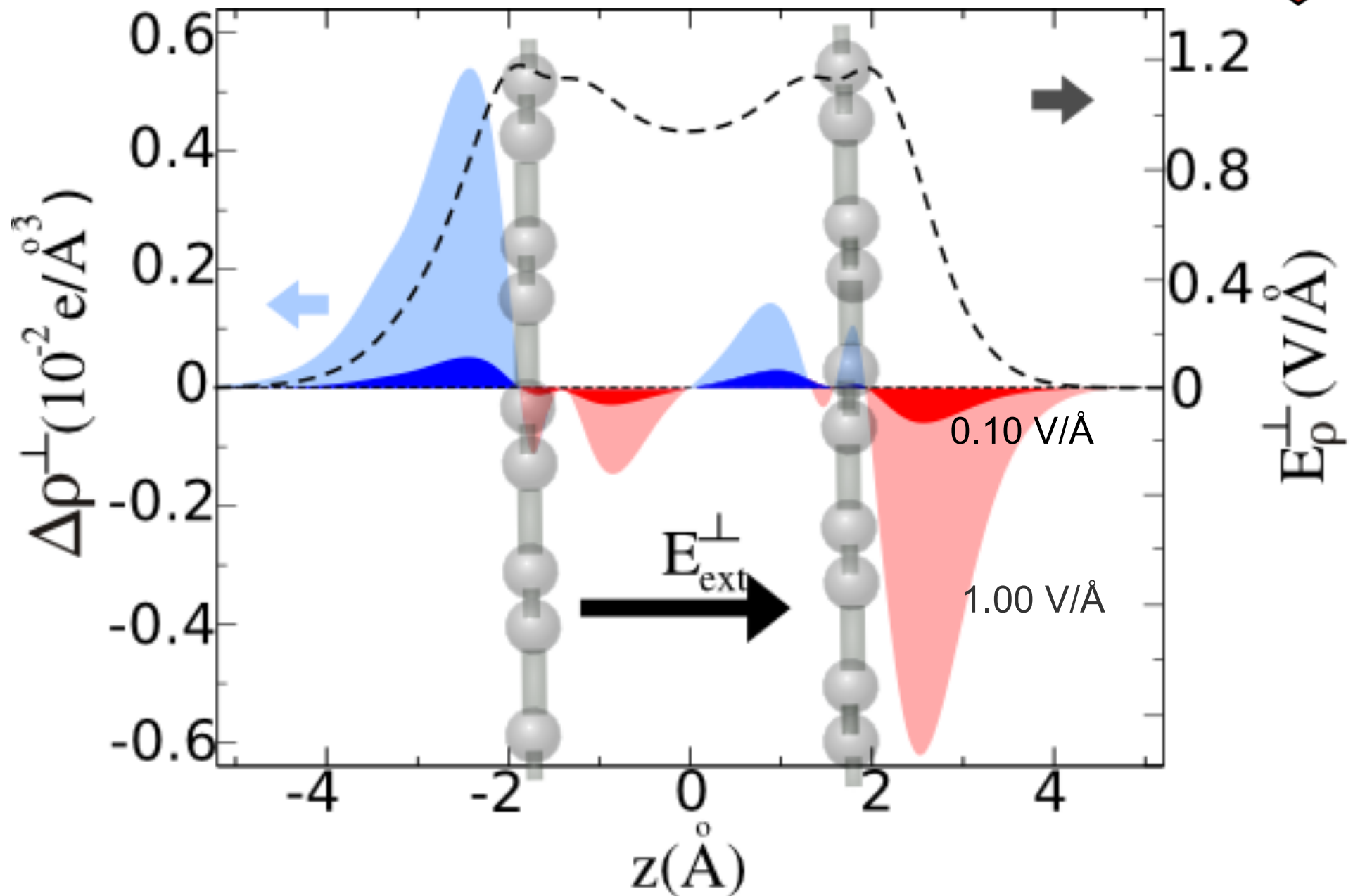


Position-dependent
interlayer electric field
(maximum and
minimal values)

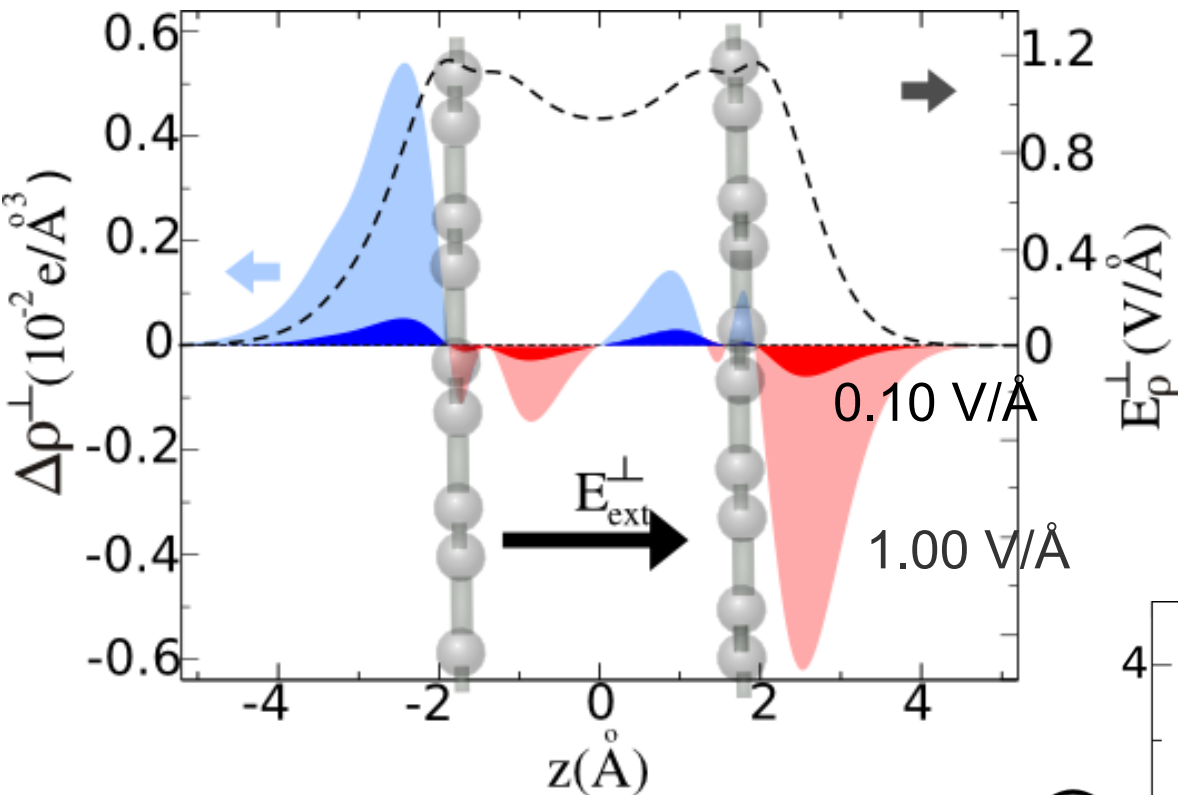
Screening is
not perfect: not a metal,
not a semiconductor

