

# **Cost-Sensitive Batch Mode Active Learning: Designing Astronomical Observation by Optimizing Telescope Time and Telescope Choice**

**Xide Xia**

**Advisor: Pavlos Protopapas**

**Finale Doshi-Velez**



*Planet*  
*Nebula*  
*Constellation*  
*Star cluster*  
*Galaxy*  
...  
...

***Questions:***

1. Which instance should be selected?
2. How about observing multiple instances at one time?
3. What's the cost?
4. Which telescope should we choose?

# 1. Which instance should be selected? - *Active Learning!*

## Single-instance Active Learning

Suppose we have a labeled set  $S$  of  $K$  input features  $x_k$  and labels  $y_k$ :  $\{(x_0, y_0), \dots, (x_{K-1}, y_{K-1})\}$ . Our goal is to select the next instance  $x_K$  to label to minimize the expected loss on the remaining data  $x_n \ni S$ :

$$(2.1) \quad \min_K \mathbb{E}_{y_K, y_n \ni S} \left[ \sum_{x_n \ni S} L(\hat{y}_n, y_n) \right]$$

where  $\hat{y}_n = f_S(x_n)$ ,  $f_S(x)$  is the classifier trained with the labeled set  $S$ , and  $L(\cdot)$  is the loss function.

# 1. Which instance should be selected? - *Active Learning!*

## Score Function: Expected Uncertainty Reduction

Our goal is to choose instances to minimize the total label uncertainty across all the unlabeled instances.

$$(3.3) \quad \min_{x_k} \mathbb{E}_{y_k} \left[ \sum_{x_n \in S \cup x_k} 1 - (p(\hat{y}_n)) \right]$$

where  $p(\hat{y}_n)$  is the probability of the most probable label for the observation  $x_n$ .

# 1. Which instance should be selected? - *Active Learning!*

## Pre-Clustering:

We assume that each point  $x_k$  in the cluster  $c$ , if it were to be labeled, will label some proportion of its cluster, depending on how close it is to the center of its cluster.



$$(3.5) \quad \text{score}(x_k) = \text{rep}(x_k, c_{x_k}) \sum_{x_i \in c} 1 - p(\hat{y}_i)$$

$$(3.4) \quad \text{rep}(x_k, c_{x_k}) \propto \exp(-\text{dist}(x_k, c_{x_k}))$$

where  $c_{x_k}$  is the center of the cluster of  $x_k$ .

## 2. How long it will take to observe the selected ones? - *Cost-sensitive Active Learning*

$$\min_K \mathbb{E}_{y_K, y_n \ni S} \left[ \sum_{x_n \ni S} L(\hat{y}_n, y_n) \right]$$

subject to  $C(S) \leq B$ .

**Observing time cost:**

$$C(\{x_i\}) \propto \sum_{x_i \in \{x_i\}} 10^{0.4 \text{mag}_{x_i}}.$$

$$(4.11) \quad \text{score}_{\text{cost}}(\{x_i\}) = \text{score}(\{x_i\}) + \lambda C(\{x_i\}).$$

where  $\lambda$  is the weight of cost that depends on how much budget we have.

## 2. How long it will take to observe the selected ones?

- *Cost-sensitive Active Learning*

Data Sets:

- *MACHO (3063\*64)*

- *EROS (8317\*64)*

Table 1: MACHO Data Set Composition

	Class	Number of objects
1	Non variable	966
2	Quasars	59
3	Be Stars	101
4	Cepheid	610
5	RR Lyrae	255
6	Eclipsing Binaries	126
7	MicroLensing	580
8	Long Period Variable	365

