

### Follow-Up Notes on Meeting 2

Several conversations with people after last week's meeting led to new counterexamples to Rosen's proposals about the principles governing grounding:

- *strong non-monotonicity*: For any facts  $[p]$  and  $[q]$  and any set of facts  $\Gamma$  such that  $[q] \notin \Gamma$ , if  $[p] \leftarrow \Gamma$ , then not:  $[p] \leftarrow [q], \Gamma$ .

*Tom Donaldson's counterexample*: If it is true that  $p$  and that  $q$ , then we have:

$$[p \vee (p \& q)] \leftarrow [p]$$

$$[p \vee (p \& q)] \leftarrow [p], [q]$$

The first of these follows from Rosen's ( $\vee$ ), and the second follows from ( $\&$ ) together with transitivity.

- ( $\vee+$ ): If it is true that  $p \vee q$ , then either  $[p \vee q] \leftarrow [p]$  or  $[p \vee q] \leftarrow [q]$ .

*Said Sallant's counterexample*: If the future is (metaphysically) open, then if we let

$$\langle p \rangle = \langle \text{There will be a sea battle tomorrow} \rangle,$$

the following can all be the case:

$$\langle p \vee \neg p \rangle \text{ is true;}$$

$$\langle [p \vee \neg p] \leftarrow [p] \rangle \text{ is false (since } \langle p \rangle \text{ is not true); and}$$

$$\langle [p \vee \neg p] \leftarrow [\neg p] \rangle \text{ is false (since } \langle \neg p \rangle \text{ is not true).}$$

- ( $\exists$ ): If it is true that  $\varphi(a)$ , then  $[(\exists x)\varphi(x)] \leftarrow [\varphi(a)]$

*a counterexample inspired by a conversation with Sharon Berry*: Suppose for reductio that ( $\exists$ ) holds. Now let

$$[p] = [\text{Something is true}].$$

By ( $\exists$ ), we have:

$$[\text{Something is true}] \leftarrow [\langle p \rangle \text{ is true}].$$

It is also extremely plausible to hold:

$$[\langle p \rangle \text{ is true}] \leftarrow [p].$$

So, by transitivity, we have:

$$[p] \leftarrow [p].$$

But this contradicts strong irreflexivity. (Indeed, it contradicts weak irreflexivity.)