Also apply for
multilayer graphene

Polarization charge is field dependent



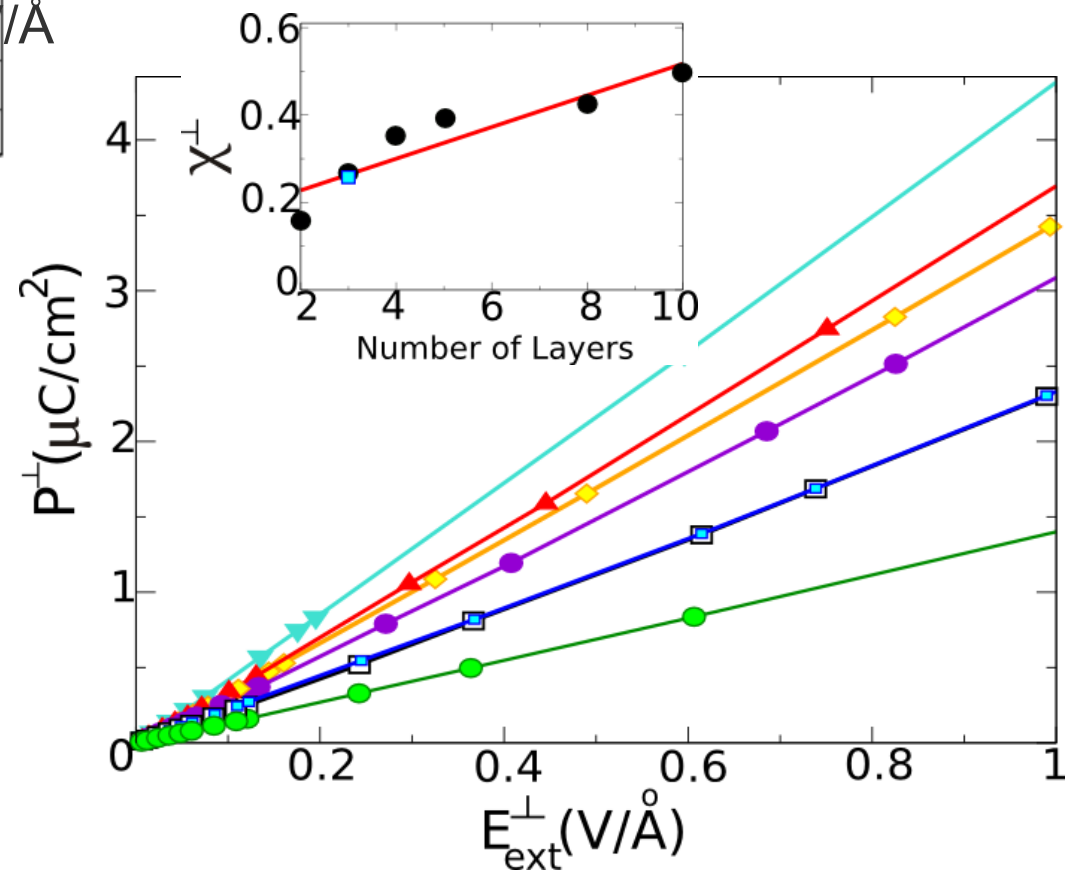
Polarization charge is field dependent



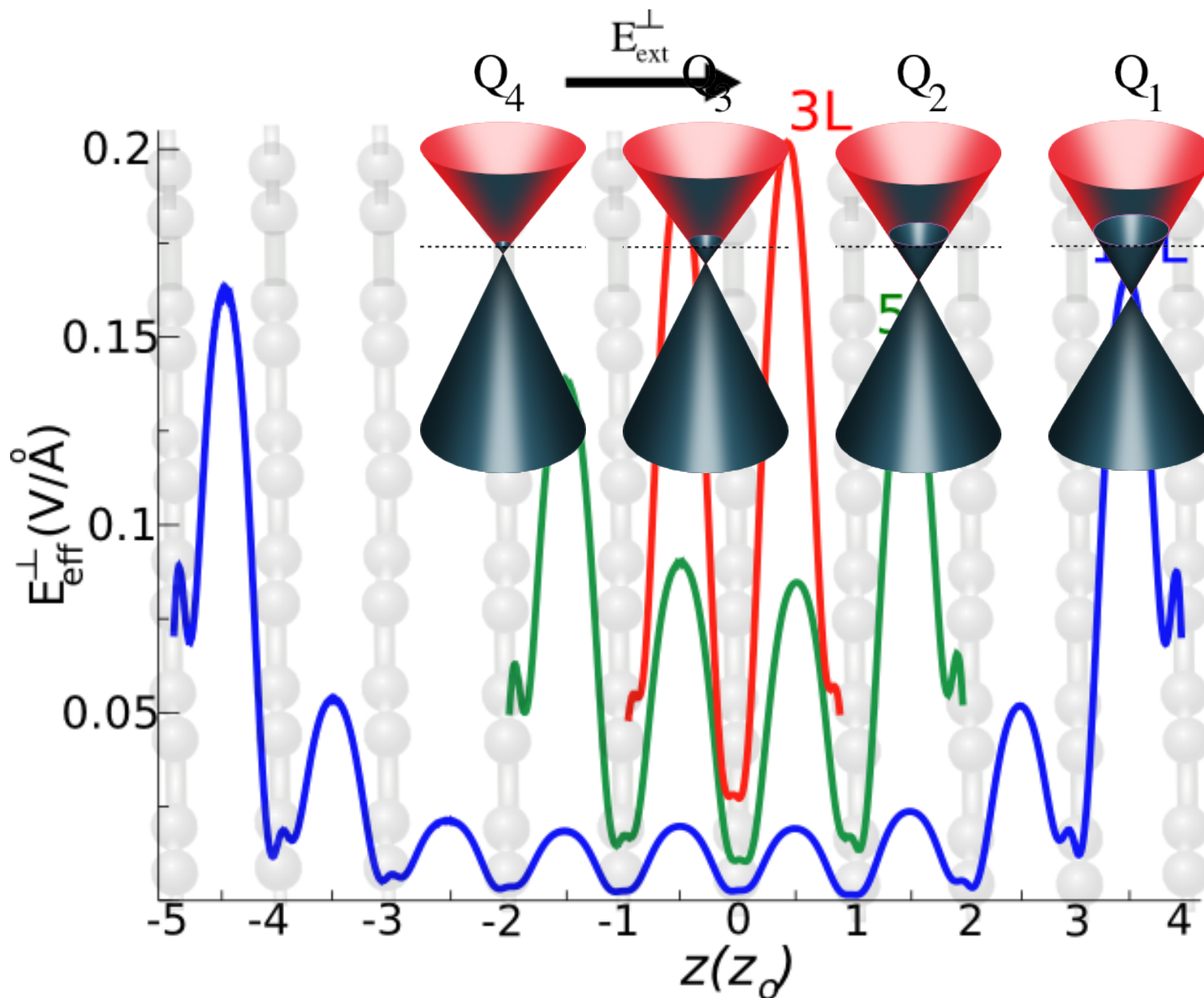
Charge accumulation/depletion at graphene layer generates the response field.

The response electric field E_{ρ} screens the external field E_{ext} as in:

$$E_{\text{tot}} = E_{\text{ext}} - E_{\rho}$$



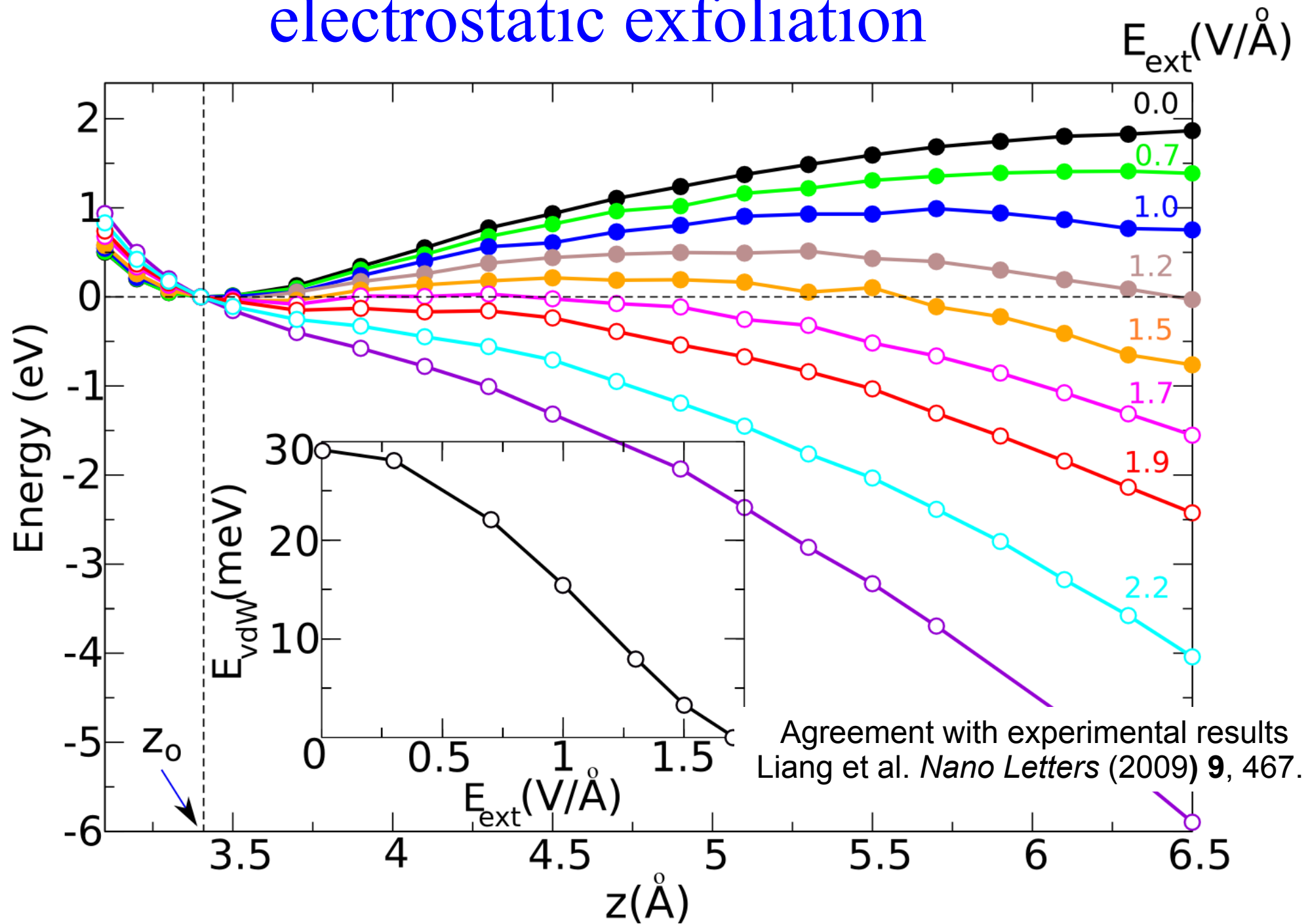
Non-linear screening is the main effect behind of electric-driven tuning of ϵ