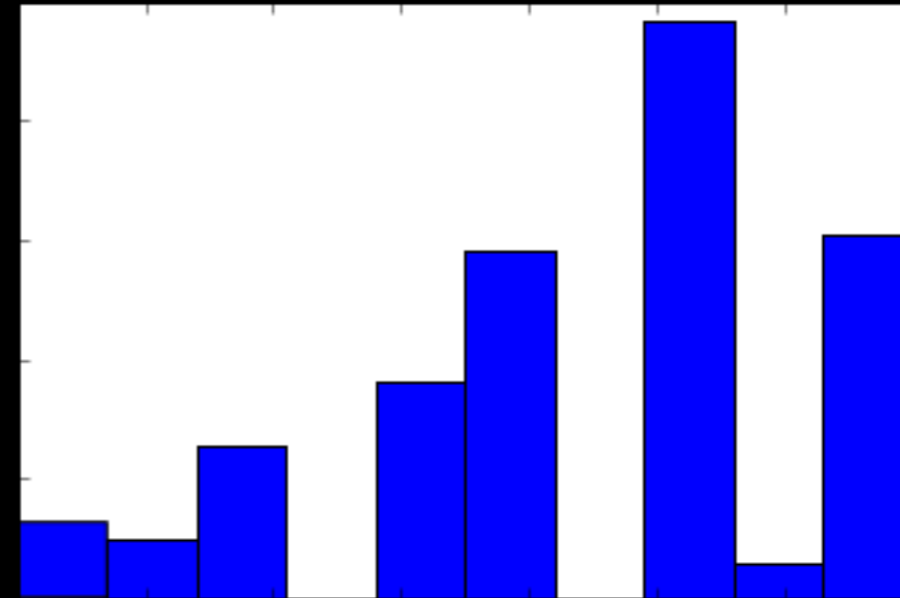
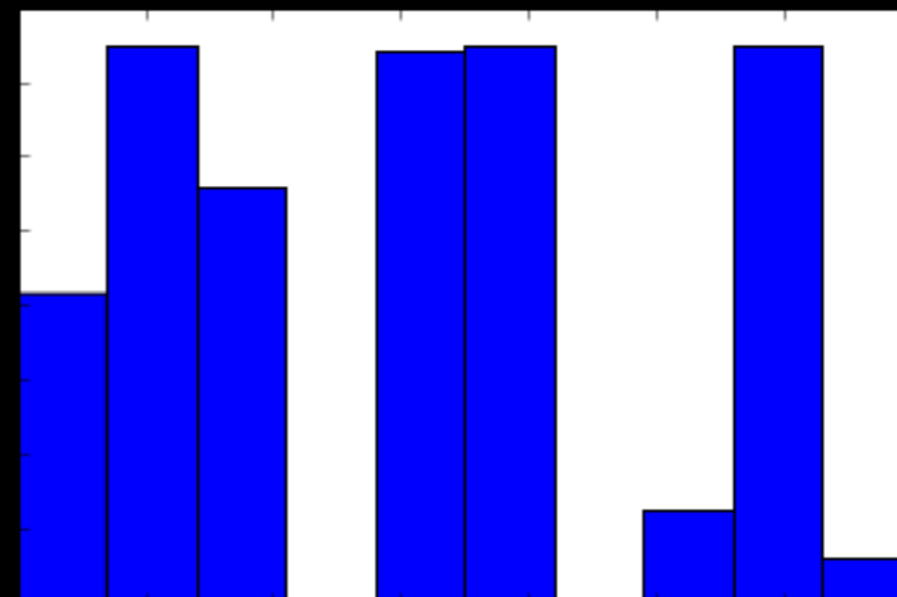