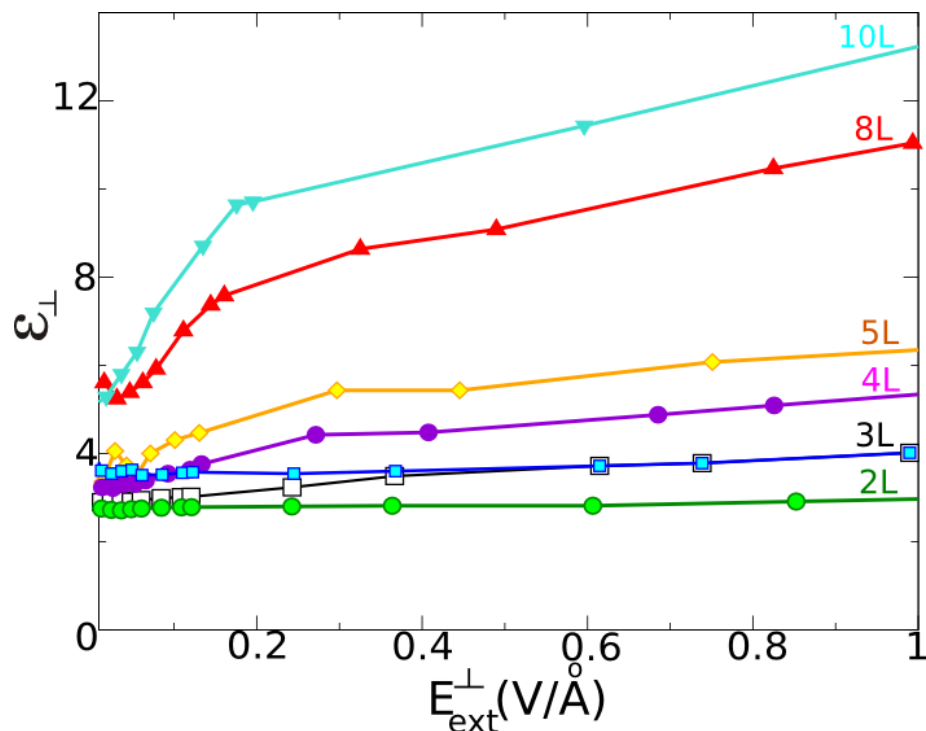
A thicker structure screens with shorter screening length than a thinner structure

The electric field is screened by the charge Q_i accumulated at each layer.

Limits on the applied electric field: electrostatic exfoliation



Messages to take home



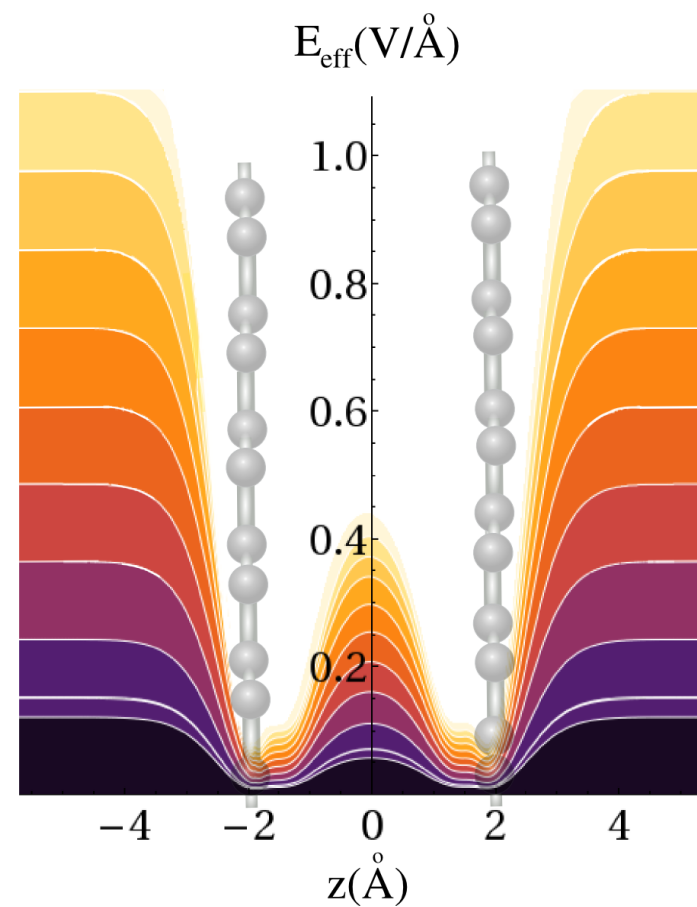
The dielectric constant of graphene is electric-field dependent