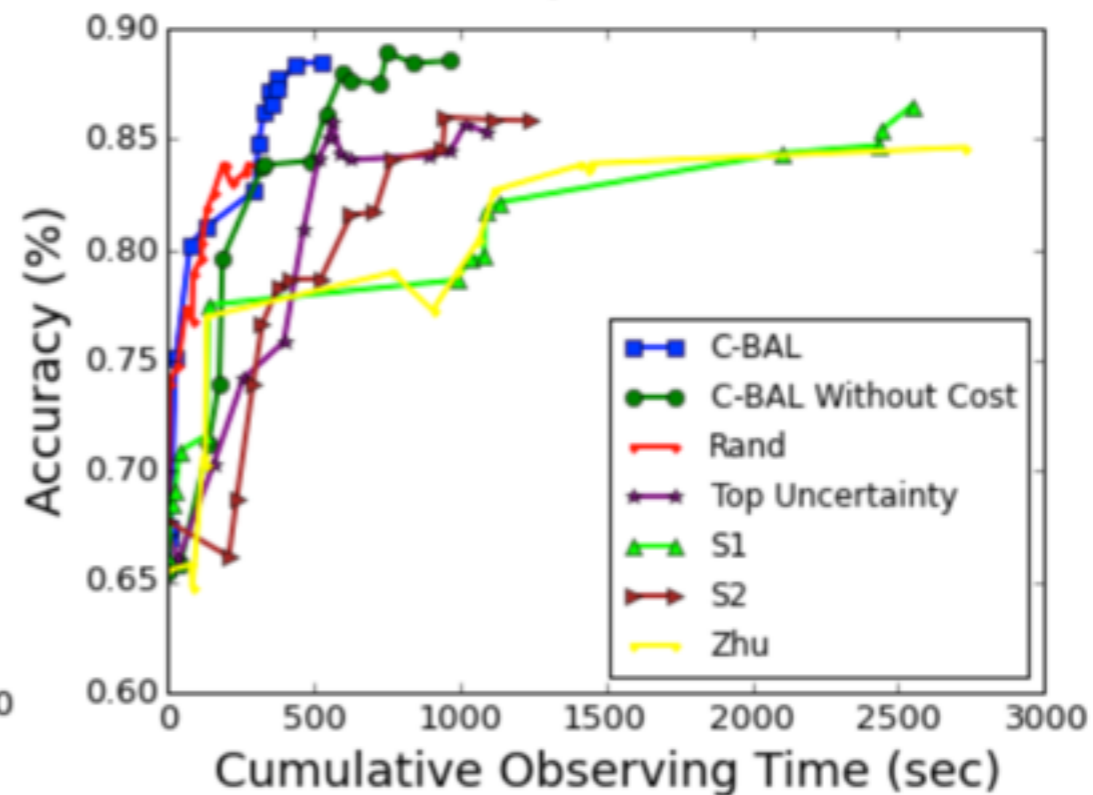
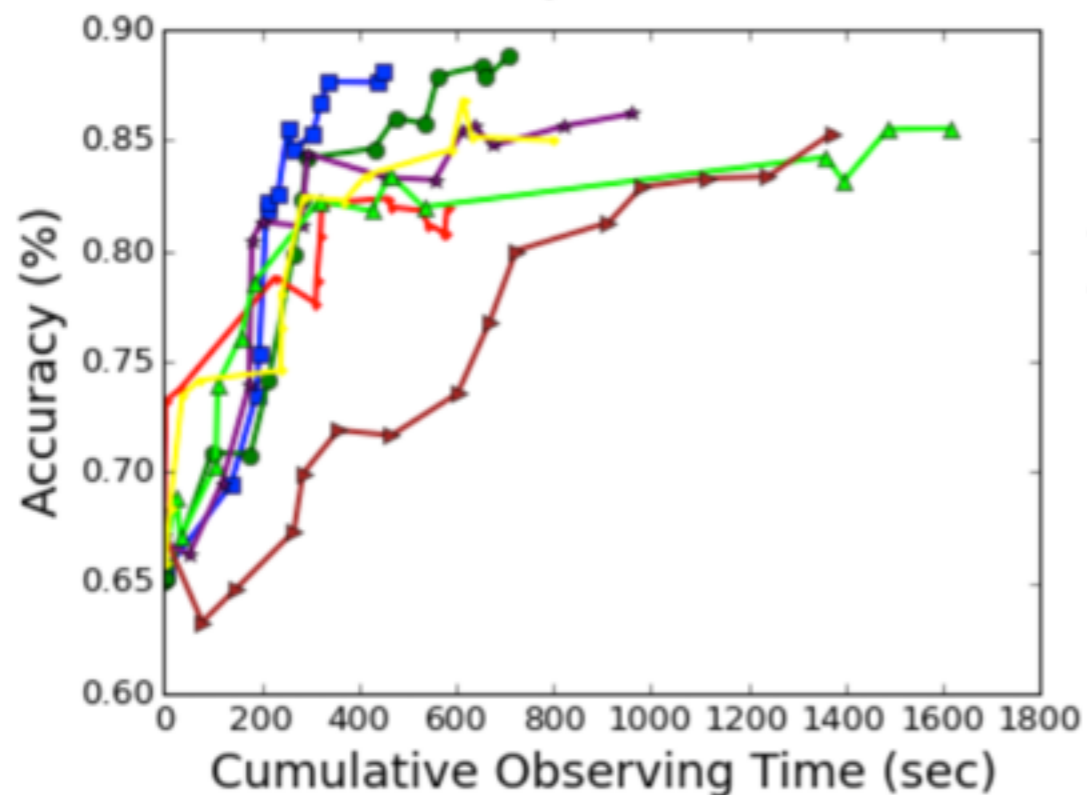