The thicker the structure (more layers) the stronger is the modulation

The non-linear screening effect is the main reason behind of the electric tuning

Electrostatic exfoliation is also possible using a bias

Other 2D-crystals, e.g, MoS_2 , also show similar behavior

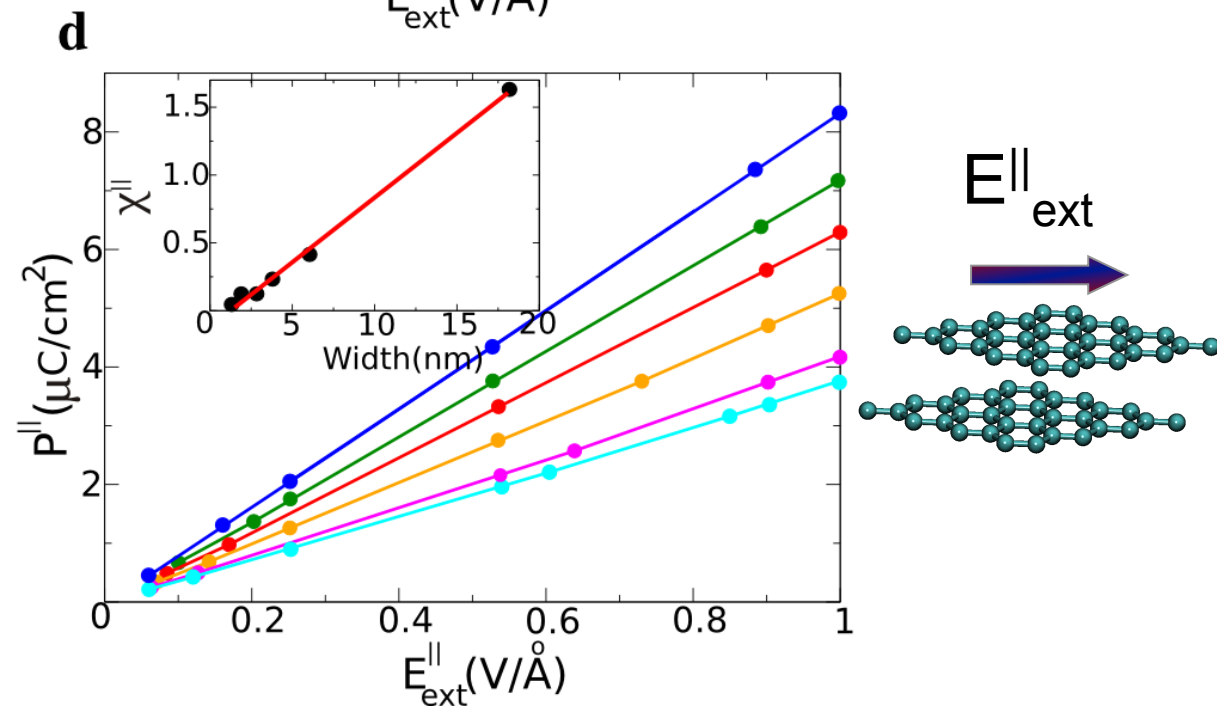
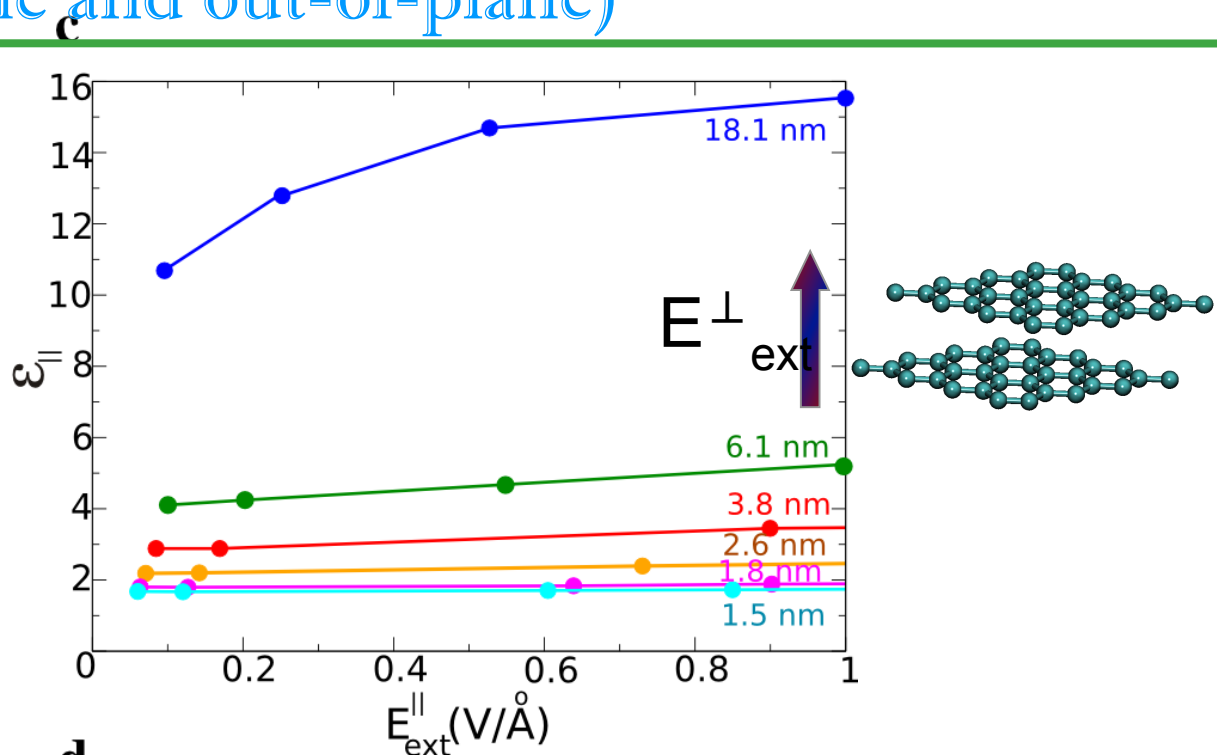
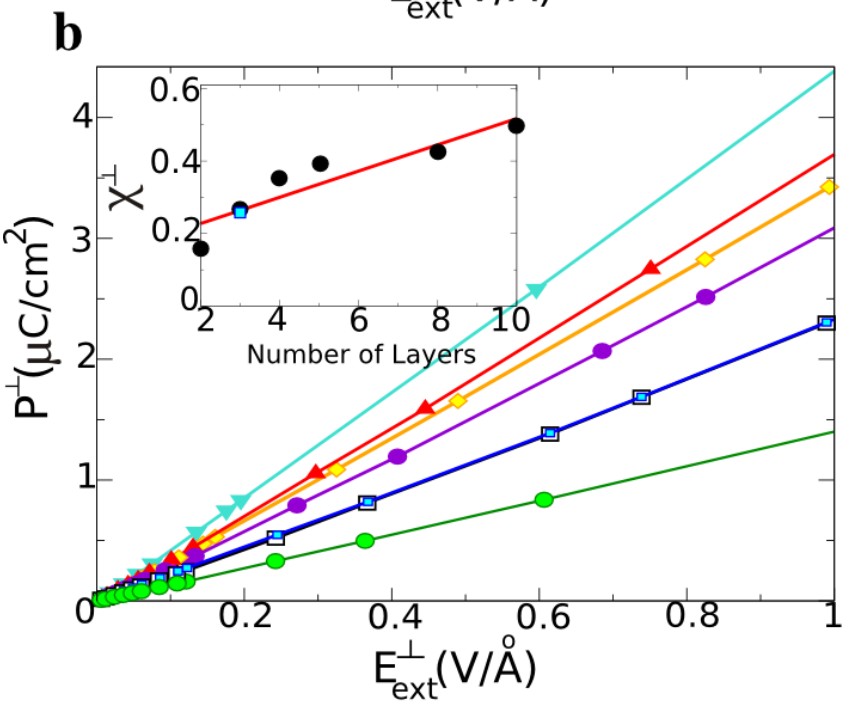
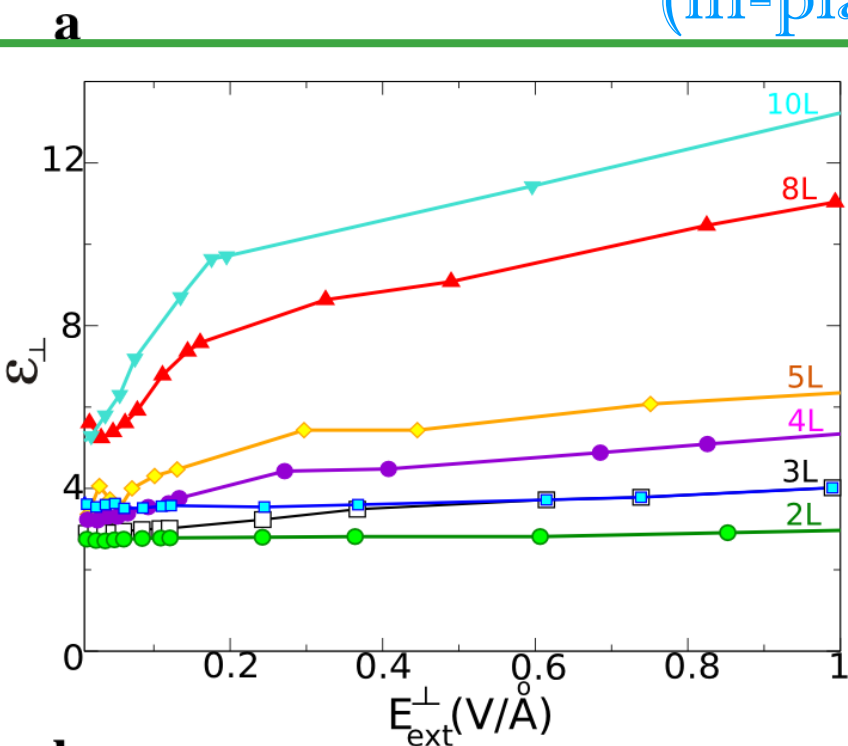