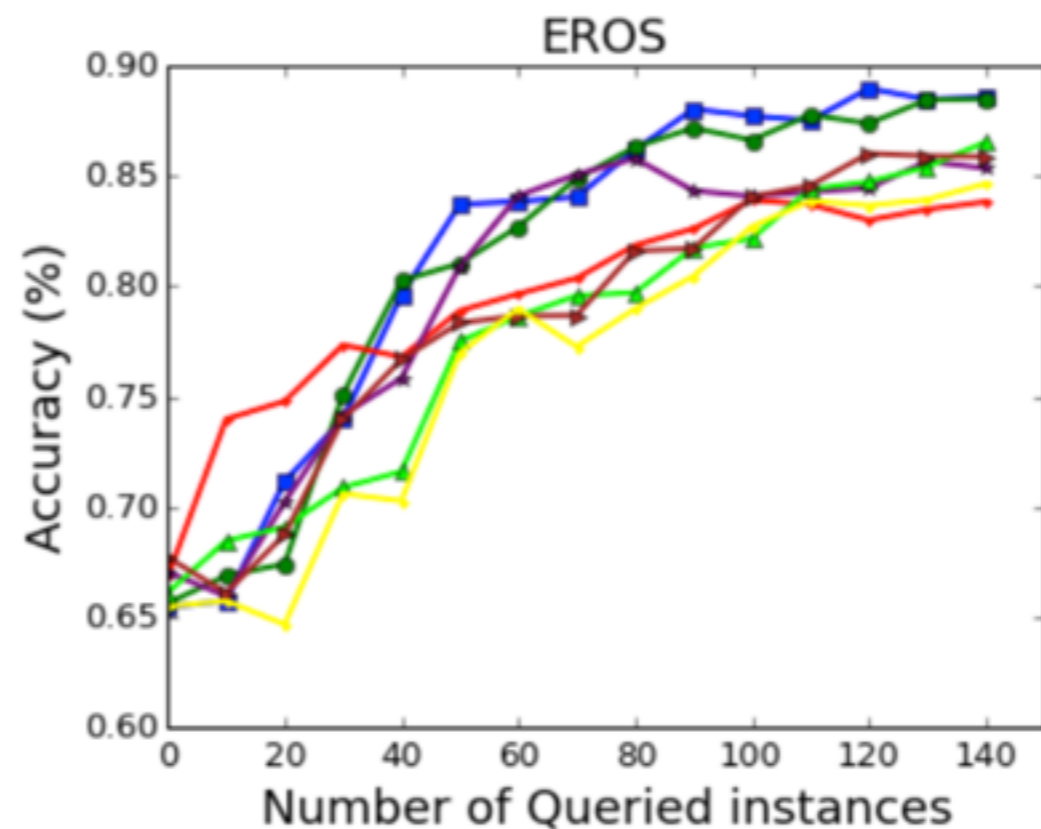
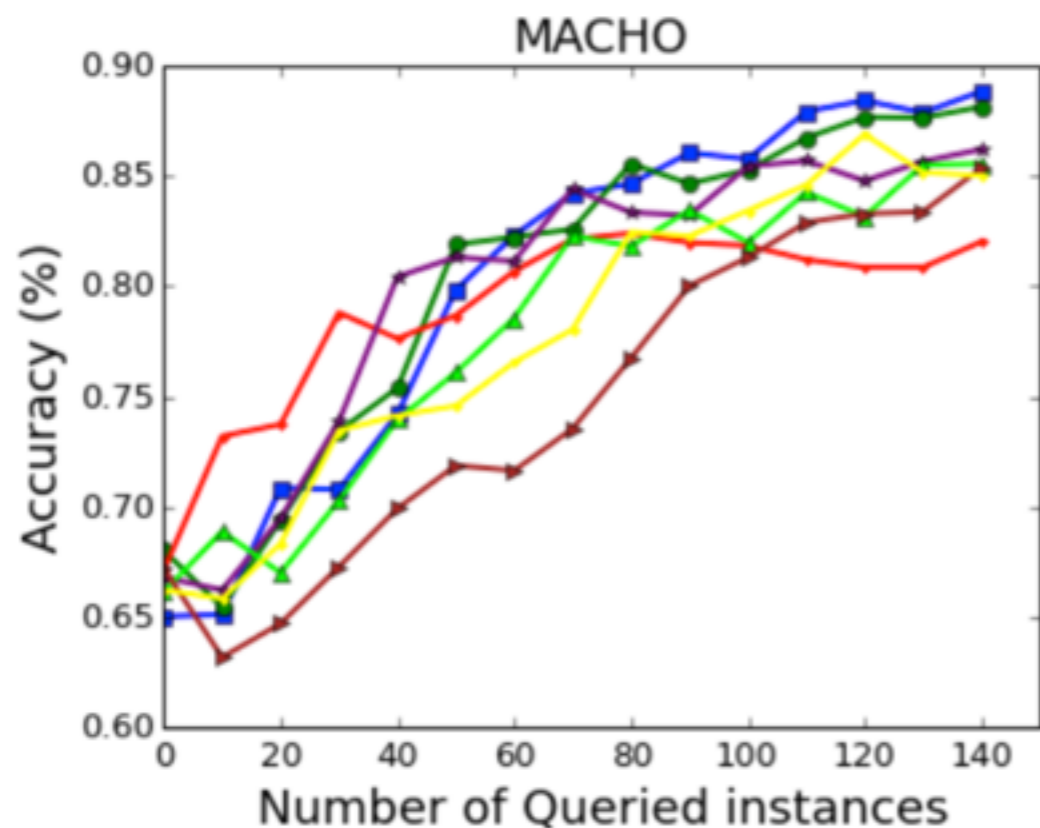
Table 2: EROS Data Set Composition