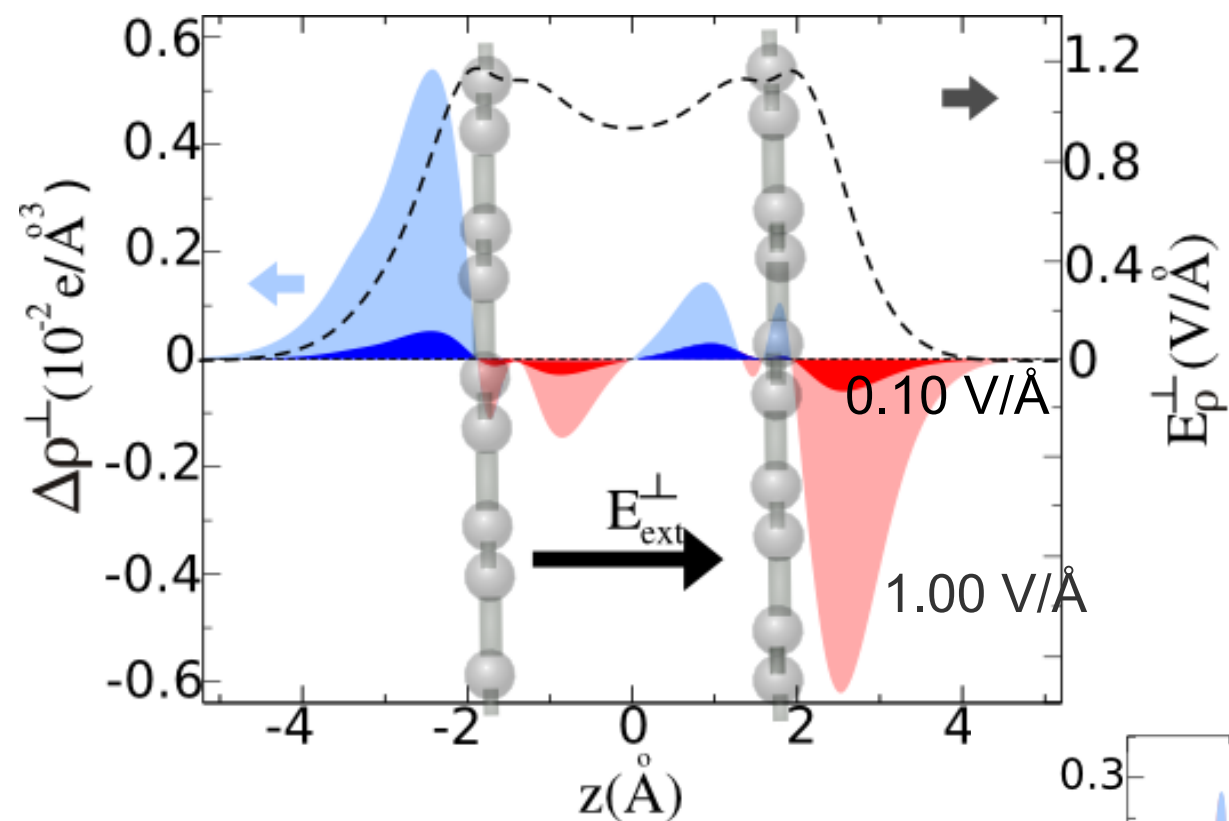
Thank you for your attention!

Acknowledgements: Xsede, supported by NSF grant numbers
TG-DMR120073, TG-DMR120049 and TG-PHY120021

Electric Field Dependence of the Effective Dielectric Constant (in-plane and out-of-plane)



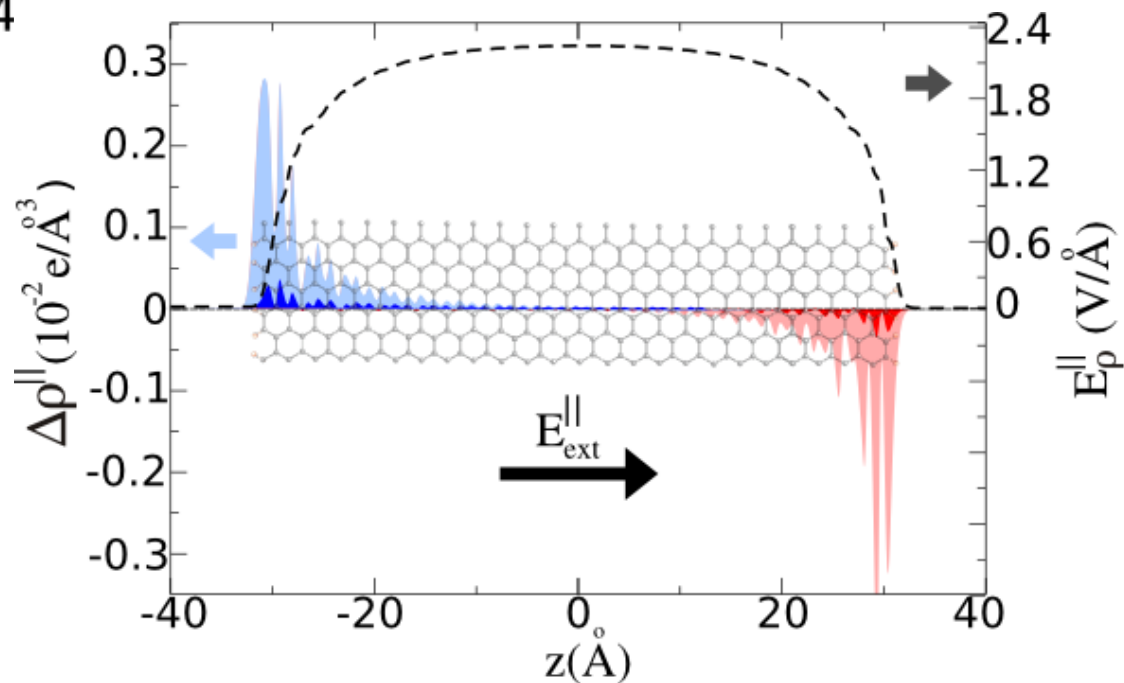
Polarization charge is field dependent



Charge accumulation/depletion at graphene layer generates the response field.

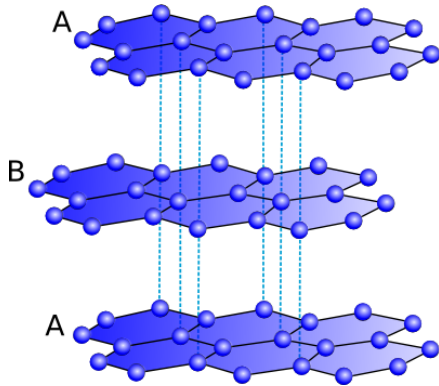
The response electric field E_ρ screens the external field E_{ext} as in:

$$E_{\text{tot}} = E_{\text{ext}} - E_\rho$$



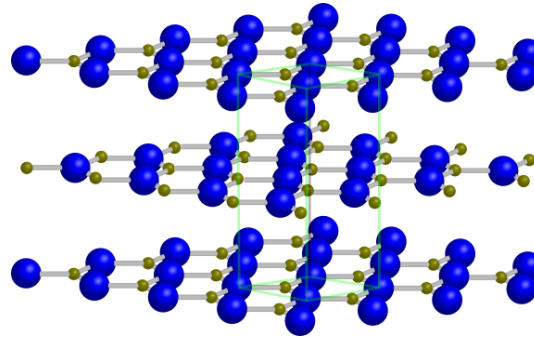
What about other 2D-materials?

Graphene



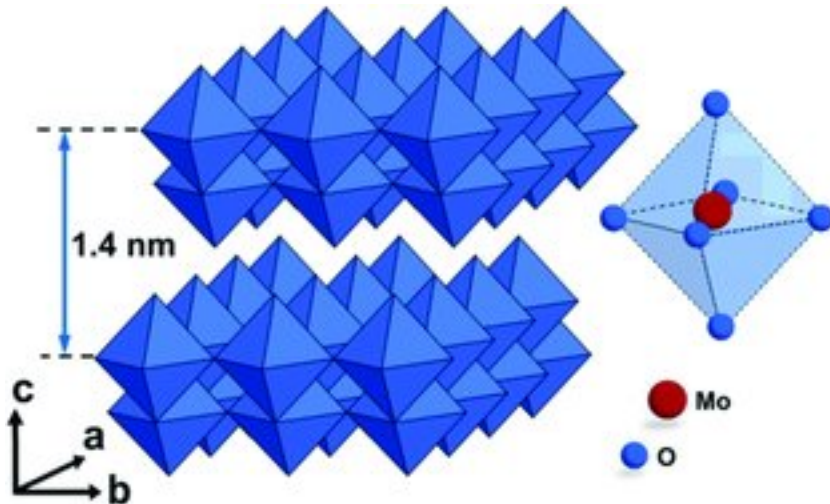
Novoselov et al. *Nature* (2005) **438**, 197.
Zhang et al. *Nature* (2005) **438**, 201.