	Class	Number of objects
1	BV	829
2	CEP	1500
3	DSCT	1114
4	EB	1484
5	LPV	1500
6	QSO	251
7	RRLYR	1499
8	T2CEP	123



## 2. How long it will take to observe the selected ones?

- *Cost-sensitive Active Learning*



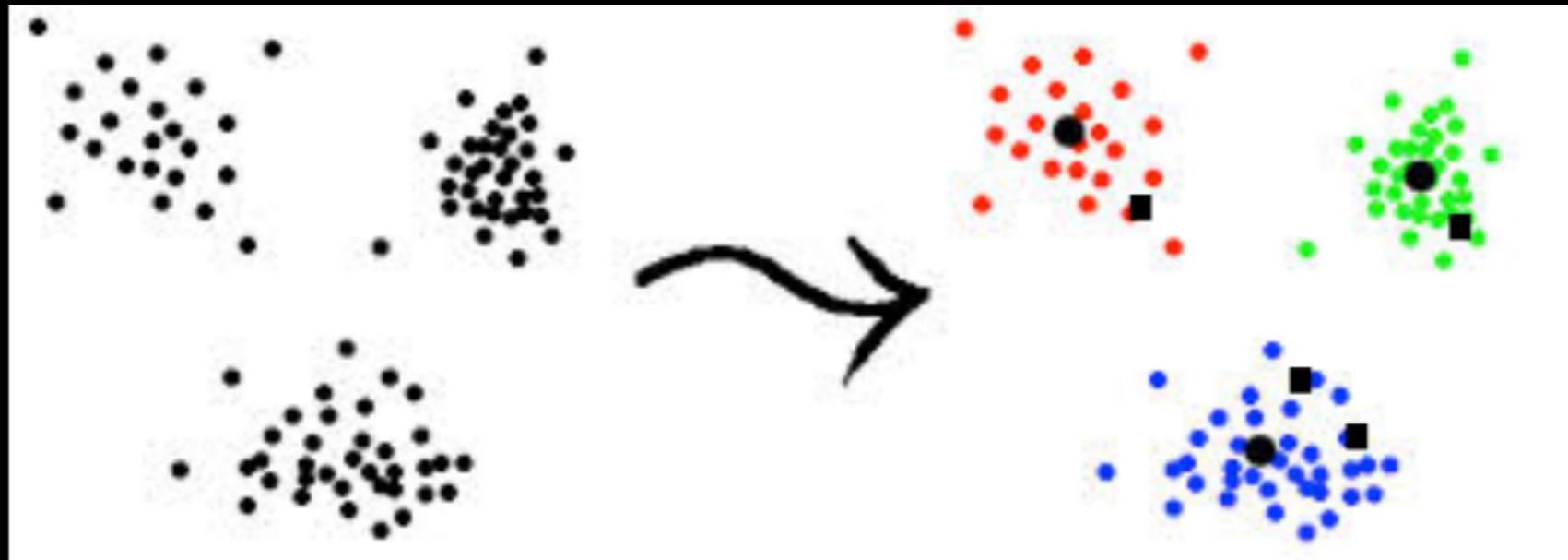


### 3. How about selecting multiple instances at one time? - *Batch Mode Active learning*



### 3. How about selecting multiple instances at one time?

- *Batch Mode Active learning*



$$\text{score}(p_i) = \sum_{c \in p_i} \max_{x_k \in c \cup p_i} (\text{rep}(x_k, c)) \sum_{x_i \in c} 1 - \max(p(\hat{y}_i))$$