h-BN



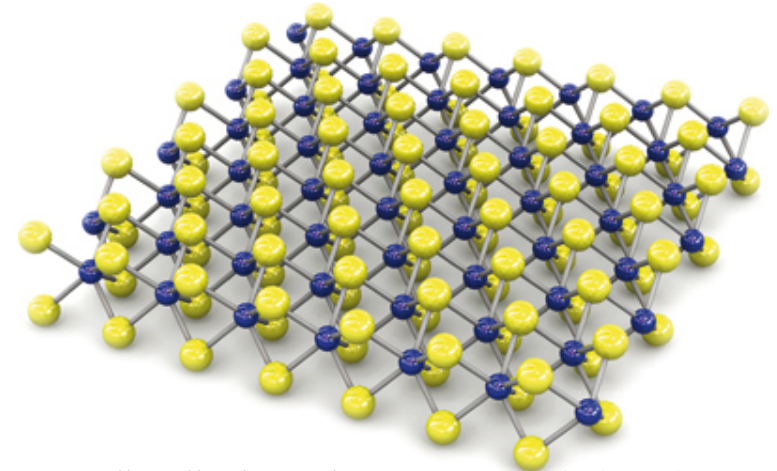
Dean et al. *Nat. Nanotech.* (2010) **5**, 722

α -MoO₃



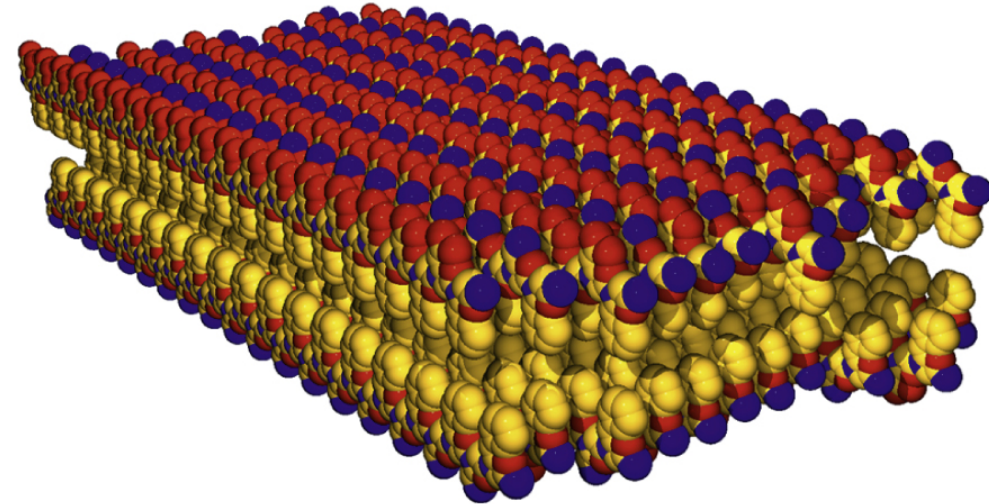
Balendhran et al. *Adv. Materials* (2013) **25**, 108

Metal dichalcogenide (WS₂, TiS₂, ZrS₂, MoSe₂, MoS₂, ...)



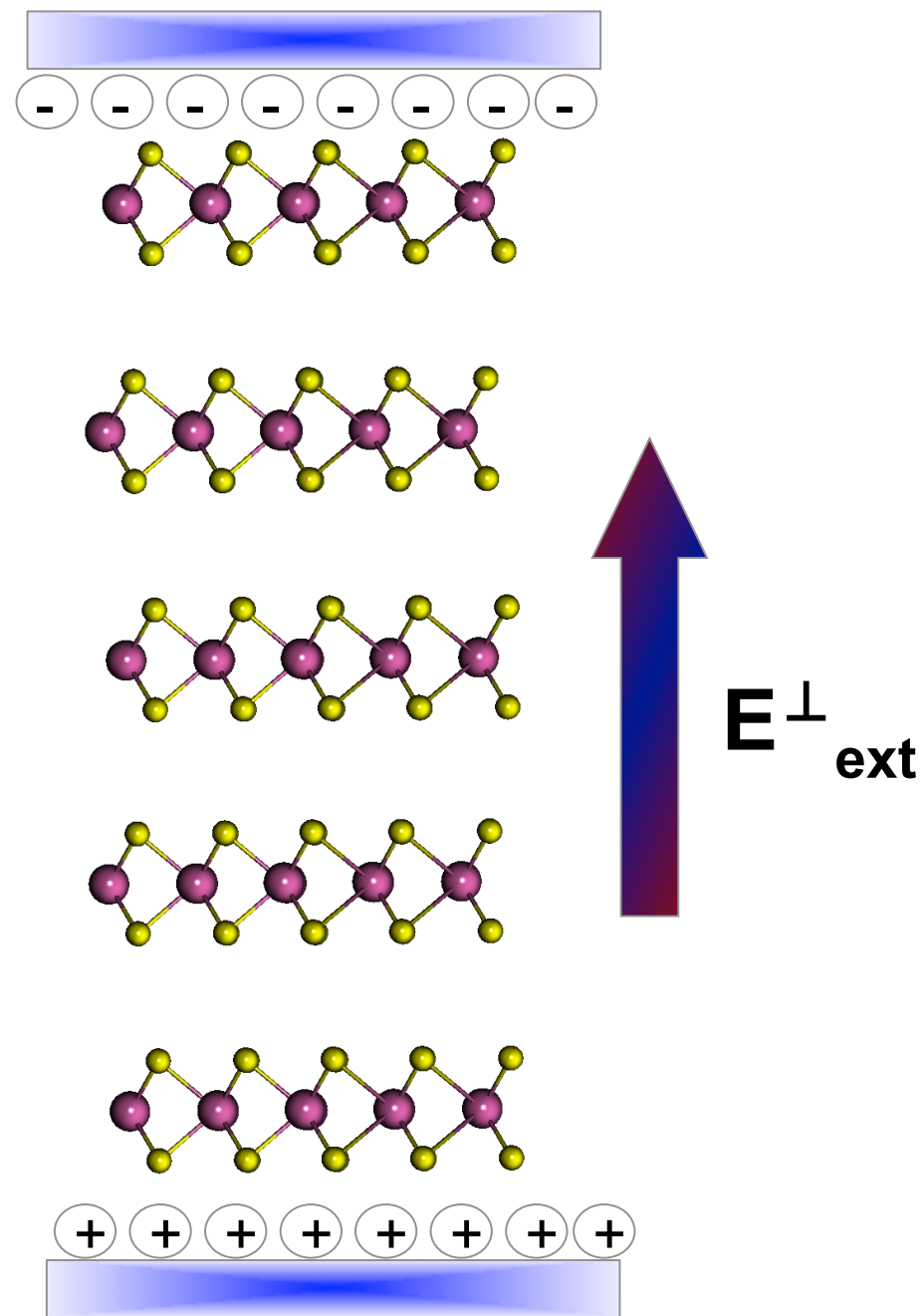
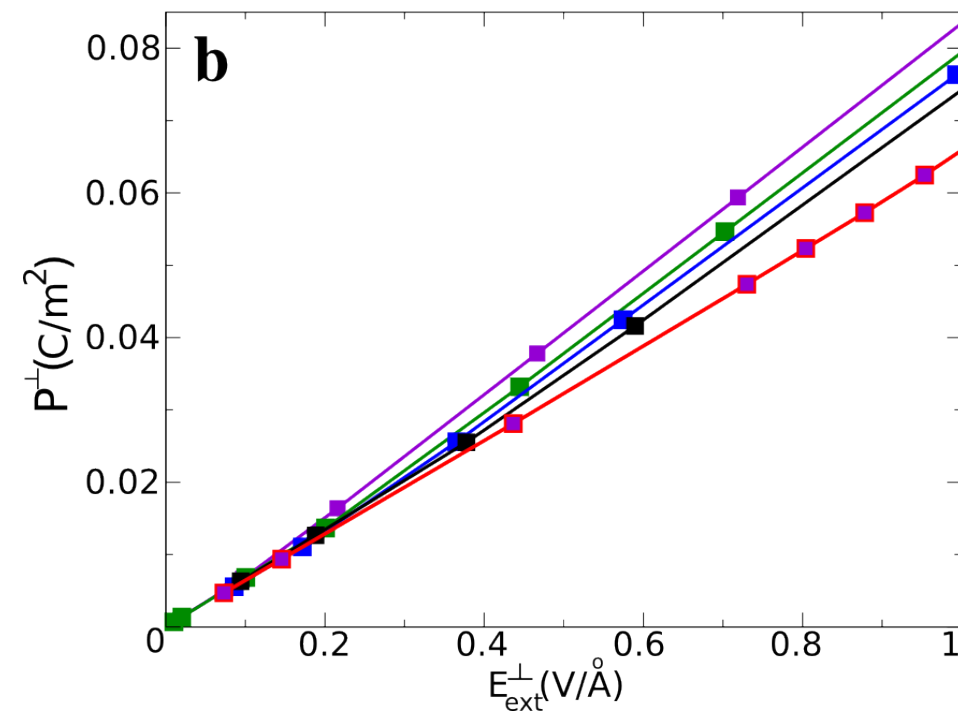
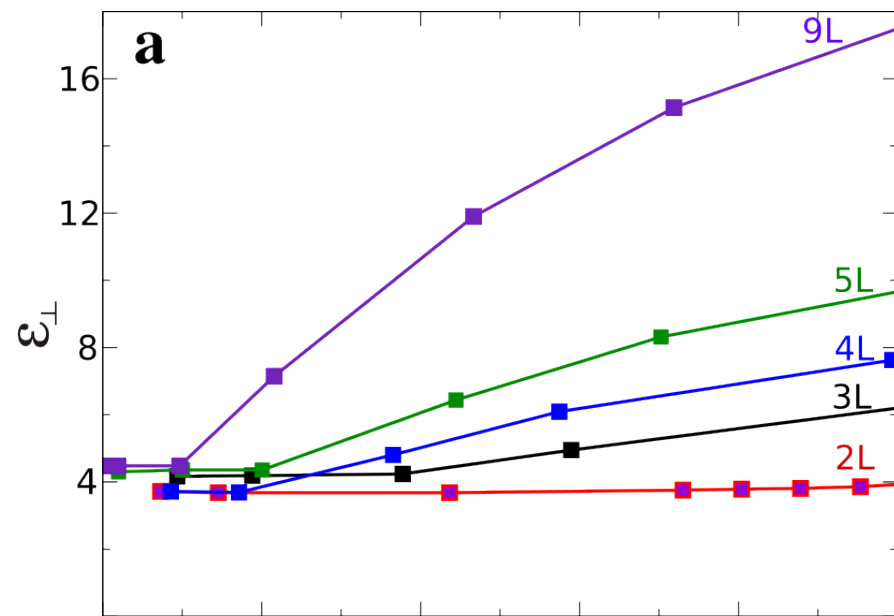
Radisavljevic et al. *Nat. Nanotech.* (2011) **6**, 147
Kim et al. *Nat. Communications* (2012) **3**:1011