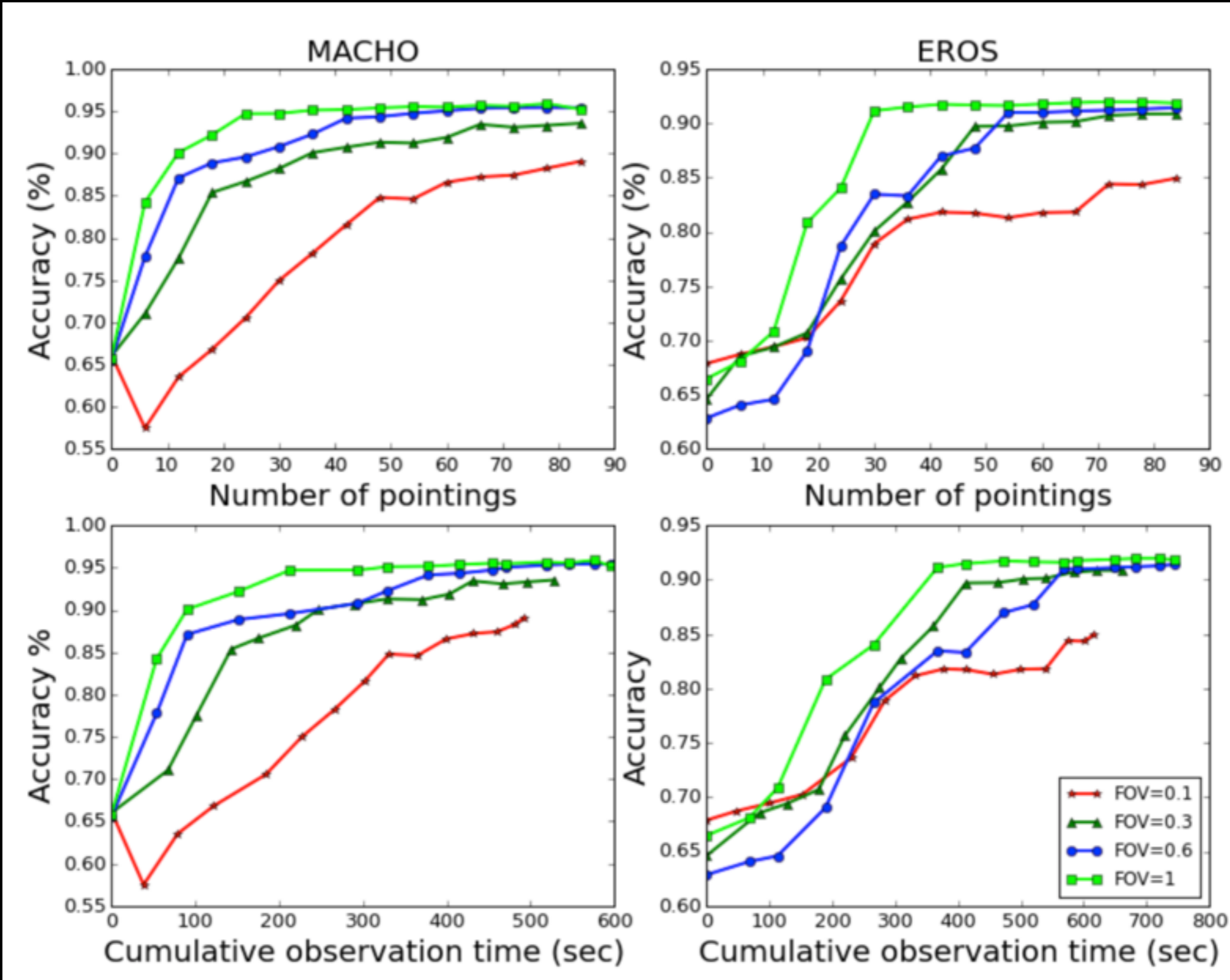
where  $c \in p_i$  are all the clusters associated with the observations in the pointing  $p_i$ .