2D-polymers

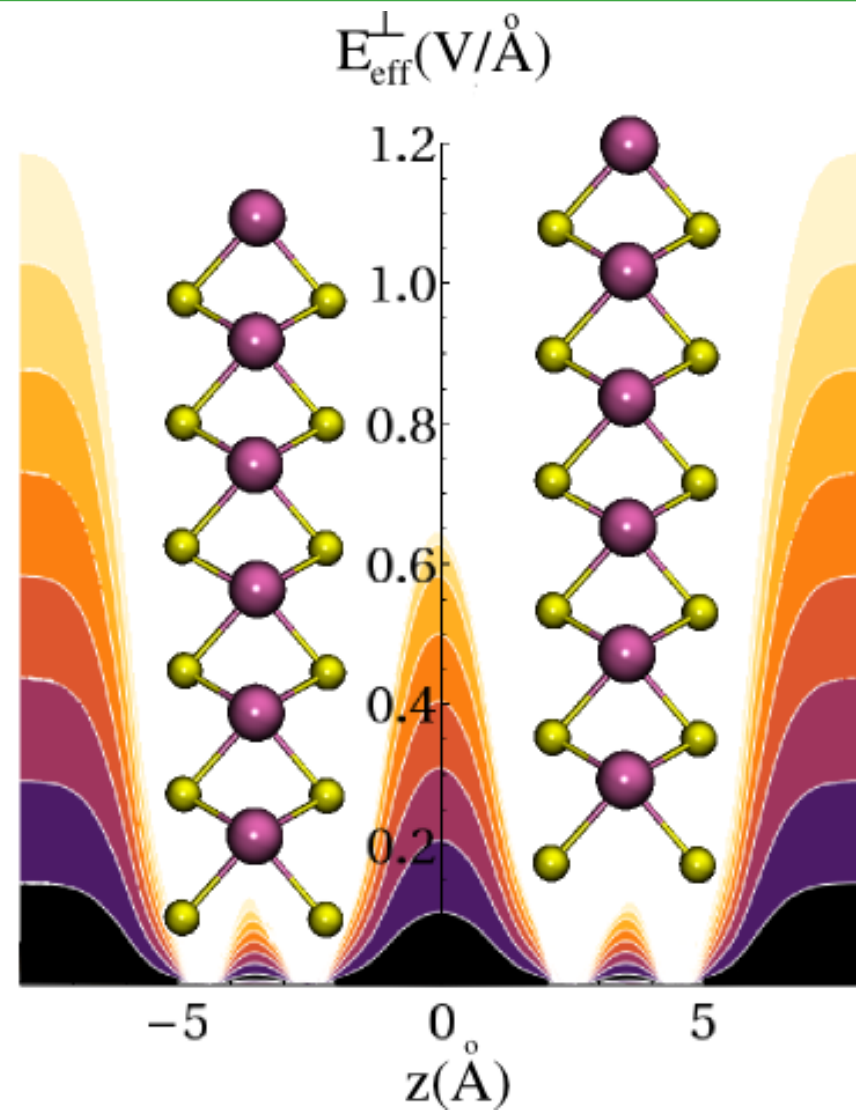


Nam et al. *Nat. Materials* (2010) **9**, 454

Electric-field control of the dielectric constant of MoS₂ materials

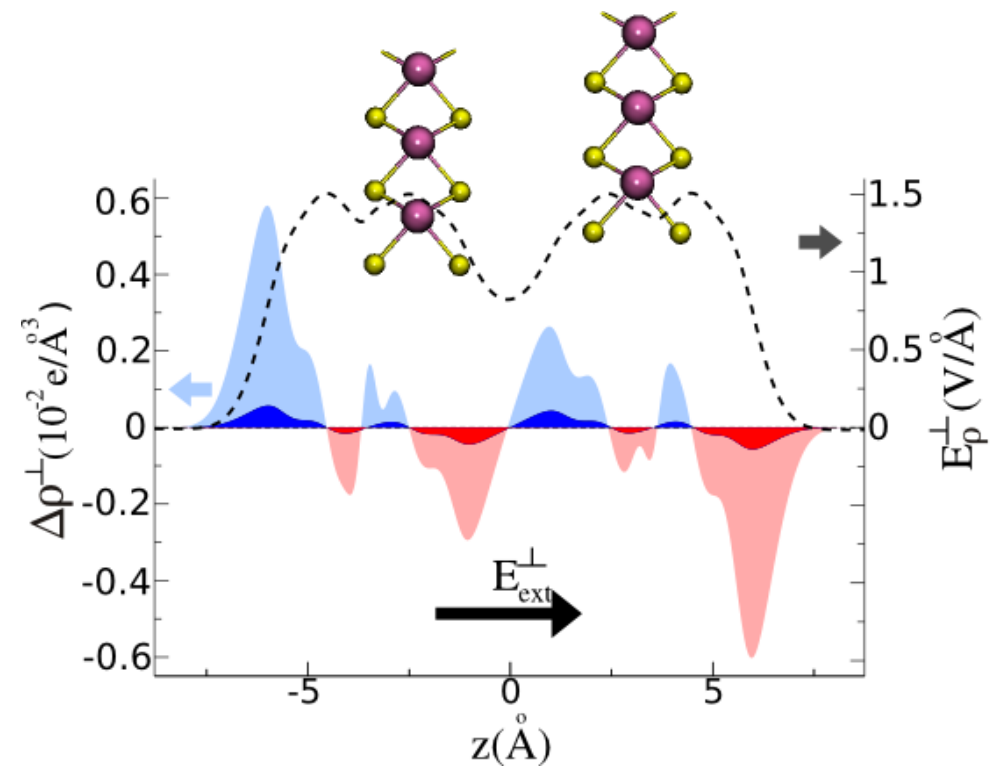


Similar behaviour as seen for multilayer graphene



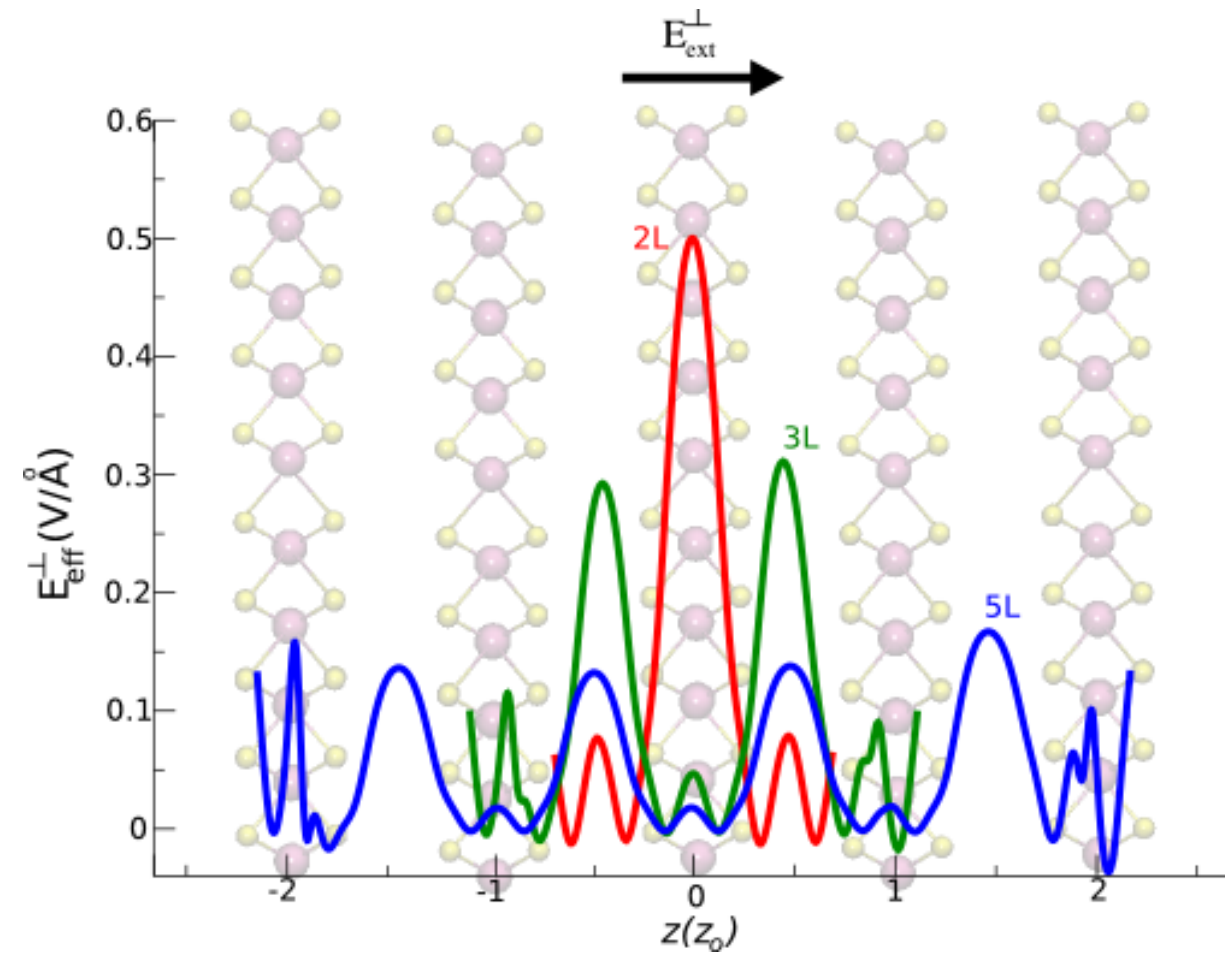
The polarization charge as well as the response field are bias dependent.

Only for small fields ($< 0.10 \text{ V}/\text{\AA}$) the static dielectric constant is really constant.



Many similarities with graphene are recovered.

Non-linear screening in multilayer MoS₂

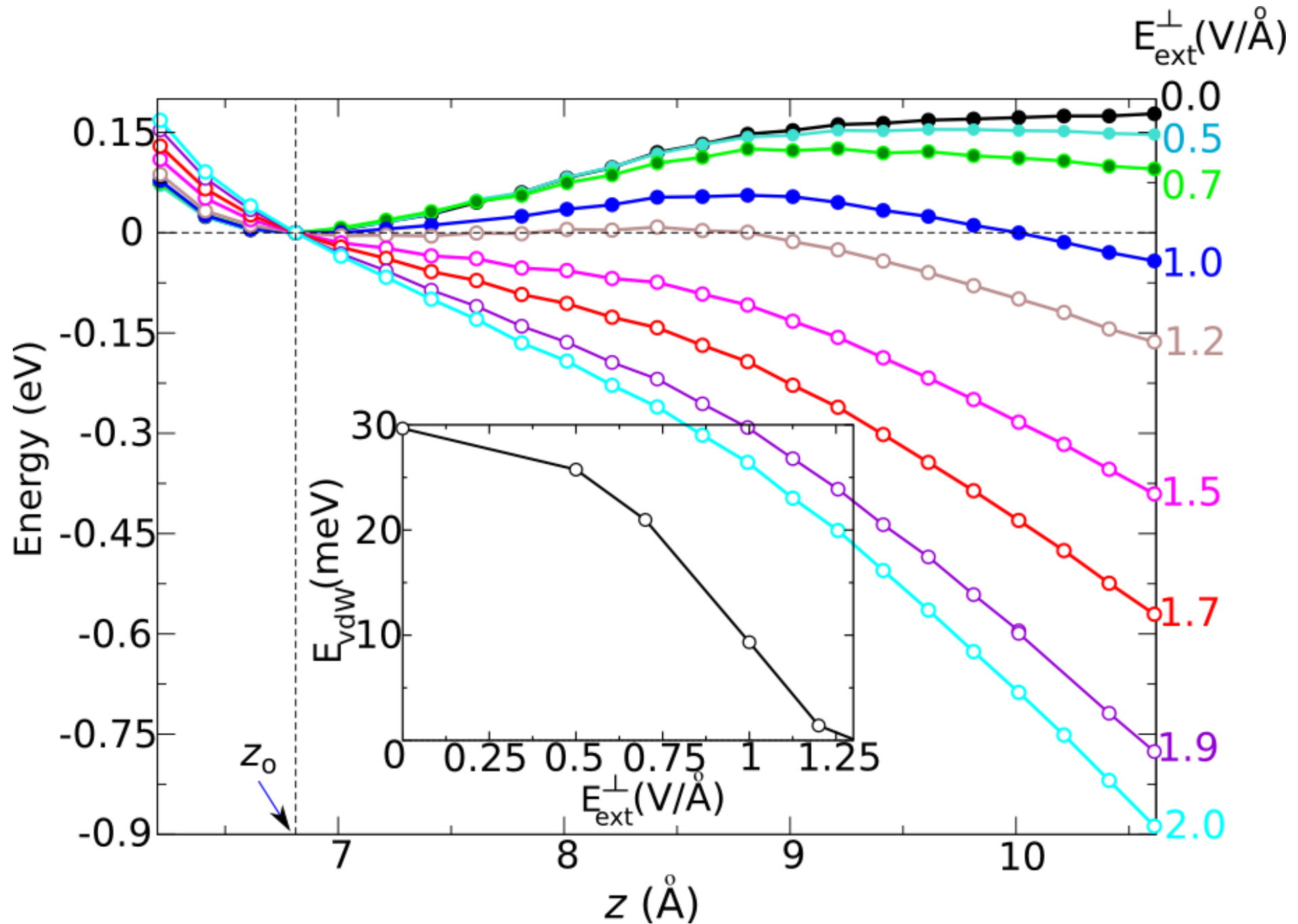


The electric field inside of the material decreases as a function of the number of layers.

The thicker the structure (more layers) the larger the value of ϵ

Oscillations are observed in-between S-Mo-S layer

Electrostatic exfoliation is also possible with MoS_2 at lower fields in comparison to Graphene



Questions? Comments?