### 3. How about selecting multiple instances at one time? - *Batch Mode Active learning*



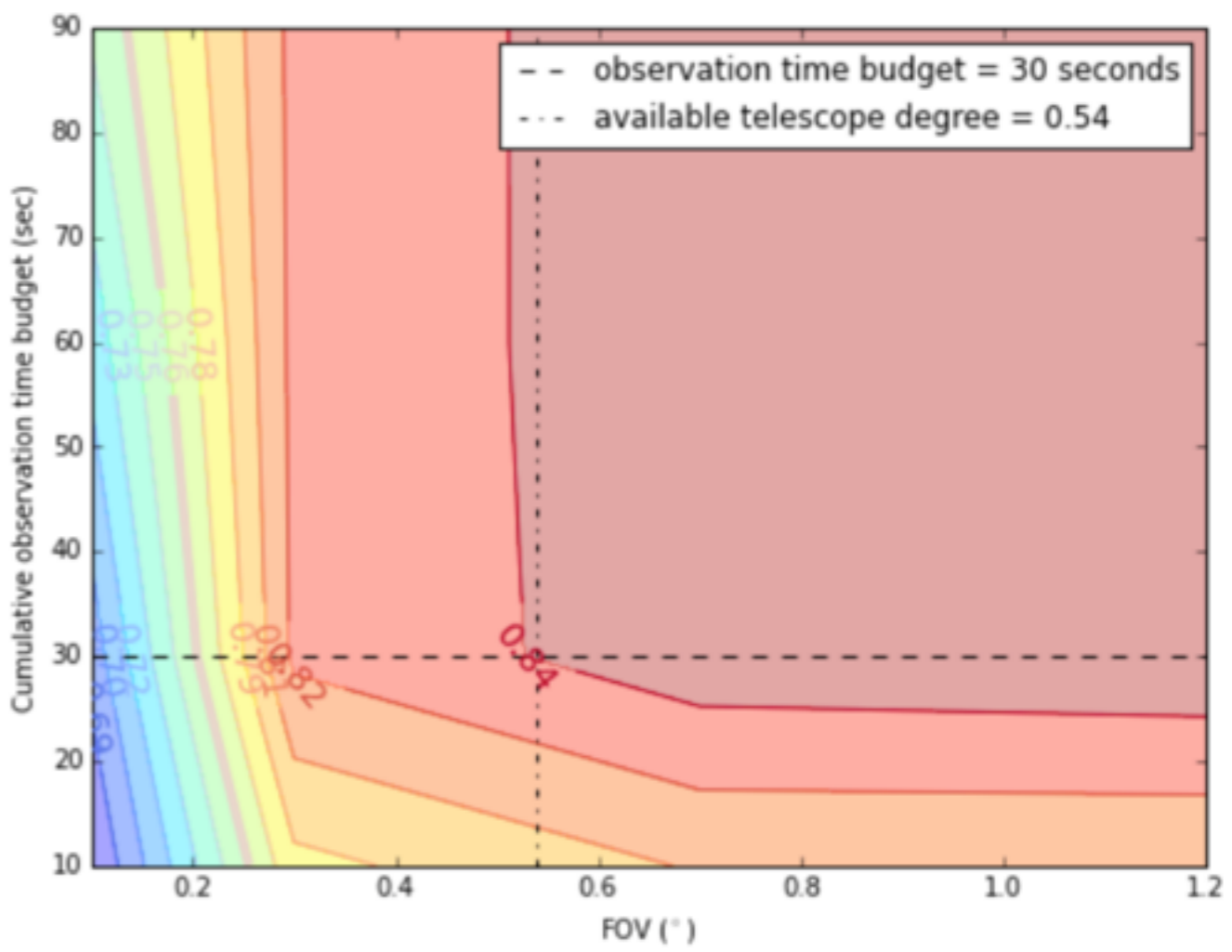
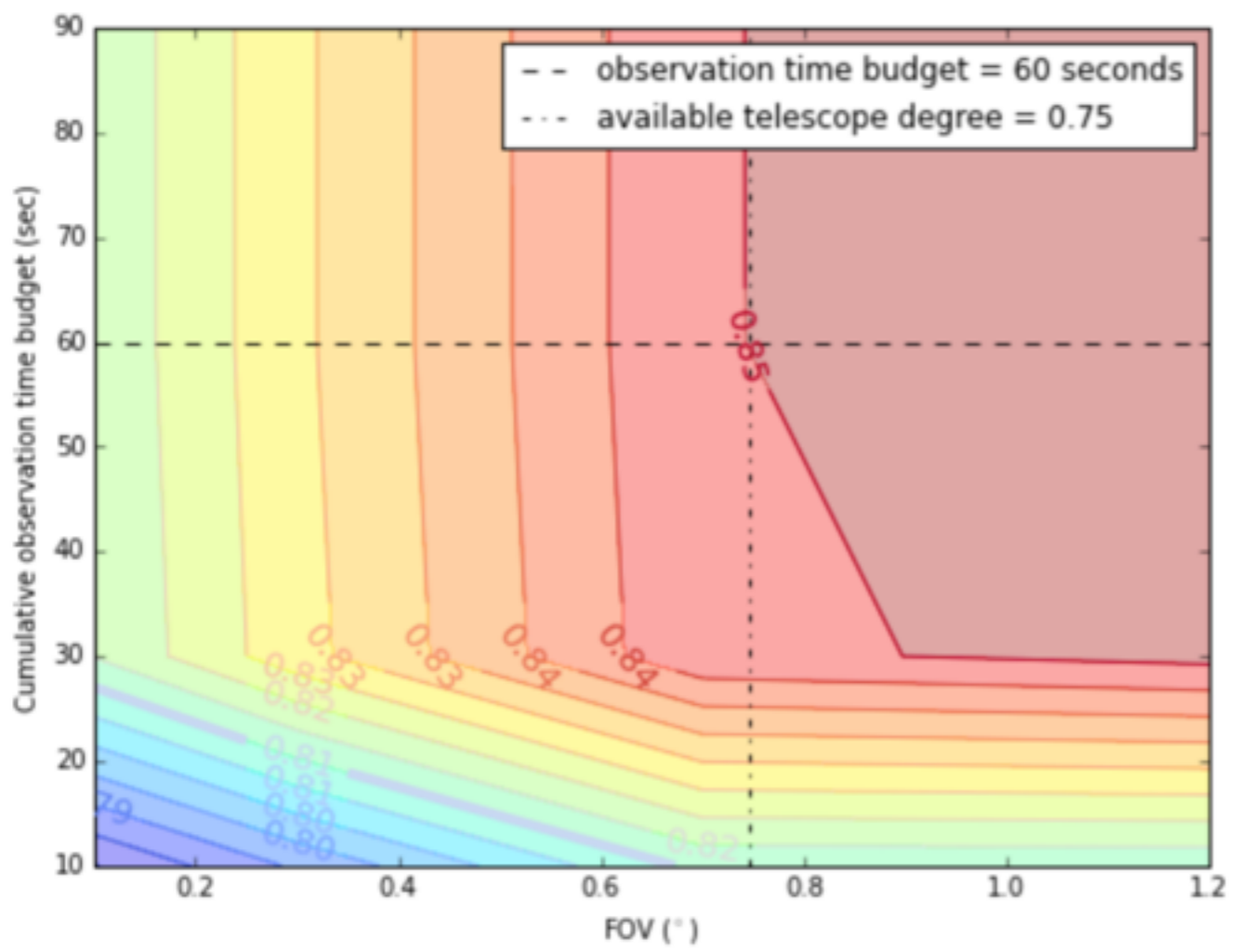
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# 3. How about selecting multiple instances at one time?

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## 4. Which telescope?

- *Application of the proposed Cost-Sensitive Batch Mode Active Learning*

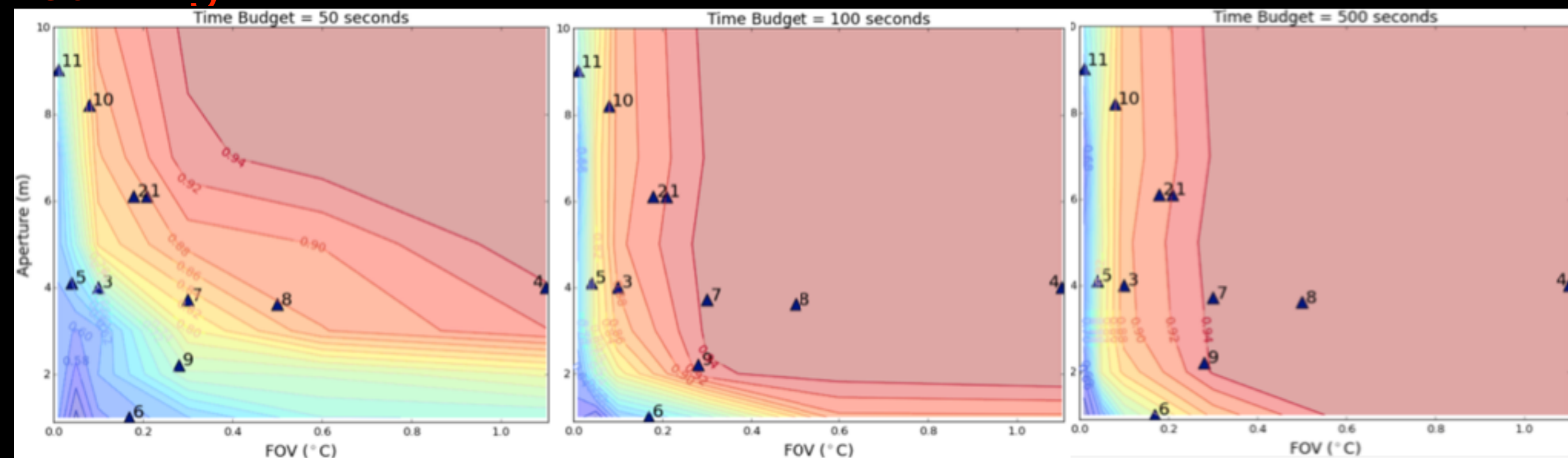
$$C(\mathbf{x}, T) = \frac{\mu}{R_T^2} 10^{0.4mag_x}.$$

Table 3: Real-World Telescope Data

	Country	Observatory	Telescope	Instrument	Apperture	FOV (arcmin)
1	Chile	Las Campanas	Bode	Mega Cam	6.1	25*25
2	Chile	Las Campanas	Bode	IMACS	6.1	21*21
3	Chile	Cerro Tololo	Blanco 4m	ISPI	4	10.25*10.25
4	Chile	Cerro Tololo	Blanco 4m	DECAM	4	132*132
5	Chile	Cerro Tololo	SOAR	SOAR Imager (SOI)	4.1	5.2*5.2
6	Chile	Cerro Tololo	SMARTS 1m	Y4K CAM	1	20*20
7	Tuscon	Kitt Peak	Mayall 4m	KOSMOS	3.7	36*36
8	Hawaii	Mauna Kea	CFHT	Mega Cam	3.6	60*60
9	Chile	La Silla	MPG/ESO 2.2-metre	WFI	2.2	33*33
10	Chile	Paranal	Very large telescopeX4	MUSE	8.2	1*1
11	Chile	Gemini	Gemini 9m	GSAOI	9	1.333*1.333

# 4. Which telescope?

- Application of the proposed Cost-Sensitive Batch Mode Active Learning



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